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Agent-Based Parallelization of a Multi-Dimensional Semantic Database Model

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Abstract

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In conventional database systems, people consistently ignore the semantic meaning in autonomous databases. It is not easy to extract significant information based on different querying contexts from a database system. Mathematical Model of Meaning (MMM) is a meta database system that extracts features from the database and explains the database by those features. It provides users with the capabilities to extract significant information under different semantic spaces. The semantic space is created dynamically with user-defined impression words to compute semantic equivalence and similarity between data items. MMM computes semantic correlations between the key data item and other data items to achieve dynamic data querying.

Multi-Agent Spatial Simulation library (MASS) is a parallel programming library that utilizes an agent-based model (ABM) to parallelize extensive data analysis. This project presents parallel
solutions to improve the performance of MMM using MASS. Multiple agent-based parallel solutions were implemented to improve the efficiency of MMM. Compared to the sequential MMM program, the parallel solution using MASS achieved 23 times speedup over the sequential program on matrix multiplication. MASS also reduced the processing time of distance sorting of multidimensional vectors by 23.70%. Additionally, this work also conducted benchmark analysis and programmability analysis between MASS and MPI Java to indicate the advantages of agent-based behavior.
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Chapter 1. INTRODUCTION

1.1 MOTIVATION

Nowadays, no matter what field you work in, data provide a unique way of looking the insights of a problem. In healthcare, datasets help epidemiological study to predict the trend of a pandemic. In the advertising field, recommendation systems analyze millions of data items to present the most relevant ads to you. Data has become a vital part of people's life that is closely related to all aspects. In the context of computer, data refers to machine-readable information. Therefore, some human-related sensitive recognition will be lost during the data transition, such as "semantic meaning", "impression", "human senses", "feelings", "sensitivity", "physiological reaction" and "psychological reaction" [1]. Mathematical Model of Meaning (MMM) provides a semantic associative computation method. It is a multidatabase system and was introduced by Dr. Kitagawa and Dr. Kiyoki [2]. In the traditional SQL-like multidatabase systems, the semantic meaning of data items is always being ignored. In MMM, it realizes semantic interoperability among data items. It takes context keywords to create semantic space and recognize data items disambiguously and dynamically according to the context [2]. Users can provide several context keywords to create a semantic space and use that semantic space to query data items. For instance, the word "buck" has a different meaning in the context of gambling and hunting. In the gambling context, "buck" is slang for a dollar. However, in the hunting context, it means some horned animals. Therefore, MMM is valuable for applications that require different query contexts.

In MMM, features are extracted from database, which can explain data items by those features. For example, in Longman dictionary, people can use 850 basic feature words to express all entries in the dictionary. In the query process, a correlation matrix is created to show
interconnections between features. In addition, a semantic space is also extracted by user-provided impression words. MMM can query the meaning of data items dynamically under different semantic spaces. Finally, the semantic projection mapped data items onto a semantic space, so that users can query under the semantic context. MMM is a computationally intensive framework that includes three massive mathematical operations: calculation of correlation matrix, eigen decomposition, and sorting data items by Euclidean distance. Hence, the parallelization is necessary to improve the query performance of MMM.

MASS is a parallelization framework that stores data in the distributed places and propagates agents to interact with places [3]. Places and agents are two important components in MASS. Place is a distributed array of elements that are dynamically allocated over a network cluster. Agents are a set of execution instances that can reside and migrate between places. Places are mapped onto the threads of computing nodes, whereas agents are mapped onto processes. Places and agents can both be running simultaneously to support parallel computing.

Compared with conventional parallel programming frameworks such as Spark and MapReduce, MASS uses agent-based modeling (ABM) to perform data parallelization. ABM views computation as an emergent collective group behavior among many agents. It simulates the biological identification of moving agents, and it is more efficient to move the computational resource to the distributed places instead of passing data around distributed places [4]. Mobile agents use this approach, but ABM finds data attributes in their collaboration [5]. In MASS, data computation is enclosed in the agent, all of which is scheduled as periodic data exchange using agent propagation.

1.2 PROJECT GOALS AND ACHIEVEMENTS

The research goals of this project are as follows:
1) **Reimplement MMM using Java and collect sequential performance benchmarks.**

   MMM was first introduced in 1993, the software and hardware performance have been improved a lot since then. We want to evaluate the performance of MMM to see which part takes the most time of the application so that we will get a better idea of the parallelization strategy.

2) **Enhance the overall performance of MMM by applying MASS.** We implemented four algorithms to parallelize MMM using agent-based approaches. We also conduct five benchmark analyses to evaluate performance improvement compared with the sequential program. In addition, we also compared MASS with MPI Java for some parts of the parallelization, which reveals MASS's strengths to some data streaming problems.

3) **Prove applicability of MASS in a real-world problem.** Before we started this project, MASS was used for analyzing large datasets and paralleling data-science applications. MASS shows excellent performance when compared with other frameworks such as MPI, MapReduce, and Spark [5]. However, MASS hasn't approved much on real-world problems. This project gives us an opportunity to explore how MASS will perform when solving those problems.

   In our work, we split MMM into three different steps and implemented the MMM using Java. By analyzing the execution performance of MMM, we identified the performance bottleneck within it. Therefore, agent-based parallelization approaches with MASS were applied to MMM, which gave us a satisfactory result compared with sequential performance. The execution time of matrix multiplication using MASS improved by 95% in comparison with the sequential program and the distance sort of multidimensional vectors also improved by 24%. The details of our achievements can be viewed in Chapter 5.
1.3 **Structure of White Paper**

The rest of this white paper is organized as follows: Chapter 2 introduces the background of MMM and MASS. Chapter 3 reviews related works of semantic database and parallel database. Chapter 4 discusses the related parallelization strategy of different steps in MMM. Chapter 5 presents the benchmarks analysis as well as the programmability analysis of MASS's implementations. At last, Chapter 6 concludes the project with future enhancements and limitations.

**Chapter 2. BACKGROUND**

2.1 **Mathematical Model of Meaning**

The relational database is unarguably the most popular database model today. It has been widely used in almost every field that needs to save structural data. As in relational databases such as SQL, database model designers have to convert data interconnections to computer language, which requires an additional direction. In addition, relational database also shows weakness in capturing the semantic meaning of data items. During a data querying process, the results from relational database are usually abstracted and returned to unnatural structural relationships. These relationships are always defined by the pre-defined foreign key declarations [6]. It always captures the logical relationship but ignores the natural semantic structures.

