¹ Design of ferromagnetic shape memory alloy composite made of Fe and ² TiNi particles

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AQ: 9 Ferromagnetic shape memory alloy (FSMA) particulate composites have been processed by spark plasma sintering with varying weight fractions of NiTi (51 at. % Ni) and Fe powders. An assortment 10 11 of experimental processing conditions such as temperature, pressure, duration of sintering, and heating rate has been chosen to characterize the relative density and superelasticity behavior of the 12 said FSMA composite. The effective magnetic properties of these processed composites have also 13 been experimentally estimated using vibrating sample magnetometry. An attempt at predicting the 14 effective magnetic properties of the FSMA composite based on Eshelby's inhomogeneous inclusion 15 method in conjunction with Mori-Tanaka's mean-field theory for larger concentrations of the 16 ferromagnetic phase has also been presented in this study. The analytical model results thus obtained 17 are compared with experimental data resulting in reasonably good agreement. © 2007 American 18 Institute of Physics. [DOI: 10.1063/1.2775289] 19

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21 INTRODUCTION

Ferromagnetic shape memory alloys (FSMAs) have attracted strong attention from the material science community in particular and actuator designers in general mainly due to their fast response and large strain capabilities. Popular FS-MAs that have been extensively studied include NiMnGa (Refs. 1–5) and FePd (Refs. 6–8) systems. There are three mechanisms of actuation associated with FSMAs under magpetic field, namely, (i) magnetic-field-induced phase transforand matter variant rearrangement, and (iii) hybrid mechanism.⁹ The first two mechanisms are operative under constant magnetic field, while the third mechanism is based an on gradient magnetic field.

An earlier study by Kato *et al.*,⁶ which was based on 35 thermodynamics, made a preliminary estimate of the mag-36 netic energy necessary to induce a phase transformation in 37 FSMAs. The general conclusion was that a large magnetic 38 (*H*) field was required for the phase change to take place for 39 both NiMnGa and FePd systems. Therefore, the first mecha-40 nism was deemed unsuitable for use in designing compact 41 actuators which may need a small and portable electromag-42 net system as a driving unit.

43 The second mechanism involves inducing the strain in a 44 FSMA with 100% martensite phase and subjecting it to a 45 *constant* H field which acts on the magnetic moments in 46 magnetic domains that exist in the martensite phase so as to 47 rotate them along the easy axis, i.e., c axis in the case of 48 NiMnGa and FePd systems. Even though the strain induced 49 by the second mechanism is very large, the corresponding 50 stress remains as modest as several megapascals under mod-51 est applied magnetic flux density (1 T). Thus, the use of the second mechanism may be advantageous in designing an ac- ⁵² tuator with large strain capability. 53

The third mechanism,^{6,9} termed as "hybrid mechanism," 54 is based on a set of chain reactions. An applied magnetic flux 55 (or field) *gradient* induces magnetic force which causes 56 stress induced martensite phase transformation resulting in 57 the phase change from stiff austenite to soft martensite 58 phase, thereby leading to large displacement. The advantages 59 of this are large stress (100 MPa in the case of FePd), modest 60 to intermediate strain, and fast actuation time. Physically, 61 such a phase change can be achieved by approaching a com- 62 pact and portable magnetic field gradient. Therefore, the third 64 hybrid mechanism is considered most suited for use in de- 65 signing compact actuators with large force capability. 66

However, the cost of processing FSMAs such as FePd is 67 very expensive. On the other hand, superelastic shape 68 memory alloys have high mechanical performances and large 69 transformation strain and stress capabilities. However, the 70 speed of superelastic SMAs by changing temperature is 71 slow. If a ferromagnetic shape memory alloy composite com- 72 posed of a ferromagnetic material (soft magnet) and a super- 73 elastic SMA can be developed and such a composite be ac-74 tuated based on the hybrid mechanism, cost-effective and 75 high-speed actuators can be designed. This has been the un- 76 derlying motivation of the present work. In the design of 77 such a composite, the requirements have been identified as 78 follows: no plastic deformation of the ferromagnetic material 79 and large transformation strain in superelastic SMA. In order 80 to achieve the optimum microstructure of FSMA composites 81 for actuator design, numerical models such as FEM or an 82 analytical approach needs to be developed. Such an analyti- 83 cal model for FSMA composites with the aim of optimizing 84 the microstructure of FSMA composite with emphasis on 85

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⁸⁶ laminated composite and helical shaped composite has been **87** developed earlier.¹⁰

This paper reports the analytical modeling of the mag-88 89 netic properties of FSMA particulate composites and also 90 elucidates the experimental work of processing such com-91 posites. The validity of the proposed model has been estab-92 lished by comparison with the measured magnetic properties 93 of the composite.

