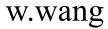
Moiré Method

Wei-Chih Wang University of Washington ME 557



Week 14

- Course Website: http://courses.washington.edu/me557/optics
- Reading Materials:
 - Week 14 reading materials are from:
- http://courses.washington.edu/me557/readings/
- Proposal due today!
- Individual meeting with me on final project Thursday afternoon.
- Continue Prims Project presentation (later after the lecture)
- Make sure you finish Lab 2 this week
- Final project presentation (6/11 afternoon).
- Final report due 6/18 5PM electronic copy must send to me not TA (abong@uw.edu)



Last Week

- Light sources
 - Chemistry 101, orbital model-> energy gap model (light in quantum), spectrum in energy gap
 - Broad band light sources (Orbital energy model, quantum theory, incandescent filament, gas discharge, LED)
 - LED (diode, diode equation, energy gap equation, threshold voltage, device efficiency, junction capacitance, emission pattern, RGB LED, OLED)
 - Narrow band light source (laser, Coherence, lasing principle, population inversion in different lasing medium- ion, molecular and atom gas laser, liquid, solid and semiconductor lasers, laser resonating cavity- monochromatic light, basic laser constitutive parameters)



This Week

- Photodetectors
 - Photoemmissive Cells
 - Semiconductor Photoelectric Transducer
 (diode equation, energy gap equation, reviser bias voltage, quantum efficiency, responsivity, junction capacitance, detector angular response, temperature effect, different detector operating mode, noises in detectors, photoconductive, photovoltaic, photodiode, PIN, APD, PDA, PSD, CCD, CMOS detectors)
 - Thermal detectors (IR and THz detectors)



This week

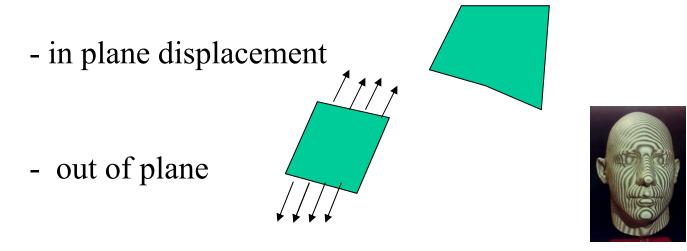
- Radiometry and Photometry
- Free Space Optics:
 - Geometric Moir
 - Shadow Moire
 - Projection Moire
 - Moire Interference
 - DIC

Moiré Methods

Moiré = The French name fro a fabric called "water silk", fabric Exhibits patterns of light/dark bands

Moiré Fringes: or the Moiré effect" refers to light/dark bands seen By superimposing two nearly identical arrays of lines or dots

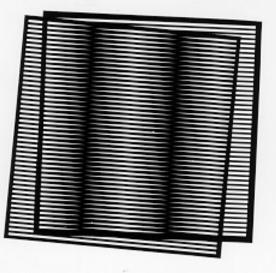
In most basic form, Moiré methods are used to measure Displacement fields; either



Geometric Moiré

Moiré effect is the mechanical interference of light by superimposed network of lines.

The pattern of broad dark lines that is observed is called a moiré pattern.



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Superimposed Gratings

Application of Geometric Moiré

- Specimen attaches to specimen surface ("specimen grating")
- Specimen viewed through a fixed grating ("reference grating")
- Specimen loaded, causing deformation/rotation of specimen grating -> Moiré fringe pattern develops.

Fringes are caused by two distinct mechanisms:

- Mismatch in pitch between reference and specimen grating (occurs due to deformation of specimen grating in the primary direction)
- Rotation of specimen grating with respect to reference grating (...rigid body rotations usually not of interest..)

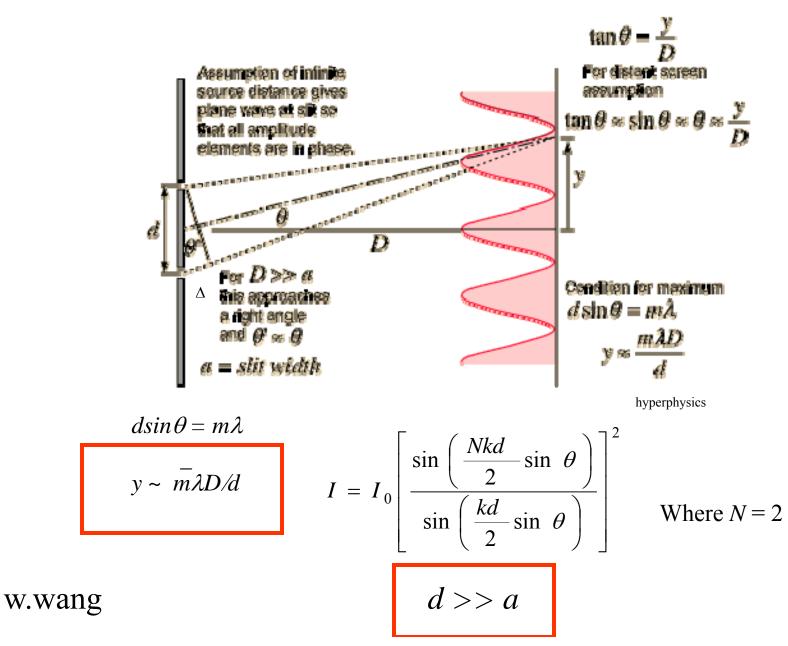
w.wangin practice, both deformation and rotation occur simultaneously

