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Genetics 453

# Evolutionary Genetics

## Population Genetics, part 2

Joe Felsenstein

Department of Genome Sciences  
University of Washington, Seattle

email: [joe@genetics.washington.edu](mailto:joe@genetics.washington.edu)

# Mutation Rates

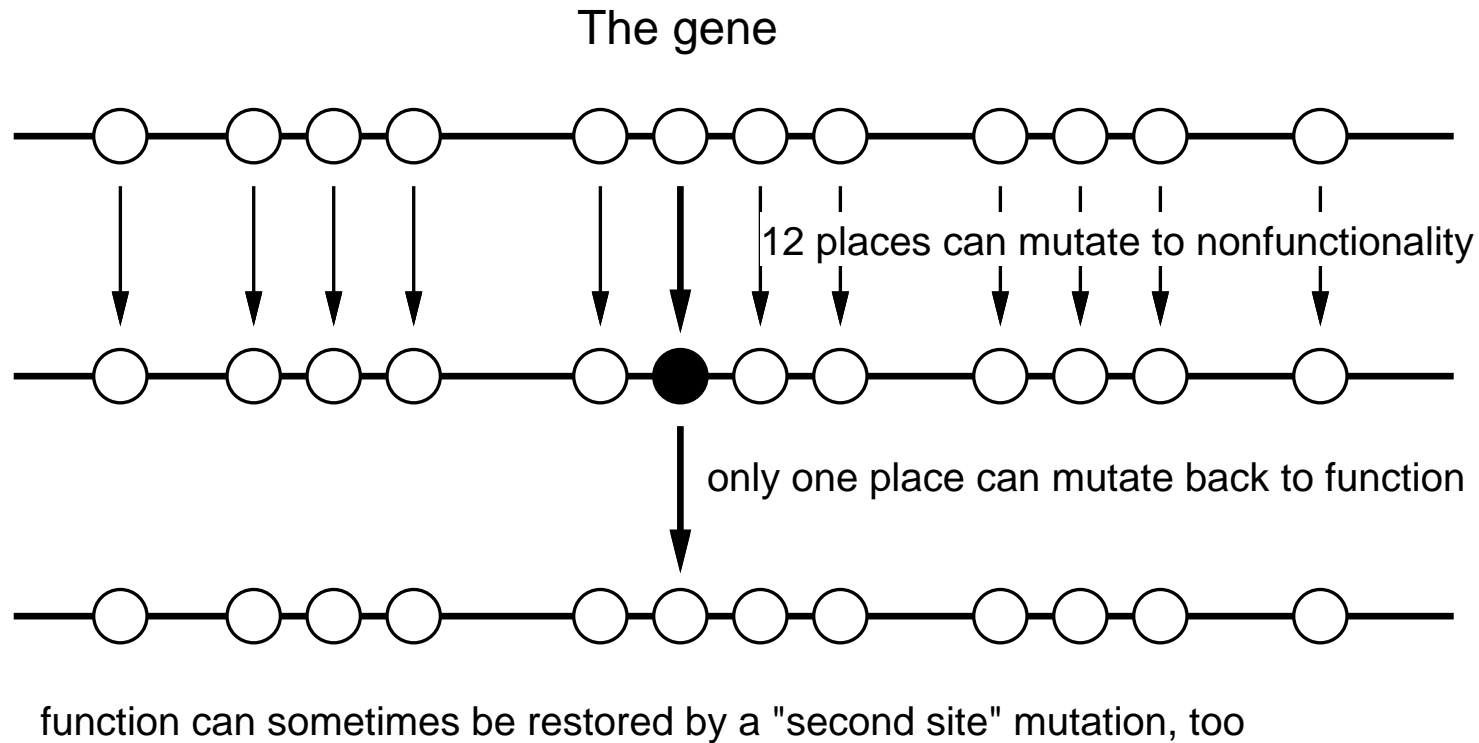
Coat color mutants in mice. From

Schlager G. and M. M. Dickie. 1967. Spontaneous mutations and mutation rates in the house mouse. *Genetics* **57**: 319-330

Locus	Gametes tested	No. of Mutations	Rate
Nonagouti	67,395	3	$4.4 \times 10^{-6}$
Brown	919,619	3	$3.3 \times 10^{-6}$
Albino	150,391	5	$33.2 \times 10^{-6}$
Dilute	839,447	10	$11.9 \times 10^{-6}$
Leaden	243,444	4	$16.4 \times 10^{-6}$
Total	2,220,376	25	$11.2 \times 10^{-6}$