This paper has been organized as follows. The process-94 95 ing of particulate Fe-TiNi composite using spark plasma sin-96 tering (SPS) with various concentrations of Fe will be dis-97 cussed in Sec. II, followed by the analytical model for 98 predicting the effective magnetic properties of the particulate 99 composites in Sec. III. A brief discussion of the results and 100 validity of the proposed model will be presented in Sec. IV, 101 followed by some conclusions in Sec. V.

102 PROCESSING OF PARTICULATE Fe-TINI COMPOSITE

103 The FSMA composite used in the present work is a "par-104 ticulate composite" composed of particulate powders of 105 SMA (TiNi) and ferromagnetic material (soft magnetic Fe). 106 The ordinary metallurgical route for processing particulate 107 composites using powders, i.e., standard sintering, produces 108 unwanted reaction products, destroying the original proper-109 ties of the constituent SMA and ferromagnet. In order to 110 circumvent unwanted reaction by-products, SPS machine 111 was used to process the particulate composites. The SPS ma-112 chine has been recently installed at the Center for Intelligent 113 Materials and Systems (CIMS), University of Washington, 114 Seattle (Dr. Sinter SPS-515S, Sumitomo Coal Mining Co., 115 Japan). Figure 1 is a schematic of the SPS equipment and the **116** sintering process.¹¹ It has been reported that sintering con-117 ducted using the SPS machine under high temperatures and 118 pressure of around 25-50 MPa for as short a time as 5 min 119 in near vacuum conditions ($\sim 5-6$ Pa) followed by rapid 120 cooling using argon gas produces remarkably good results.¹² AQ: 121 In fact, as shown earlier, due to the short sintering time, the 122 samples produced at CIMS were of extremely high quality,

123 exhibiting low percentage of the intermetallics.¹² In this study, two different kinds of TiNi powders have 124 125 been used, namely, (1) large microsized TiNi (50.9 at. % Ni 126 and 49.1 at. % Ti) with average diameter of 212 μ m sup-127 plied by Sumitomo Metals, Japan, and (2) smaller nanosized 128 TiNi (51 at. % Ni and 49 at. % Ti) with average diameter of 129 100 nm supplied by Argonide, USA. An ingot of TiNi alloy 130 made by Sumitomo Metals, Osaka, Japan, was shipped to 131 Fukuda Metals, Kyoto, Japan, where plasma rotating elec-132 trode process (PREP) was used to process TiNi powders with **133** average diameter of 212 μ m. The particulate FSMA compos-134 ite specimens obtained using these powders were analyzed 135 for superelastic properties. The results would be presented at 136 a later point.

Iron metal powders of average particle size of 100 nm 137 138 were purchased from Argonide Inc. These were processed by 139 electroexplosion wire (EEW) technique. The chemical com-140 position of the iron wire (soft iron) used by Argonide to 141 make the metal powders is as follows: 0.78%-0.82% Mn,



FIG. 1. Schematic of (a) SPS device and (b) SPS process (Ref. 13).

<0.1% Cr, 0.08%–0.098% Ni, 0.66%–0.82% Si, 0.081%– ¹⁴² 0.082% Cu, <0.05% V, <0.01% Mo, <0.1% W, and carbon 143 whose content was not determined.

Due to the very small particle size (100 nm), these iron 145 powders are very reactive and special care was taken while 146 handling them. They were stored in vacuum sealed glass 147 vials in a dormant state mixed with hexane. The required 148 weight fractions of iron powder and TiNi powder were taken 149 in a glass vial and acetylene solution was added to it. The 150 glass vial was then put in a Thinky® mixer for 10 min to 151 obtain a homogeneous mixture of the powders on evapora- 152 tion of acetylene. The presence of acetylene not only aided 153 the mixing process but also prevented the iron powder from 154 getting oxidized. The homogeneous mixture was then placed 155 in the mold and sintering operation was conducted at the set 156 temperature, heating rate, and pressure. After sintering, each 157 sample was aged at 320 °C for 30 min. This aging condition 158 was chosen based on our previous results documented by 159 Zhao et al.¹⁹ 160