In a database, the semantics usually refer to three major categories: formal semantics, lexical semantics, and conceptual semantics [6]. The formal semantics means the feeling and sense of people. The lexical semantics represents the underlying meaning of a word and data item, and the conceptual semantics usually indicates the cognitive structure of data items. In order to realize the semantic meaning in the database, it not only focuses on the underlying meaning of data items but also the relationship of what they stand for. Data items always cannot be identified independently.
MMM is a semantic database model that helps users to discover data items with equivalent or similar meanings. In the normal SQL-like database, a data item is queried by pattern matching. The SELECT and WHERE clauses are used to filter data items through user-provided conditions. Comparing with a SQL-like database, the data item is queried by semantic associative search where data items are projected onto semantic spaces. MMM calculates the Euclidean distance between data items to find out the most relevant data items based on user-selected semantic spaces. The following sections present the technical details of three steps in MMM and discuss how does semantic associative work in MMM.

2.1.1  

Correlation Matrix Calculation

Overall, MMM can be separated into three different steps. The first step is to formalize the initial input data into matrix $A$, which is an $m$ rows by $n$ columns matrix. In this matrix, each feature is translated into a column, and each data item is represented as a row in a matrix. To create the initial input matrix, we refer to the basic words that explain all the dictionary's vocabulary entries as features. For example, the word "nice" can be expressed by features "kind", "nice" and "friend" and the word "small" can be expressed by features "amount", "average", "importance", "-large", "size" and "small" itself. Figure 2.1 shows a matrix to use $n$ features to explain all $m$ words. For example, in the word "nice", each feature word is set to 1 to illustrate the positive relationship between feature word and data word. In the case of "small", the negative value "-1" is set on the column of "large" to explain the negative value of this column. If features are not used to explain vocabulary terms, the columns corresponding to those features are set to "0" [1].
Afterward, we calculate the correlation matrix $M$ in order to prepare for the eigen decomposition in step 2. During the correlation matrix calculation, we first normalize the matrix in the row direction. The Frobenius norm is applied to each row and a $1 \times n$ normalized vector will be retrieved. The Frobenius norm is given by:

$$||F|| = \left( \sum_{i,j} \text{abs}(a_{ij})^2 \right)^{1/2}$$

Next, the original matrix is normalized by the normalized vector to get a normalized matrix. Finally, we multiply the normalized matrix with its transpose matrix to get the final correlation matrix. This matrix multiplication operates on two $m \times n$ and $n \times m$ matrices which will take a significant amount of time when matrix size gets larger. Therefore, the parallelization of this step is necessary, which will be discussed in the following section.

### 2.1.2 User-Defined Subspace Extraction with Eigen Decomposition

In MMM, the semantic associative search is deployed on a semantic space. The queries and retrieval candidates are mapped onto the semantic space, the retrieval candidates and query items will be calculated in correlation to the semantic space. There are three steps to perform the associative search:
1) User provides a context by a set of impression words \(\{u_1, u_2, u_3, \ldots, u_l\}\). The impression words must be a subset of data items in original matrix \(A\).

2) A subspace will be created by given context impression words.

3) All the data items will be mapped onto the subspace, and a normalization vector will be calculated as the correlation value between the context and the information resources.

In the above steps, a user-defined semantic space is created, and an orthogonal matrix \(Q\) will be formed as \(Q = (Q_1, Q_2, \ldots, Q_v)^T\) where \(Q_1, Q_2, \ldots Q_v\) are eigenvectors from the previous-generated correlation matrix. Eigenvectors are called semantic elements in MMM, and all eigenvalues are real. Eigenvectors are mutually orthogonal because the correlation matrix is symmetric. As shown in the following equation, we can get \(2^v\) potential semantic spaces to add up all the combinations together.

\[
I = \{q_1, q_2, \ldots, q_n \} \\
q_1 + q_2, \ldots, q_{v-1} + q_v \\
\ldots \\
q_1 + q_2 + \ldots + q_v \}
\]

In order to narrow it down into a smaller dimension of semantic space, Fourier expansion between user-provided impression words \(u_1, u_2, u_3, \ldots, u_l\) and eigenvectors \(q_1, q_2, q_3, \ldots q_v\) will be calculated. The vectors that are normalized in the infinity norm are called semantic center [2].

The semantic center can be calculated by:

\[
G = \frac{\sum_{i=1}^{l} u_1, \ldots, \sum_{i=1}^{l} u_{iv}}{||\sum_{i=1}^{l} u_1, \ldots, \sum_{i=1}^{l} u_{iv}||^{\infty}}
\]

Lastly, the semantic centers will be kept only if their values are greater than a positive real number \(\varepsilon\) \((0 < \varepsilon < 1)\). The index of semantic centers will be recorded, and the corresponding semantic element will be formed into the semantic space.
2.1.3 Sorting the Data Items by Calculating Euclidean Distance

In this step, we sort the data items by calculating Euclidean distance to finally get the query results. Upon finishing the previous steps, each data item has been projected onto the user-defined semantic space. By querying the data, there are two scenarios. The first one is to identify the nearest neighbors in the specified data item set $W$ from keyword $P$ in the semantic space (Figure 2.2 (b)). This corresponds to finding the closest data item between the given keyword in terms of meaning. The second one is to find the top $N$ items from the user-defined semantic space (Figure 2.2 (c)). In this scenario, users don't provide a keyword to query against. MMM queries the top $N$ items according to the current semantic space.

![Figure 2.2. Dynamic Semantic Spaces](image)

2.2 MASS

Multi-Agent Spatial Simulation (MASS) is a parallel computing library built with agent-based model to parallelize applications by propagating agents onto different places. For the alternative parallelization framework to MASS, such as Spark and MapReduce, they all use parallel data streaming to exploit a form of parallel processing. The dataset is streamed from the input source and processed by multi-threads in a computing cluster. Computer nodes perform a sequence of
operations on the data stream in parallel and return the results to the downstream. In this way, each individual request has to go through the whole process of data streaming.

On the other hand, with agent-based approach, MASS is able to save the data into a dedicated area so that further agents can retrieve data on demand. In addition, the database system requires the parallelization framework should be able to analyze data on the fly. Once the system receives a query request, the parallelization framework should minimize the data-reading process. MASS can also satisfy this requirement by spawning new agents to take charge of new requests. In MASS, there are two major components, Places and Agents. In the following sections, we will discuss the programming model of MASS as well as the main functionalities of places and agents.