Trait	Population examined	Mutation rate	Number of mutants/10 <sup>6</sup> gametes	Authors
A. Autosomal mutations				
Achondroplasia	Denmark	$1 \times 10^{-5}$	10	Mørch, corrected by Slat Stevenson
	Northern Ireland	$1.3 \times 10^{-5}$	13	
Aniridia	Germany (Reg. Bez. Münster)	$6-9 \times 10^{-6}$	6-9	Schiemann Møllenbach, corrected by Penrose
	Denmark	$2.9(-5) \times 10^{-6}$	2.9(-5)	
Dystrophia myotonica	Michigan (U.S.A.)	$2.6 \times 10^{-6}$	2.6	Shaw et al. Lynas Klein, corrected by Todorov et al.
	Northern Ireland	$8 \times 10^{-6}$	8	
	Switzerland	$1.1 \times 10^{-5}$	11	
Retinoblastoma	England, Michigan (U.S.A.), Switzerland, Germany	$6-7 \times 10^{-6}$	6-7	Vogel  Czeizel et al. Schappert-Kimmijser et al. Matsunaga Briart-Guillemot et al.
	Hungary	$6 \times 10^{-6}$	6	
	The Netherlands	$1.23 \times 10^{-5}$	12.3	
	Japan	$8 \times 10^{-6}$	8	
	France	$5 \times 10^{-6}$	5	
Acrocephalosyndactyly (Apert's syndrome)	England	$3 \times 10^{-6}$	3	Blank Tünte and Lenz
	Germany (Reg. Bez. Münster)	$4 \times 10^{-6}$	4	
Osteogenesis imperfecta	Sweden	$0.7-1.3 \times 10^{-5}$	7-13	Smårs Schröder
	Germany (Reg. Bez. Münster)	$1.0 \times 10^{-5}$	10	
Tuberous sclerosis (epiloia)	Oxford Regional Hospital Board Area (G.B.)	$1.05 \times 10^{-5}$	10.5	Nevin and Pearce  Singer
	Chinese	$6 \times 10^{-6}$	6	
Neurofibromatosis	Michigan (U.S.A.)	$1 \times 10^{-4}$	100	Crowe et al. Sergeyev
	Moscow (U.S.S.R.)	$4.4-4.9 \times 10^{-5}$	44-49	
Polyposis of intestines	Michigan (U.S.A.)	$1.3 \times 10^{-5}$	13	Reed and Neel
Marfan's syndrome	Northern Ireland	$4.2-5.8 \times 10^{-6}$	4.2-5.8	Lynas
Polycystic disease	Denmark	$6.5-12 \times 10^{-5}$	65-120	Dalgaard

# Why mutants inactivating a functional gene will be more frequent than back mutations



## Sequence space

For sequences of length 1000, there are  $3 \times 1000 = 3000$  "neighbors" one step away in sequence space

But there are  $4^{1000}$  sequences, which is about  $10^{602}$  in all !

No two of them are more than 1000 steps apart

Hard to draw such a space

How do we ever evolve? Wouldn't it be impossible to find one of the tiny fraction of possible sequences that would be even marginally functional?

The answer seems to be that the sequences are clustered

An example of such clustering is the English language, as illustrated by a popular word game:

W	O	R	D
W	O	R	<b>E</b>
<b>G</b>	O	R	E
G	O	<b>N</b>	E
G	<b>E</b>	N	E

But the word BCGH  
cannot be made into  
an English word

There are also only a tiny fraction of all 456,976 four-letter words that are English words

But they are clustered, so that it is possible to "evolve" from one to another through intermediates

## Estimation of a human mutation rate

By an equilibrium calculation. Huntington's disease. Dominant. Does not express itself until after age 40. Reduction in fitness maybe 2%.