The results of the SPS processing of TiNi-Fe composites 161 are summarized in Table I. It was not possible to obtain 162 dense samples exhibiting superelasticity using nanosized 163 TiNi and Fe powders. The SPS processing of pure TiNi 164 samples using the nanosized TiNi powders under 900 °C and 165 50 MPa resulted in a high density TiNi specimen with its 166 porosity reduced to 2%. However, differential scanning calo- 167

	Sample ID SPS conditions, composition	Density measured (g/cm ³)	Theoretical density (g/cm ³)	Porosity (%)
Nanosized TiNi powder	600 °C×5 min×50 MPa, 100 K/min pure 51 at. % TiNi (100 nm) sample	4.16	6.40	35
	800 °C×5 min×50 MPa, 100 K/min pure 51 at. % TiNi (100 nm) sample	4.90	6.40	23.4
	850 °C×5 min×50 MPa, 100 K/min pure 51 at. % TiNi (100 nm) sample	5.55	6.40	13.3
	900 °C×5 min×50 MPa, 100 K/min pure 51 at. % TiNi (100 nm) sample	6.27	6.40	2.0
Microsized TiNi powder	600 °C×5 min×50 MPa, 100 K/min 51 at.% TiNi (212 µm)+33.33 wt% Fe (100 nm)	6.66	6.88	3.2
	700 °C×5 min×50 MPa, 100 K/min 51 at. % TiNi (212 μm)+33.33 wt % Fe (100 nm)	6.65	6.88	3.2
	800 °C×5 min×50 MPa, 100 K/min 51 at. % TiNi (212 μm)+33.33 wt % Fe (100 nm)	6.65	6.88	3.2
	700 °C×5 min×50 MPa, 100 K/min 51 at. $\%$ TiNi (212 μ m)+33.33 wt $\%$ Fe (74 μ m)	6.56	6.88	4.6
	900 °C×5 min×50 MPa, 100 K/min pure 51 at. % TiNi (212 μm) sample	6.26	6.40	2.1

TABLE I. Summary of SPS processed TiNi-Fe composites including 100% TiNi specimen.

¹⁶⁸ rimeter (DSC) (Perkin Elmer DSC-6) data of this TiNi speci¹⁶⁹ men did not exhibit any shape memory properties. In fact,
¹⁷⁰ x-ray diffraction (XRD) results of this TiNi specimen
¹⁷¹ showed TiNi₃ peaks which persisted after solution quenching
¹⁷² (see Fig. 2).¹⁵ These poor data of TiNi–Fe composite using
¹⁷³ nanosized TiNi powders led us to switch to larger microsized
¹⁷⁴ TiNi powers and nanosized Fe powders.

The results of SPS processed composites using this com-Tr6 bination is shown in the lower half of Table I where relative Tr7 densities of 97% and higher were obtained at reasonably low Tr8 sintering temperatures of around 700 °C. The iron particles Tr9 fill in the gaps between TiNi powders and form the matrix B0 phase of the composite after the sintering operation is com-B1 pleted. The microstructures of these sintered samples



FIG. 2. XRD data of 900 $^{\circ}C\times5$ min $\times50$ MPa, 100 K/min pure 51 at. % TiNi (100 nm) sample.

(700 °C SPS) are characterized using scanning electron microscopy (SEM) (T330A Hitachi). Figure 3 shows SEM images of a finely polished specimen after sintering. Structural 184 compositions of the samples are characterized using XRD. 185 The density is measured using a technique based on 186 Archimede's principle. 187

Determination of the transformation temperatures was 188 the next step in the material characterization process. This 189 was conducted by DSC tests with a heating/cooling rate of 190 10 °C. DSC experiments of the dense SPS specimen of 191 30 wt % TiNi (212 μ m diameter)+70 wt % Fe (100 nm) 192 AQ: processed at 700 °C, 5 min sintering time, and 50 MPa pres- 193 sure revealed the transformation temperatures as A_f (austen- 194 ite finish)=40°C, A_s (austenite start)=28°C, M_f (martensite 195 finish)=15°C, and M_s (martensite start)=30°C. These 196 TiNi-Fe composite specimens were then cut into cylinders of 197 5 mm diameter using electrical discharge machining (EDM). 198 The specimens were then tested using Instron model 8562 199 compression testing equipment. Figure 4(b) depicts a typical 200 stress-strain response of TiNi-Fe composite tested at 41 °C 201 (which is slightly higher than $A_f = 40 \,^{\circ}$ C) exhibiting a super- 202 elastic loop. 203