2.2.1 Place

Places is a multidimensional array of elements that are uniformly distributed over computing machines in a cluster. Each partition of places utilizes the multi-core of computing nodes, and further subdivided portion is allocated on a different computing core. The place is managed by a set of network-independent array indices, and it is capable of saving data and exchanging data with its neighbors. As visualized in Figure 2.3, remote nodes start the MASS application by forking processes over a cluster. Each computing node is connected over SSH channels through TCP connections [7]. In general, MASS splits places into smaller stripes vertically, and each strip is executed by a different thread. The most important function in places class is callAll(), that invokes a user-defined function in all array elements. The function is processed among multi-processes and threads. The user needs to pass a functionId as the identifier to the function.
2.2.2 Agent

In MASS, *Agents* are a set of execution instances which can reside and migrate between places. Agents use array indices to indicate the next place's location. During agents migration, agents can carry data members from the source location to the destination location and terminate or replicate themselves upon arrival. Comparing with places, agents are grouped into bundles, and each bundle is assigned to a different process. Multiple threads periodically check agents in and out that are ready to execute the new agent [3]. Agents class have three important function interface, `callAll()`, `migrate()`, and `manageAll()`. The `callAll()` function invokes a user-created function on every active
agent, and the user-created function is pointed by functionId. migrate() function initiates an agent migration to a new place by calling places index. manageAll() function updates the status of an agent. Under the hood of manageAll() function, it checks the size of each agent bag and synchronizes all threads together. The most recent version of MASS also supports event-driven agent behaviors to allow users to associate functions upon agents' departure, arrival, and creation. Each of them is annotated as @OnDeparture, @OnArrival, and @OnCreation [8].

Chapter 3. RELATED WORKS

This chapter describes the existing semantic database and parallelized database. It discusses the advantage of our approach and the limitations of past research.

3.1 PARALLEL DATABASE

Parallel database has been widely adopted by data-intensive applications. It provides optimized performance and high scalability compared with traditional database. In the traditional database, the size of disk space and memory space always limits the number of data items that can be fit in a database. As data size grows bigger, parallel database can store the data item in a distributed fashion and improve its processing speed with multiple computing nodes and CPUs. In the parallel database system, where operations are performed simultaneously, a single task can be distributed onto multiple nodes and combine results by finishing the task.

There are three types of architecture for parallel machines. They are shared-disk, shared-memory, and shared-nothing architectures [9]. Shared-memory architecture typically means that all computer nodes share a global memory space. In [10], authors proposed multiple algorithms that use remote direct memory (RDMA) in parallel database system. The work dynamically manages RMDA-registered memory to improve the database performance. A shared-disk parallel
database system was proposed in [11]. The shared-disk system has a low communication overhead compared to other architectures. Especially for the reading actions, the operations can spread over multiple nodes to shorten the response time. It provides flexibility for the reading operations.

Our proposed MMM and MASS integrated solution is a shared-nothing architecture. The advantage of shared-nothing architecture is high extensibility and high availability. Compare with other shared-nothing architecture, such as MySQL Cluster, MASS is easier to scale up the system without considering data partitioning. The data can be fed into places of new machines instead of syncing up with previously existing nodes. In addition, our solution also eliminates single points of failure. With agent-based approach, a single failure will only cause some agents to be terminated but other agents can continue work on their tasks. Moreover, MASS is capable to operate multiple concurrent requests and analyze data on the fly. Once places are initialized, agents can make use of the initialized data to do operations and analysis and concurrent requests can be handled by new spawned agents. Our solution is more flexible and reliable compared to other discussed work.

3.2 Semantic Database

In 1978, Semantic Data Model (SDM) was firstly introduced by Michael Hammer, which provides a high-level semantic-based modeling mechanism to capture and express the structural formalism for databases [12]. SDM facilitates data querying from different perspectives, where users can query data by declaring their views of a large database. Although SDM leads to some redundancy of data storage by providing multiple perspectives of a database, users can still benefit from its enriched relationship schema to better understand the data in a natural way. In World Wide Web, W3C introduced the standard of Web Ontology Language (OWL) and the Resource Description Format (RDF) to realize a semantic web. The purpose of introducing a semantic web is to make machines can understand and interpret complex human requests based on their meaning [13]. The
focus of OWL and RDF is known as triples, which is the form of subject-predicate-object. The subject and object denote the resources, and the predicate tells the relationship between subject and resources, as well as describes the traits or aspects of the resources. OWL and RDF utilize a metadata model to express semantic meaning in web resources and various syntax notations to make the semantic meaning understandable by machines. With the growing amount of web information being processed and extracted, the most valuable and related information can be filtered by domains. Also, the web crawler can be beneficial from the semantic web information.

In [14], a semantic-based model to represent big multimedia data is proposed. The work describes a property-based graph that allows users to express the concept and relationship between multimedia data items. A graph database is utilized to save key-value pairs of data items and traverse their connections. Their work presents a machine-understandable representation that organizes the semantic associations between multimedia data items.

Most semantic database models highly rely on either modeling information in a relational database or modeling the resources and their relationship of data items [6][14]. In addition, some semantic databases are limited to specific domains, and they usually don't provide a general semantic database solution. In the vision of MMM, it doesn't rely on any relational database. A group of features represents the value of data items. In addition, MMM can realize the dynamic recognition of the context by a semantic projection that cannot be achieved by other discussed literature.

3.3 Summary

To summarize, our integrated system with MMM and MASS has the following advantages.

1) MMM, as a semantic database model, is a complete mathematical model. MMM doesn't require assistance from any other relational database or graphs to save the semantic
structure. MMM can use semantic projection and semantic associative search to realize data search by semantic meaning under a different context.

2) By using the agent-based model in our system, the system can achieve the best scalability and availability. Since MASS is based on shared-nothing architecture, we can add more computing resources on demand. Therefore, the architecture will not set any obstacles when scaling up the system.

Chapter 4. PARALLELIZATION

This chapter, it presents multiple agent-based parallelization algorithms, each applied to a different MMM step. Additionally, it also discusses the sequential results of MMM, which are programmed in Java.

4.1 SEQUENTIAL RESULTS OF MMM

We first implemented MMM using Java to retrieve the sequential benchmarks. The sequential benchmarks are organized in 3 steps, as we previously mentioned.

Figure 4.1 shows the execution time measured with `System.currentTimeMillis()` when handling different sizes of datasets. The datasets are generated with random double values. Overall, step 1 costs the most time in MMM. The matrix normalization and multiplication take over 90% of the overall time. When the matrix size reaches 40000 rows and 2000 columns, it takes more time than other datasets, which takes over 40 minutes to complete the calculation. As for step 2, it accounts for 7% of the total time on average. It has the highest percentage of overall time when the matrix size is at 10000 rows and 2000 columns, which is 17%. As of step 3, the performance of sorting all data items is based on the distance between themselves and the key data item. The benchmarks indicate step 3 has the smallest percentage of overall time, and the slowest one takes
1607 milliseconds. The benchmark of step 3 is conducted by using memory to retrieve. However, in the real world, data should be saved in the hard drive instead. Given this assumption, the execution time of data sorting will be much slower than what we measured.