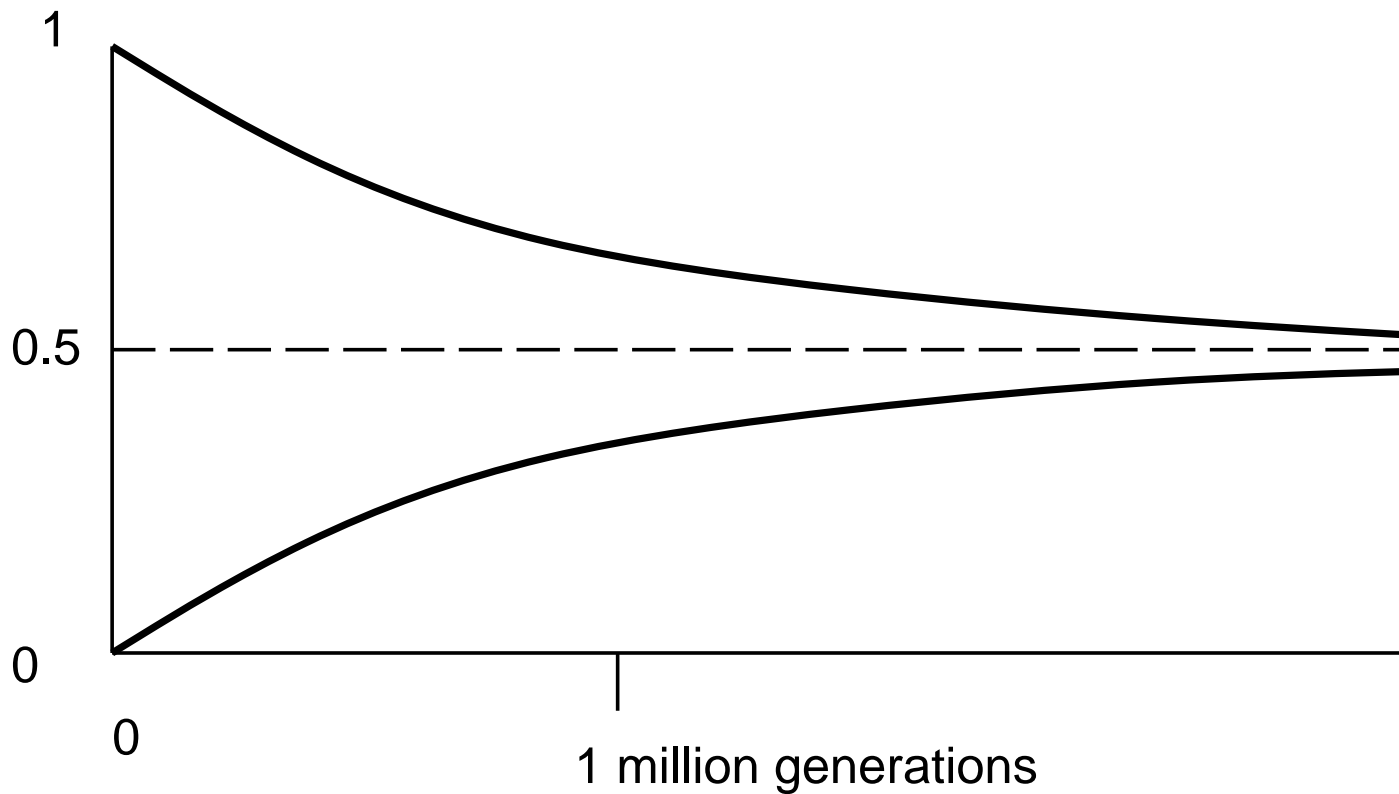
If allele frequency  $q$ ,  $2q(1 - q)$  of everyone are carriers. 0.02 of these die. Each has half its copies the Huntington's allele. So as fraction of carriers  $\simeq 1/100,000$ , the fraction of all copies that are mutations that are eliminated is  $0.00001 \times 1/2 \times 0.02 \simeq 10^{-7}$

If we are at equilibrium between mutation and selection, this is also the fraction of copies that have a new mutation.

Similar calculations can be done with recessive alleles.

## Mutation as an evolutionary force

If we have two alleles  $A$  and  $a$ , and mutation rate from  $A$  to  $a$  is  $10^{-6}$  and mutation rate back is the same,



Mutation is critical in introducing new alleles but is very slow

This freeware-friendly presentation prepared with

- Linux (operating system)
- PDFLaTeX (mathematical typesetting and PDF preparation)
- Idraw (drawing program to modify plots and draw figures)
- Adobe Acrobat Reader (to display the PDF in full-screen mode)

(except that we had to use Microsoft Windows to project this as the X server I have in Linux is not too great)