THEORETICAL MODEL

Composite magnetic permeability

In this section, Eshelby's equivalent inclusion method¹⁶ 206 in conjunction with Mori-Tanaka's mean-field theory¹⁷ has 207 been used to predict the effective magnetic properties (effec- 208 tive magnetic permeability and saturation magnetization) of 209 Fe–TiNi particulate composite. The first step involved defin- 210 ing a representative volume element (RVE) of the particulate 211 composite used in this study. To this end, the Fe phase was 212 chosen as the *f* phase or inhomogeneity and the TiNi SMA 213 phase was chosen as the *m* phase in the RVE, as depicted in 214 Fig. 5. The implications of such a definition will be discussed 215

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216 at a later point. Thus, the properties of the Fe phase are **217** represented by the subscript f in the evolution of Eshelby's **218** model while the properties of SMA are denoted by the sub-**219** script m, as depicted in Fig. 5. In the absence of inhomoge-**220** neities, the matrix SMA phase has the following property:

$$B = \mu_m \cdot H_m, \tag{1}$$

222 where *B* is the magnetic flux, H_m is the magnetic field inten-223 sity, and μ_m is the magnetic permeability of the matrix ma-224 terial. Equation (1) is reminiscent of an originally proposed 225 equivalent stress-strain formulation and now widely accepted 226 Eshelby model.¹⁶ For paramagnetic materials (such as TiNi 227 SMA material), the magnetic susceptibility χ typically lies in 228 the range of $10^{-3}-10^{-5}$; consequently, the magnetization 229 vector is very weak. Therefore, the magnetic field intensity 230 in the matrix phase takes the following form:¹⁸

$$H_m = H_o + M \Leftrightarrow H_m \approx H_o, \tag{2}$$

232 where H_o is the applied magnetic field intensity on the do-233 main under consideration as depicted in Fig. 5(a). Essen-234 tially, Eq. (2) conveys that due to the weak magnetization of 235 paramagnetic materials constituting the particulate phase of 236 the composite domain, the magnetic field intensity of the 237 matrix phase would be equal to the applied magnetic field 238 intensity. Equation (2) is valid for most paramagnetic mate-239 rials such as TiNi for which the magnetization vector M240 \approx 0. Equation (1) can thus be written as

$$B = \mu_m \cdot H_o. \tag{3}$$

 The error associated with neglecting the magnetization for paramagnetics has been found to be of the order of 0.01%, which is considered acceptable in the present work.¹⁸ Upon addition of an inhomogeneity (*f* phase), the flux and field vectors are related as follows in Ω (see Fig. 5):



FIG. 4. TiNi 30 wt % Fe composite specimen with SPS at 700 °C, 5 min, 50 MPa pressure, then aged at 320 °C for 1 h experimental results. (a) DSC data yielding A_f =40 °C, A_s =28 °C, M_s =30 °C, and M_f =15 °C. (b) Compression stress-strain curve of this composite specimen at 41 °C (= A_f), exhibiting to some extent superelastic loop.

FIG. 3. SEM images of the processed 33.33 wt % Fe (100 nm)+66.67 wt %, 51 at. % TiNi (212 μ m) particulate composite. (a) 150× magnification image, (b) 350× magnification image, (c) area composition map, and (d) line compositional map.

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FIG. 5. Analytical modeling of particulate TiNi–Fe composite based on Eshelby's equivalent inclusion method. (a) Schematic of the actual composite and (b) Eshelby's model.