As the number of rows increased from 10,000 to 20,000, the total time of performance increased by 1.6 times. While the number of columns increased from 1000 to 2000, the total performance time increased almost five times. When calculating the eigen decomposition, the size of the symmetric matrix is determined by the original column size. And the time complexity of eigen decomposition is O(n^3) [15]. Hence, column size has a more severe effect than row size on the overall performance. Based on the previous analysis, it is worthwhile parallelizing MMM. In the following session, we discuss the parallelization strategy for each step of MMM.

![Figure 4.1. MASS Sequential Benchmarks](image)

**Figure 4.1. MASS Sequential Benchmarks**

### 4.2 Step I: Matrix Multiplication

#### 4.2.1 Cannon's Algorithm

Matrix multiplication is one of the most popular benchmarks for the parallel framework. In parallel computing, people use Cannon's Algorithm to improve performance [16]. In general, Cannon’s
algorithm includes two steps (Figure 4.2). The first step is to align the matrix of A and B so that in each processor $P_{i,j}$, the $j$ value of A is the same as the $i$ value of B. The second step is to move each submatrix A one step left and submatrix B one step up and perform block multiplication. Finally, the multiplication result is generated by adding up the products of each shifting.

![Alignment of matrices](image)

Figure 4.2. Programming Model of Cannon's Algorithm [17]

In order to implement Cannon’s algorithm using MASS, we created a `SubMatrix` class and a `Shifter` class to extend Place and Agent respectively. The `SubMatrix` class provides memory and computing resources. Each place is initialized in the CPU cores of computing nodes. Upon
initialization, the place will read the data from the CSV file and save their corresponding portion into the memory space.

In the Shifter class it spawns two agents at each place, one is responsible for the multiplier matrix $A$, and the other is responsible for the multiplier matrix $B$. As shown in Listing 1, In order to make the initial alignment, each agent grabs the data from the place where it is spawned and migrates to the designated places (line 3 and line 16). In line 7 to 11 and line 21 to 25, agent A and agent B are finding the coordinate of the next destination place. Agent A shifts $i$ columns left, and agent B shifts $j$ rows up. After initial alignment, each agent does the matrix calculation and saves the temporary result into the place's memory. When finishing the initial alignment, agents will collect data and sum it up to get the final calculation results.

```java
1. if (getAgentId() % 2 == 0) { // A agent
2.     this.tag = 'A';
3.     this.subMatrix = deepCopyMatrix(place.matrixA);
4.     int row = place.getIndex()[0];
5.     int col = place.getIndex()[1];
6.     int newCol = 0;
7.     if (row != 0){
8.         newCol = (placeSize + getIndex()[1] - row) % placeSize;
9.     } else {
10.        newCol = col;
11.    }
12.    this.nextSubMatrix = new int[]{row, newCol};
13.    place.matrixA = null;
14. } else { // B agent
15.     this.tag = 'B';
16.     this.subMatrix = deepCopyMatrix(place.matrixB);
17.     // alignment B matrix: for col j, shift j row up
18.     int row = place.getIndex()[0];
19.     int col = place.getIndex()[1];
20.     int newRow = 0;
21.     if (col != 0){
22.         newRow = (placeSize + getIndex()[0] - col) % placeSize;
23.     } else {
24.         newRow = row;
```
25.    }
26.    this.nextSubMatrix = new int[]{newRow, col};
27.    place.matrixB = null;
28.    }

Listing 1. Agent Migration of Shifter Class in Cannon's Algorithm

Compared with other parallel approaches, agents move over matrices instead of the conventional approach to shifting data to neighboring elements. MASS provides a more flexible way for data exchange; developers do not need to worry about the potential deadlock, which is likely to happen with MPI. In MPI, *MPI_SEND* and *MPI_RECV* will block the program until the send or receive buffer can be reused [18]. If both ranks send data through the same buffer, the program will deadlock.

4.2.2 Parallel I/O

By implementing Cannon's Algorithm, the value of data items has to be read into memory first. In our former implementation, the data is read by the master node and distributed over the slave ranks. There are several drawbacks by doing this way. First, the size of the input matrix file is limited by the memory space of the master node, this will also bound the scalability. Next, the file reading speed is not optimized. Since only one node reads and distributes the data, it doesn't make use of the power of multiple machines. The speed of data I/O has a significant impact on the overall programming performance. The data I/O brings a large overhead in our parallelization program, which significantly curtails the effectiveness of MASS. Based on these considerations, we implement parallel I/O for csv files.

In order to enhance the parallel I/O within the MASS library, each place must be able to open and read the same CSV file in parallel. Hence, all the implementations have been done within the Place class. We implemented the CSV file reading feature on top of the current MASS parallel I/O
implementations. In the new design of parallel I/O, it firstly opens the file by taking the given file path argument, which determines the file's name and whether the file's type is supported. Currently, MASS parallel I/O supports NetCDF, TXT, and CSV files. If the given file type is not supported, then -1 is returned. Otherwise, this file will be opened and saved into the fileTable. The open method is a synchronized method so that only one place will perform the open task on individual computing node. The file reading is implemented by splitting the file into an equal number of bytes, and each computing node gets a corresponding portion. However, since each data record's character length is different for the CSV file, directly splitting the file will make records lose some digits. To solve this problem, we add paddings on each line to make sure they all have the same length. In this case, when we split the file by an equal number of bytes, every computing node gets the same number of rows. The following method is added in the CsvFile.java class, which is used explicitly for handling CSV parallel I/O.

- **public double[][] readToArray(int placeOrder):** this method takes place’s order as argument and returns a 2d double array back. The whole CSV string is retrieved from the memory buffer as well as the row size and column size. Afterward, we loop through every line and assign corresponding columns to each place. As shown in Listing 2, each computing node breaks the data vertically, and data in array[row][col] will be read later into each place. This design aligns with Cannon's algorithms' requirement which requires slave nodes to save the data as a submatrix and start doing the calculation right away.

```java
1. String csvString = new String(entireCsvFileBuffer);
2. String[] rows = csvString.split("\n");
3. String[] cols = rows[0].split(",");
4. int nRow = rows.length;
5. int nCol = cols.length / myTotalPlaces;
6. double arr[][] = new double[nRow][nCol];
```
for (int row = 0; row < nRow; row++) {
    cols = rows[row].split(",");
    int colOffset = placeOrder * nCol;
    for (int col = 0; col < nCol; col++) {
        arr[row][col] = Double.parseDouble(cols[colOffset++].replace("\uFEFF", ",");
    }
}

Listing 2. Read Data to Array of MASS places

4.3 STEP II: EIGEN DECOMPOSITION

4.3.1 Householder Transformation

In step 2, the most time-consuming operation is eigen decomposition. The eigenvalue problem is one of the fundamental problems in linear algebra. Eigenvectors make understanding linear transformation easy. It represents the directions along when linear transformation performs. The fundamental linear transformations are stretching, compressing and flipping [19]. The eigenvalues represent the factors when this linear transformation happens. In MMM, the eigenvectors define user-defined semantic space characteristics, which provide essential information for semantic projection and distance calculation.

Upon the completion of step 1, we get a real symmetric matrix $A$. A scalar $\lambda$ is called an eigenvalue and a nonzero column vector $z$ is the corresponding eigenvector if $Az = \lambda z$. $\lambda$ is always a real number when matrix $A$ is real symmetric [20]. In order to find eigenvalue and eigenvectors, the eigen decomposition will be calculated to get the eigenvectors. In general, this decomposition often goes under the name matrix diagonalization [21]. The matrix diagonalization of a matrix transfers this process into a product of three other matrices and only one of which is diagonal [19] [20].
The real symmetric matrix $A$ is reduced to real tridiagonal form $T$ (Figure 4.3), which can be expressed as $A = QTQ^T$. In this process, we utilize householder factorization, which applied orthogonal projector in an iteration process. For $n \times n$ matrix, we need to do $n - 2$ iterations to get a tridiagonal system. For $k = 1, 2, 3, \ldots n - 2$ as follows:

$$A^k = H^k A^{k-1} H^k$$

where $H$ is householder matrix and $A^{k-1}$ is the result from the last iteration. Upon getting the symmetric tridiagonal matrix $T$, we need to factorize $T$ as $T = SAS^T$. The diagonal entries of $A$ are the eigenvalues of $T$, which are also the eigenvalues of input matrix $A$ [22].

4.3.2 Parallelization of Eigen Decomposition

Typically, the eigen decomposition is solved in two successive steps: tridiagonal transformation and extract solution from the tridiagonal matrix. In the first step, there are multiple iterations applied to get the tridiagonal form. Since each iteration relies on the results from the previous iteration, we cannot simply distribute those into subprocesses. In [23], Dongarra et al. introduced a divide and conquer approach to implement the parallelization. In their implementation, the given matrix is split into smaller subproblems.

$$T = \begin{pmatrix} T_1 & \vdots \\ \vdots & T_2 \end{pmatrix} + pww^T$$

(4.1)
As shown in 4.1, the original input matrix is divided into two half-sized submatrices. For \(1 \leq k \leq n\), the \(T_1\) and \(T_2\) are the \(k\)th diagonal elements. When subproblems are small enough, the QR refactor is called so that

\[
T_1 = Q_1 \Lambda_1 Q_1^T \tag{4.2}
\]
\[
T_2 = Q_2 \Lambda_2 Q_2^T \tag{4.3}
\]

Finally, the backward computation will be called to form the tridiagonal matrix and compute the eigenvectors of matrix \(T\). Because of the time restriction of this project, we don't have chance to implement this parallelization algorithm with MASS. We wish we can tackle this problem in future.

4.4 STEP III: EUCLIDEAN DISTANCE SORT OF MULTI-DIMENSIONAL VECTORS

4.4.1 Parallelization Algorithm

In step 3 of MMM, it requires sorting data items by the distance from the key data item to others. In our original proposal, we wanted to use agent propagation for the parallelization implementation. An agent spawns at the location of a test data item. They will propagate to the surrounding places until one agent collides with others. As shown in Figure 4.4, this approach works well in one-dimension to three-dimensional spaces. However, it would be tough to find out the number of surrounding data items for agents to migrate to when it comes to higher-dimensional space than three-dimension. Therefore, we cannot make use of this methodology in our implementation. Instead, a modified agent propagation algorithm is introduced for the distance calculation of multi-dimensional vectors.
In this modified algorithm, we firstly evenly distribute the input data into multiple layers. For instance, as illustrated in Figure 4.5, if the value of data items falls into the range from 0 to 1, and we have three layers in total, each layer will be in the interval of 0 to 0.33, 0.34 to 0.66, and 0.67 to 1. Then we initialize $3 \times n$ places in MASS where $n$ is the dimension of the vector. During agents’ initialization, agents migrate to the starting place where the key data item has valid data in the corresponding column and agent level. Agents will traverse along the vertical direction to discover if surrounding places contain the value of other data items. Upon arriving at a new place that maintains a value between 0 and 1, the agent calculates the distance between the key data item and corresponding data item and then saves the results in memory. To avoid duplicate distance calculation, we assign each agent with a group of consecutive data items. The index of data item can be determined from $\text{sizeOfDataItem} / \text{agentSize} \times \text{agentIndex}$ to $\text{sizeOfDataItem} / \text{agentSize} \times (\text{agentIndex} + 1)$. This can also give us a number of data items that an agent is responsible for ($x$). The migration will stop when the following conditions reached:
1) agents have visited all levels so that all distances between key data items and other data items have been recorded.

2) when there are only \( m \) active agents left, the program will stop agents' migration

The reason for having the second condition is that users tend only to get top \( N \)-related data items in step 3. Threshold \( m \) can be retrieved by \( n - \frac{(sizeOfDataItems - N)}{x} \). By using the threshold of active agents left, we can save up the time and resources to skip those low-relevant data items.

<table>
<thead>
<tr>
<th>Column1</th>
<th>f1</th>
<th>f2</th>
<th>f3</th>
<th>f4</th>
<th>f5</th>
<th>f6</th>
<th>f7</th>
<th>f8</th>
<th>f9</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.34 - 0.66</td>
<td>A</td>
<td>A</td>
<td>A</td>
<td>A</td>
<td>B</td>
<td>B</td>
<td>B</td>
<td>A</td>
<td>A</td>
</tr>
<tr>
<td>0.67 - 0.99</td>
<td>B</td>
<td>A</td>
<td>A</td>
<td>A</td>
<td>A</td>
<td>A</td>
<td>B</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Figure 4.5. Agent Propagation in Multi-Dimensional Space.

Listing 3, it illustrates the shifting process of agents. Each agent that finds data in the current place iterates all target vector indexes (line 1 - 9). Once an unvisited vector is found, agents will calculate the Euclidean distance between two vectors and save it to a HashMap. Finally, the index of destination place will be determined by calculating the current index modulo size of layers, and agents will migrate to the next place.

```
1. for(int i = this.targetVectorIndexMin; i < this.targetVectorIndexMax; i++) {
2.     if(valueMap.containsKey(i)) {
3.         double [] value = place.getArrayFromRandomAccessFile(dataSetFile, i, this.dataSize);
4.         double distance = calculateDistance(place.keyData, value);
5.         this.results.put(i, distance);
6.     }
7. }
8. int newY = currY;
9. int newX = (currX + 1) % this.levels;
10. migrate(newY, newX);
```
4.4.2 File I/O with RandomAccessFile

In this implementation, the size of memory space limits the data that can be retrieved, 8GB memory space can only fit 500,000 rows with 2000 features. In addition, in the real database system, data is usually saved in the hard disk instead of memory space. Therefore, we decide to bring RandomAccessFile for agents to retrieve values of data items.