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$$B + B_d = \mu_f \cdot (H_o + H_d) = \mu_m \cdot (H_o + H_d - H^*), \quad (4)$$

 where B_d and H_d are the disturbance flux and field vectors, respectively. Physically, H_d represents the demagnetization field characteristic of ferromagnetics. By definition for ferro-magnetics,

252
$$B = \mu_o \cdot (H_o + M - N \cdot M) = \mu_f \cdot (H - N \cdot M), \qquad (5)$$

 where *N* is the demagnetization factor, a tensor quantity de- pending only on the shape of the inhomogeneity, analogous to Eshelby's tensor *S* of the mechanical case. Choosing H_d = $-N \cdot M$ in Eq. (5), we get

257
$$H_d = N \cdot H^* = S^m \cdot H^*$$
 or $B + B_d = \mu_f \cdot (H_o + S^m \cdot H^*)$

258
$$= \mu_m \cdot (H_o + S^m \cdot H^* - H^*),$$

 where $S^m = N$ has been looked upon as the "Eshelby tensor" for the magnetic case. From Eq. (6), H^* can be solved. When the volume fraction of ferromagnetic inhomogeneities (*f*) be- comes finite, the interactions between ferromagnetic particles need to be accounted for. This has been accomplished by utilizing Mori-Tanaka's mean-field theory in the present case (atomic interaction effects have been neglected here). \overline{H} has been coined as the average magnetic field and Eq. (6) is modified as follows taking into account the volume fraction

269
$$B + B_d = \mu_f \cdot (H_o + \bar{H} + H_d) = \mu_m \cdot (H_o + \bar{H} + H_d)$$

270 $-H^*$ or $B_d = \mu_m \cdot (\bar{H} + H_d - H^*)$. (7)

271 Since the volume integration of H_d must vanish over the **272** entire domain, we get

273
$$\bar{H} = -f(H_d - H^*).$$
 (8)

274 Substituting in (7) and simplifying gives us

275
$$H^* = \{(\mu_f - \mu_m) \cdot [(1 - f)S^m + fI] + \mu_m\}^{-1} \cdot (\mu_m$$

276
$$-\mu_f) \cdot H_o.$$
 (9)

277 The corresponding concentration factor tensor A can be **278** evaluated as¹⁶

AQ:

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$$H_{f} = H_{o} + \bar{H} + H_{d} = H_{o} + H_{d}(1 - f) + fH^{*} = H_{o} + [(1 - f)S^{m} + fI] \cdot H^{*} \text{ or } H_{f} = A \cdot H_{o},$$
(10) 280

with

$$A = (I + [(1 - f)S^m + fI] \cdot \{(\mu_f - \mu_m) \cdot [(1 - f)S^m + fI]$$
 282

$$+\mu_m\}^{-1} \cdot (\mu_m - \mu_f)).$$
 283

Therefore,

$$\mu_c = \mu_m + f(\mu_f - \mu_m) \cdot A, \tag{11} \ 285$$

where μ_c represents the effective magnetic permeability of 286 the composite. Therefore, by knowing the properties of the 287 individual constituents of the composite and the geometry of 288 the inclusion, the composite magnetic permeability can be 289 evaluated. The computation of the demagnetization factor 290 has been done by many researchers and the values are therefore known.^{19,20} 292

Saturation magnetization (M_s^c)

The magnetic field intensity in the composite is evalu- 294 ated as follows: 295

$$H_c = (1 - f)\langle H_m \rangle + f\langle H_f \rangle,$$
²⁹⁶

where $\langle H_m \rangle$, $\langle H_f \rangle$ are volume averaged quantities (the angu- 297 lar brackets denote volume average over the entire domain). 298 Using the procedure outlined in Taya's book,²¹ the composite 299 magnetic field intensity takes the following form: 300

$$H_c = H_o + M_s^c = H_o + fM_s$$
 or $M_s^c = fM_s$. (12) 301

Here, M_s is the saturation magnetization of the ferroparticu- 302 late or the *f* phase of the composite and M_s^c represents the 303 composite saturation magnetization. Based on this formula- 304 tion, the magnetization at saturation M_s of TiNi–Fe compos- 305 ites processed at different weight fractions was predicted and 306 compared with the experimental values. The following sec- 307 tion outlines the results. 308

RESULTS

(6)

After characterizing the sintered samples with various 310 volume fractions as shown in Table I, the samples satisfying 311 the key requirements (DSC showing peaks of shape memory 312 properties) were chosen, namely, particulate TiNi/Fe pro- 313 cessed by SPS at 700 °C in vacuum for 5 min and 50 MPa 314 with 30%, 50% and 70% Fe by weight. The magnetization 315 (M)-magnetic field (H) curves of the composite specimens 316 were then measured using the vibrating specimen magneto- 317 meter (VSM) located at Tohoku University in order to com- 318 pare with the theoretical predictions. The model predictions 319 of saturation magnetization were compared with measured 320 magnetization at saturation, resulting in a good match. A 321 comparison of magnetization at saturation (M_s) of TiNi-Fe 322 composites between predictions and experimental data is 323 summarized in Table II. 324