A random access file behaves like a large array of bytes [24]. A file pointer, which is similar to a cursor, can be moved to any position on the byte array. It reads bytes starting at the file pointer and advances a certain number of bytes to read the content. Similar to previously mentioned parallel I/O, this feature is also added to the place class.

By implementing these functions, MASS is able to access the data directly from the hard drive instead of saving all of them into RAM. There are several tradeoffs of using this methodology. First of all, MASS gets rid of the restrictions of memory space. Place doesn't need to keep a copy of the whole database. Instead, agents can access their required records on demand. This behavior simulates data querying in the real database. Technically, we can handle any size of database using this methodology. Moreover, in MMM, users don't query all related data items under a semantic space. Instead, only top N items will be returned. In this case, the number of file I/O can be limited. While the frequency of file I/O is narrowed down, the speed of reading a file from a hard drive is still much slower than directly taking it from memory space. If the number of file I/O gets bigger, it will inevitably reduce efficiency.
Chapter 5. RESULTS

This chapter shows experimental results of MASS and MPI implementations discussed in Chapter 3. It also compares the experimental results with sequential. The detailed benchmarks data can be found in Appendix.

5.1 EXECUTION ENVIRONMENT

The experiments are conducted in cssmpi cluster at the University of Washington Bothell. There are eight computing nodes in cssmpi cluster which provides us with 4-core Intel(R) Xeon(R) Gold 6130 CPU with 20GB memory space. The MASS library 1.3.0 and MPI Java [25] are used in our experiment. The MASS java is configured with 4GB initial heap size and 12GB maximum heap space. The testing dataset is random generated with double precision.

5.2 MATRIX MULTIPLICATION

5.2.1 Computation Results

The experiments were conducted to evaluate and compare large-scale matrix multiplication performance using MASS, MPI Java and sequential Java programs. Previous students have conducted benchmark comparisons between MASS with Spark and MapReduce. The results showed that Spark and MapReduce were much slower than MASS [26]. Therefore, we only compare MASS with MPI Java in our benchmark.

For MASS and MPI Java, they use Cannon's algorithm, and the sequential Java program uses the basic matrix multiplication algorithm. The testing data is a square matrix that has 2048 rows and 2048 columns. We used four computing nodes to conduct benchmarks with both MPI and MASS. The number of computing nodes must be divisible by the matrix size in Cannon’s
algorithm. Therefore, this project would only be able to test with four nodes in a cluster. To gain the best performance of data I/O, we used the /tmp folder of each computing node in cssmpi cluster. The /tmp folder is directly connected to each computer in the cluster that no longer requires data to be transferred over a distributed network. In this way, we are able to reduce the network overhead.

Figure 5.1 visualizes the execution time, we include MASS initialization time, MASS place initialization time, file reading time as well as the actual calculation time. The MASS initialization time consists of the time of processing $\text{MASS.init()}$. During this process, MASS establishes the ssh connection between the master node and slave nodes and passes messages between nodes to verify the connections. The MASS place initialization time includes the bootstrap of places over computing nodes and assigns places onto different computing nodes.

![Matrix Calculation Benchmarks](image-url)
MPI Java takes 15319.6 milliseconds in total, which exceeded MASS and sequential program's performance. MASS also has good performance results, which achieves 20370.83 milliseconds using parallel I/O and 20587.67 milliseconds without using parallel I/O. When we look at the calculation time only, MASS has the best performance. It takes around 5000 milliseconds while MPI Java takes 12937.2 milliseconds and the sequential program takes over 115693.8 milliseconds. By comparing the calculation performance between MASS and MPI, we can see that MASS improves over 95% from the sequential program while MPI Java improves around 88% from the sequential program. This is because MASS uses multi-core capability, whereas MPI only uses a single core on each machine. In this case, the number of computing nodes of MASS increases from 4 to 16, and each computing node is responsible for a smaller submatrix size so that the overall performance is faster than MPI. In MASS, the MASS initialization time takes the most time. This time is static, and it will not change with the change of the number of computing nodes. In this case, we expect the percentage of MASS initialization will be relatively small when we use more computing nodes, and MASS will have a chance to surpass MPI in terms of overall performance.

In MPI Java programs, the file reading time is around 2300 milliseconds, accounting for 15% of the overall processing time. MASS improves the file reading time significantly by implementing the parallel I/O. It dropped the file reading time from 1507 milliseconds to 993 milliseconds which is a 34% improvement.

5.2.2 MASS Programmability Analysis

This section discusses programmability analysis between MASS with MapReduce, Spark, and MPI Java.
MapReduce and Spart introduce a new programming paradigm. With MapReduce, operations are separated into two types of procedures, \textit{Map} and \textit{Reduce}. The map procedure filters and sorts the input data, and the reduce method behaves like a summary operation \cite{27}. The whole process is very similar to the divide and conquer algorithm. This programming model with multi-threaded implementations provides better scalability and fault tolerance. In order to fit the model of MapReduce, developers need to be familiar with new data structures (Map and Queue), which will bring extra learnings to developers.

Spark is a cluster computing platform, and it extends MapReduce to support nonlinear dataflow structure on distributed programs \cite{28}. The core of Spark is Resilient Distributed Dataset (RDD), which is a read-only collection of items distributed across computing nodes in a cluster. The input data is transformed into RDDs in a Spark application, and each computing node receives a corresponding portion of RDD partitions. In Spark application, there are two types of operations. \textit{Transformation} converts the data input into a new RDD, and \textit{Action} performs operations on input RDD to return results. Same as the abovementioned MapReduce, this new programming paradigm brings a steep learning curve to developers. Moreover, during the data stream, the data transformation in MapReduce and Spark leads to extra unnecessary efforts to satisfy the framework's requirements. This drawback in iterative MapReduce or RDD transformations results in additional overhead due to the need to exchange data over clusters.

On the contrary, MASS uses an agent-based approach, and it simulates the problem-solving process using agents. Although Spark has a built-in matrix multiplication library, RDD requires transforming all input data instead of submatrix only. Since communication among data items is only allowed from data shuffling and sorting in Spark and MapReduce, their implementation of matrix multiplication is extremely difficult. On the other hand, a matrix is laid out smoothly over
a cluster system with places, and agents work as messengers in Cannon’s algorithm. That’s why MASS can parallelize Cannon’s algorithm much easier than Spark and MapReduce.

When we look at Cannon’s algorithm with MASS and MPI Java, the most challenging part in Cannon’s algorithm is data transmission between different ranks. In MPI, this can be achieved using `MPI_SEND` and `MPI_RECV`. Since MPI doesn’t support multiple dimension array data transmission, we have to allocate arrays into a contiguous format. Moreover, MPI ranks are organized in linear order. Developers have to map their rank numbers into a 2d array to get the relationship between rank number and submatrices' id. MPI provides users with `MPI_Cart_create` method to create a communicator in a 2d topology format. We utilize this method to achieve rank mapping. In contrast, MASS offers a more convenient way to work with Cannon's algorithm than MPI Java. Places are a multidimensional array so that they can easily be mapped with submatrices. MASS utilizes agents to carry data among computing nodes, and this gives developers a more intuitive way to think about data transactions.

Lastly, the deadlock is the most common mistake in MPI. Developers have to be aware that for every `MPI_SEND` there must be a pairing `MPI_RECV`. For example, as shown in Figure 5.2, this may end in deadlock as rank 0 and rank 1 are sending simultaneously, but none of them are receiving data. In comparison with MPI, MASS allows flexible communication between submatrices that won't cause deadlock during data transmission. Thus, matrix multiplication requiring frequent data transmission between submatrices benefit from MASS's flexibility and reliability.
5.3 **MULTI-DIMENSIONAL VECTOR DISTANCE SORTING**

In this section, we present the experimental results of multi-dimensional vector distance sorting using MASS. We test on different data set and the value of data is in double precision. We also compare the benchmarks between MASS and the sequential Java program. There are multiple processes in the MASS program. The first one is to initialize MASS and places, which includes starting MASS processes and saving the index of valid data into places. Secondly, in the MASS program, we didn’t take account of the place's initialization time. This is because we consider the database as a read-intensive database, so that the place initialization won't be processed in a frequent manner. We only focus on the agent shifting time to sort the distance of multi-dimensional vectors. In the sequential program, we conduct experiments using random access files. The value of data items is retrieved by random access file pointer and the distances between general data items and the key data item are sorted to get the final ranks.

![Figure 5.2. Deadlocks in MPI](image-url)
5.3.1 **Computational Results**

As shown in Figure 5.3, the performance of MASS using memory space is slower than the sequential program. The testing data size is 50,000 rows and 2000 columns. MASS retrieves the top 5452 data items and the sequential program retrieves all 50,000 data items. The MASS program executes three iterations, and the iteration ends when 1500 or fewer agents are alive.

![Figure 5.3. Data Sorting with Memory Space](image)

When we compare the benchmarks using *RandomAccessFile* to retrieve data values, MASS has some advantages compared to the sequential Java program when the data size gets larger. When the data size is at 50,000 rows * 2000 columns, it takes MASS 7285 milliseconds to sort 3831 top data items and takes sequential program 9549 milliseconds to sort 50000 data items. However, when data size decreases to 20,000 rows * 2000 columns, the advantage of MASS no longer exists. MASS becomes slower than the sequential program, which is 38.8% slower than the sequential program (Figure 5.4).
In the MASS implementation, the number of layers (i.e., the number of partitioned ranges between 0.0 and 1.0) also affects the overall performance. In general, the bigger the number of layers, the faster performance would be. When the number of layers increases, the data distribution to the place becomes more granular. Each place gets a smaller number of data items than bigger layers. In this case, when agents traverse into a new place, it takes less time to calculate distance and sort data items.

<table>
<thead>
<tr>
<th>Levels</th>
<th>Data Size</th>
<th>Time (ms)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>50000 * 2000</td>
<td>15690</td>
</tr>
<tr>
<td>20</td>
<td>50000 * 2000</td>
<td>7285</td>
</tr>
<tr>
<td>10</td>
<td>20000 * 2000</td>
<td>7750</td>
</tr>
<tr>
<td>20</td>
<td>20000 * 2000</td>
<td>5208</td>
</tr>
</tbody>
</table>
Considering the scenarios in real-world database systems, MASS can be utilized to query large-scale databases. Once MASS applications and places are initialized, the performance of data querying is superior to the sequential Java program. In addition, MASS is also able to handle multiple querying requests in parallel. Upon a new request arrives, a new group of agents could be spawned onto places and migrate to the neighbors to fulfill the user's request. However, the sequential program has to re-calculate the distance whenever the key data item got changed. Additionally, when data size gets larger, MASS can easily pick up the most related data items using the agent migration approach, while a sequential program needs to sort all data items that put it in a disadvantaged position. Therefore, MASS is well suited for multi-dimensional vector distance sorting in the data querying context.

Chapter 6. CONCLUSION

6.1 ACHIEVEMENT

As a database, MMM handles data queries on the fly in accordance with the user-provided impression words. It applied semantic correlations computations between different data items with context computation mechanisms. After examining the performance conducted by the sequential program, we found MMM is a high computational framework that requires large-scale mathematical operations. When the data size is 40,000 rows * 2000 columns, the total execution time of MMM is over 40 minutes. MMM creates a space to save data items, and places of MASS can support this space. Therefore, we applied MASS to parallelize MMM using the agent-based methodology.

For step 1 of MMM, we utilized Cannon’s Algorithm with MASS. MASS showed a significant performance improvement over the sequential program and MPI Java program. On
average, MASS with parallel I/O achieved 23 times speedup over the sequential program on 2048 * 2048 matrix multiplication. By comparison with other parallel frameworks, it also improved the efficiency by 2.47 times over MPI Java. With the new parallel I/O feature added into MASS, MASS utilized the advantage of distributed systems to reduce the overhead in data I/O. The file reading time reduced by 57% compared to the sequential execution. This feature also enhanced the scalability of MASS to deal with millions of data with a moderate performance impact. Concluding that, MMM delivered the best computation performance with reactive agents and facilitated user-defined submatrices mapping in distributed arrays.

The work of sorting distance of multidimensional vectors indicates that MASS is capable of solving real-world problems. In comparison with the sequential problem, MASS provides a solution for high concurrency scenarios. MASS is suitable to handle multiple requests concurrently with multi-threading programming. Additionally, MASS also offers a competitive benchmark to acquire the top related data items in MMM.

6.2 Future Work

As for future work, the following tasks can be implemented. In step 2 of MMM, the parallelization of eigen decomposition is not finished. In the future, eigen decomposition can be parallelized along with divide and conquer techniques to improve the performance significantly. In MMM, we want to clarify some technical details of step 3. The projections between vectors to the semantic space are still ambiguous. We want to identify the accurate math formulas to identify the projections between vectors to the semantic space. Besides, in our implementations, we tried handling multiple querying requests at the same time. However, we are not clear what the maximum limitations of MASS are. Hence, we want to test the max number of concurrent requests that the system can handle. Furthermore, MASS and MMM require a real-world database to verify correctness and
efficiency. This would give us more confidence in our integrated system to apply to more practical applications in the future.
BIBLIOGRAPHY


[26] C. Liu, "Development of Application Programs Oriented to Agent-Based Data Analysis," p. 60.