The results of Table II have also been plotted in Fig. 6. 325 Table II and Fig. 6 show good agreement between the ex- 326 periment and the proposed analytical model despite the fact 327 that at lower wt % of Fe filler, the predicted M_s^c is slightly 328 Gururaja, Taya, and Kang

TABLE II. Comparison of predicted magnetization at saturation of TiNi-Fe particulate with measured data.

Fe	Volume fraction of Fe ^a	M_s^c (emu/g)		
(wt. %)	(f)	Expt.	Predicted	
30	0.26133	40	52.266	
50	0.4522	93	90.44	
70	0.6582	135	131.64	
100	1.0	200	200	

 ${}^{a}f = \{1/1 + [(1-w)/w]\rho_{Fe}/\rho_{NiTi}\}; \rho_{Fe}, \rho_{NiTi} \text{ are the densities of Fe and TiNi}$ (7874 and 6500 g/cm³, respectively).

³²⁹ overestimated. At lower f, smaller sized Fe particles tend to 330 be distributed along the boundaries of larger sized NiTi **331** particles.¹³ At larger f, on the other hand, Fe filler particles 332 become more uniformly distributed, forming a continuous **333** matrix, similar to the model configuration [Fig. 5(a)]. There-**334** fore, for lower f, the predicted values of M_s^c deviate slightly **335** from the experimental data while for larger f, we see very 336 good agreement, as evidenced in Table II and Fig. 6.

337 The present model is based on Eshelby's effective me-338 dium theory (EMT) with Mori-Tanaka's mean-field theory; 339 thus its validity is good for the entire range of filler weight **340** (volume) fraction, $0 \le f \le 1$. It should further be pointed out **341** here that the average size of NiTi is 212 μ m, which is con-342 siderably larger than that of the constituent Fe powder of 343 100 nm size. Compositional maps of the particulate compos-344 ites indicated that the Fe phase forms the matrix phase of the 345 composite unlike the model presented in Fig. 5. The impli-346 cations of this discrepancy need to be investigated further 347 and shall be looked into in future studies. However, despite 348 this assumption, as mentioned previously, the predictions 349 seem to match with the observed experimental values.

350 CONCLUSIONS

351 The combination of microsized TiNi powders and nano-352 sized Fe powders resulted in the formation of high density 353 specimens which exhibited superior stress-strain characteris-354 tics. Nanosized Fe powders tend to fill in the gaps between 355 microsized TiNi powders much better than microsized Fe 356 powders, thereby enhancing the bonding, resulting in stron-357 ger load transference at TiNi-Fe interfaces. Such an interface 358 behavior facilitates the phase transformation demonstrated



FIG. 6. Comparison of saturation magnetization (M_s) of TiNi–Fe particulate composites as a function of Fe predicted by Eshelby's model (filled circular symbols) and experimental data (filled square symbols).

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by the TiNi phase of the composite. This synergy between ³⁵⁹ the two phases of the composite is expected to benefit actua- 360 tor designers using this particular material system. Several 361 combinations of the microsized TiNi and nanosized Fe were 362 chosen and the respective stress-strain curves for each com- 363 bination were looked upon. Due to obvious space con- 364 straints, not all the stress-strain curves have been included in 365 this paper. Instead, one representative stress-strain curve 366 demonstrating the phase transformation phenomenon has 367 been included in the present work. The selection of an opti- 368 mal volume fraction of TiNi and temperature/pressure/ 369 duration of SPS process was found to be very critical in the 370 formation of a sample that would exhibit the SMA properties 371 under compression testing.²² Consequently, series of experi- 372 ments were conducted to identify these optimal volume frac- 373 tion and SPS process conditions using a design of experi- 374 ments approach and a few optimal conditions have been 375 identified. The microstructure of the composite was also 376 studied using SEM and transmission electron microscopy 377 (TEM) studies. 378

An extension of Eshelby's method for the determination 379 of effective magnetic properties of a FSMA system has been 380 proposed in the present paper and the predicted results were 381 compared with experimental results, leading to a validation 382 of the proposed model. 383

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