APPENDIX A

Appendix 1. MMM sequential results, execution time are measured in milliseconds

Table 1. MASS Sequential Benchmark

<table>
<thead>
<tr>
<th>Data Items</th>
<th>Features</th>
<th>Context Size</th>
<th>Step 1</th>
<th>Step 2</th>
<th>Step 3</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>10000</td>
<td>1000</td>
<td>4</td>
<td>88180</td>
<td>5604</td>
<td>173</td>
<td>93957</td>
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<td>77729</td>
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</tr>
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<td>6773</td>
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<td>148474</td>
</tr>
<tr>
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</tr>
<tr>
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<td>1000</td>
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</tr>
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<td>86487</td>
<td>1607</td>
<td>2400879</td>
</tr>
</tbody>
</table>

Appendix 2. Benchmark performance of MMM step 1, execution time are measured in milliseconds

Table 2. Execution Benchmark of MMM Step 1

<table>
<thead>
<tr>
<th>No.</th>
<th>MASS Initialization Time</th>
<th>MASS Place Initialization Time</th>
<th>File Reading Time</th>
<th>Calculation Time</th>
<th>Total Time</th>
<th>Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>15607</td>
<td>89</td>
<td>973</td>
<td>4612</td>
<td>21281</td>
<td>MASS(Tmp Folder w/ parallel IO)</td>
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<tr>
<td>2</td>
<td>13277</td>
<td>96</td>
<td>939</td>
<td>4626</td>
<td>18938</td>
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<tr>
<td>3</td>
<td>13122</td>
<td>117</td>
<td>1207</td>
<td>5261</td>
<td>19707</td>
<td>MASS(Tmp Folder w/ parallel IO)</td>
</tr>
<tr>
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<td>14661</td>
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<tr>
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<td>20936</td>
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<tr>
<td></td>
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<td></td>
</tr>
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<tr>
<td>6</td>
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<td>1019</td>
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<td></td>
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<td></td>
<td>MPI 4 nodes</td>
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<td>Sequential</td>
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</tr>
<tr>
<td>21</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Sequential</td>
<td></td>
</tr>
<tr>
<td>22</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td>Sequential</td>
<td></td>
</tr>
</tbody>
</table>
Appendix 3. Benchmark performance of MMM step 3, execution time are measured in milliseconds

Table 3. Execution Benchmark of MMM Step 3

<table>
<thead>
<tr>
<th>DataSize</th>
<th>Framework</th>
<th>Time</th>
<th>Type</th>
<th>Levels</th>
</tr>
</thead>
<tbody>
<tr>
<td>50000*2000</td>
<td>MASS</td>
<td>7285</td>
<td>RandomAccessFile</td>
<td>20</td>
</tr>
<tr>
<td>50000*2000</td>
<td>Sequential</td>
<td>9549</td>
<td>RandomAccessFile</td>
<td></td>
</tr>
<tr>
<td>20000*2000</td>
<td>MASS</td>
<td>5208</td>
<td>RandomAccessFile</td>
<td>20</td>
</tr>
<tr>
<td>20000*2000</td>
<td>Sequential</td>
<td>3750</td>
<td>RandomAccessFile</td>
<td></td>
</tr>
<tr>
<td>50000*2000</td>
<td>MASS</td>
<td>15690</td>
<td>RandomAccessFile</td>
<td>10</td>
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<tr>
<td>20000*2000</td>
<td>MASS</td>
<td>7750</td>
<td>RandomAccessFile</td>
<td>10</td>
</tr>
</tbody>
</table>

Appendix 4. Screenshot of running MMM step 1 with MASS

```
1    Data path: /tmp/xiaotli/data/2048_2048/2048_2048.csv
2    Time Elapsed of initializing MASS = 14461
3    Time Elapsed of creating palces = 83
4    Time Elapsed of reading input files at each place= 857
5    Time Elapsed of Agents creation = 186
6    Time Elapsed of subMatrix alignment = 195
7    Time Elapsed of subMatrix shifting = 4360
8    Time Elapsed of gathering the final matrix = 371
9    Total time Elapsed = 20142
```
Appendix 5. Screenshot of running MMM step 1 with MPI Java

![Screenshot of running MMM step 1 with MPI Java](image)

Appendix 6. Screenshot of running MMM step 3 with MASS

![Screenshot of running MMM step 3 with MASS](image)

Appendix 7. Functions that are used in RandomAccessFile

```java
protected void openWithRandomAccessFile(String filePath):
    this method takes the given
    filePath, determines the file’s location and whether its type is supported. For reading with
    RandomAccessFile, currently we only accept CSV files. If the file type is supported, it creates a
    random access file stream to read from. Additionally, the random access file also expects each
```

line in the input file to have the same alignment so that the user can use row index to access data of full row. To meet the even alignment requirement, rows need to have the same number of characters. Since we don't support writing bytes back to the file, we use “r” (read only) mode to open the file. A new FileDescriptor object is created to represent the connection to the file, and a random access file stream will be put into the random access file table of the current working place. The openWithRandomAccessFile method is synchronized to ensure only one place opens the file as well as the file table. The file table is organized using filePath as the key and random access file stream object as the value.

```java
protected void openWithRandomAccessFile(String filePath) throws IOException {
    synchronized (RAFileTable) {
        if (RAFileTable.containsKey(filePath)) {
            logFormattedDebug(formattedLog: "Index: %d, %d, put into RandomAccessFile Table", getIndex()[0], getIndex()[1]);
            RandomAccessFile file = new RandomAccessFile(filePath, mode: "r");
            RAFileTable.put(filePath, file);
        }
    }
}
```

**public RandomAccessFile getFileFromRandomAccessFileTable(String filePath):** this method takes one parameter and returns the corresponding random access file stream object. This method is also synchronized for preventing thread interference and memory consistency errors.

```java
public RandomAccessFile getFileFromRandomAccessFileTable(String filePath) throws IOException {
    synchronized (RAFileTable) {
        if (RAFileTable.containsKey(filePath)) {
            logFormattedDebug(formattedLog: "Index: %d, %d, get from RandomAccessFile Table", getBaseName()[0], getBaseName()[1]);
            return RAFileTable.get(filePath);
        } else {
            throw new IOException("Can not find file by the filePath");
        }
    }
}
```

**public double[][] getArrayFromRandomAccessFile(RandomAccessFile file, int rowIndex, int rows):** this method takes three parameters in total, which are random access file stream object, the row index and the number of total rows. This method calculates the length of the file and
divides it by the number of rows to get byte length of each row. The file-pointer offset is set to the starting point of the corresponding row and reads the whole line. This method converts byte array to double array and returns the data back.