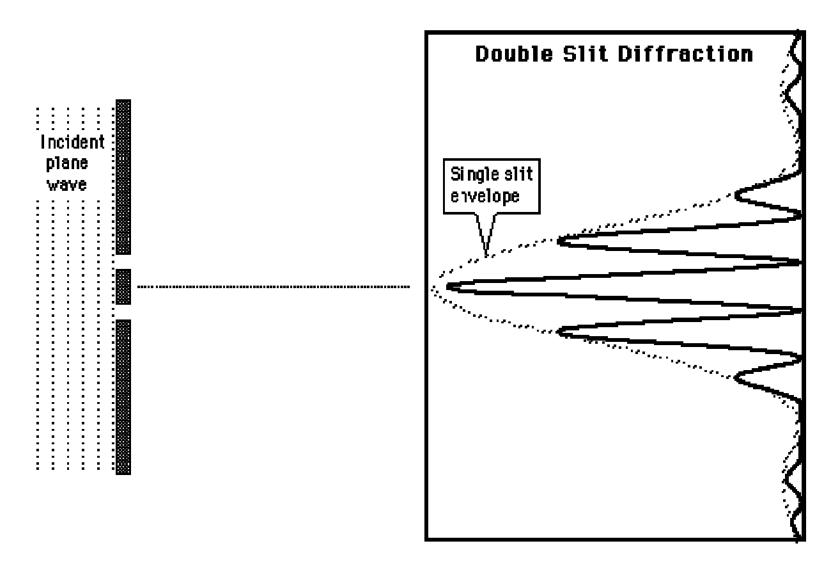
Moiré methods can be grouped into two major groups:

- 1. Geometric Moiré
 - Fringes patterns can be interfered based strictly on "geometry"
 - in-plane Moiré in-plane displacement
 - shadow Moiré out of plane displacement
 - out of plane Moiré
- 2. Moiré interferometry
 - Interference of fringes seen required consideration of diffraction effects. (grating frequency is higher than geometric moiré)

Moire is one type of spatial interference Interference magnify the signal so we can measure it more easily!

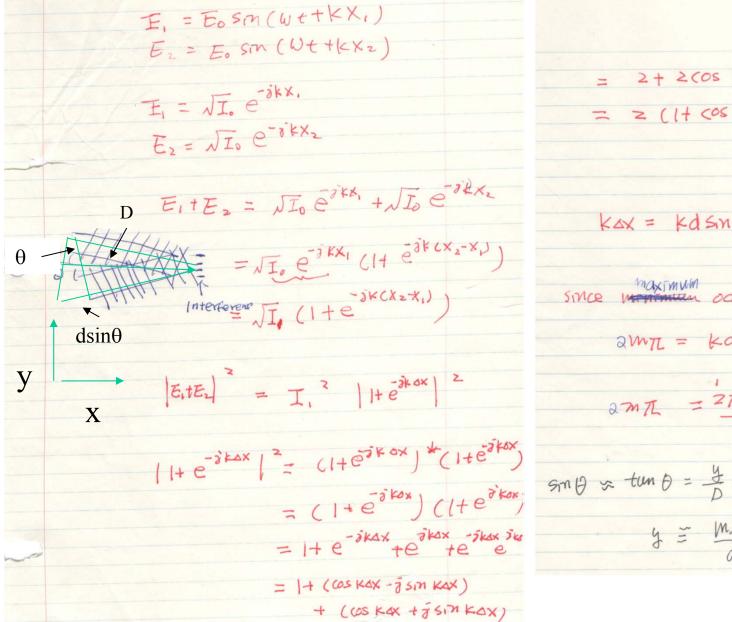
Double Slits Interference





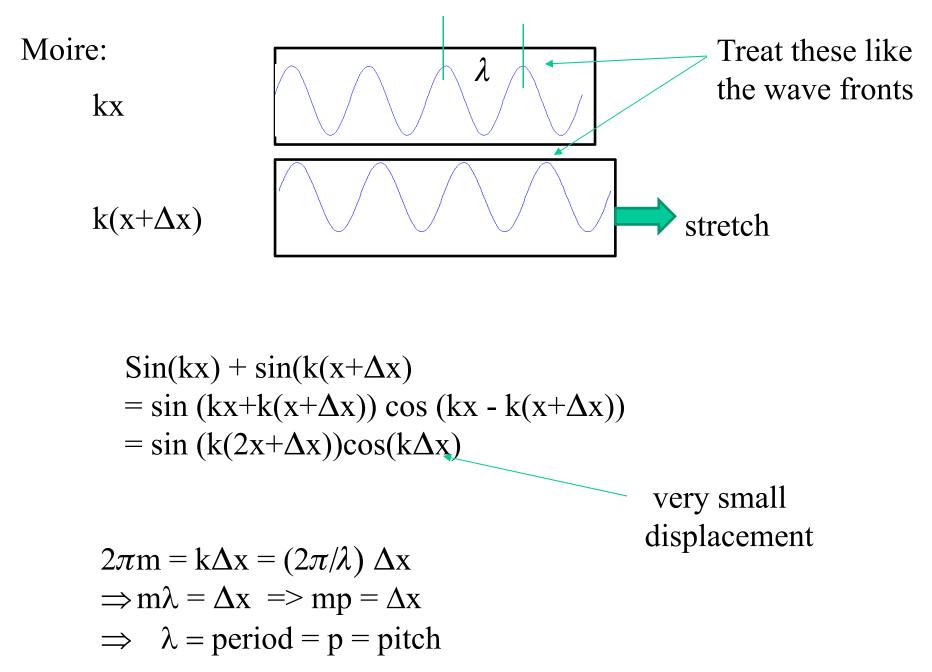
Slit separation ~ slit width N=2 interference due to two waves separate by a distance d

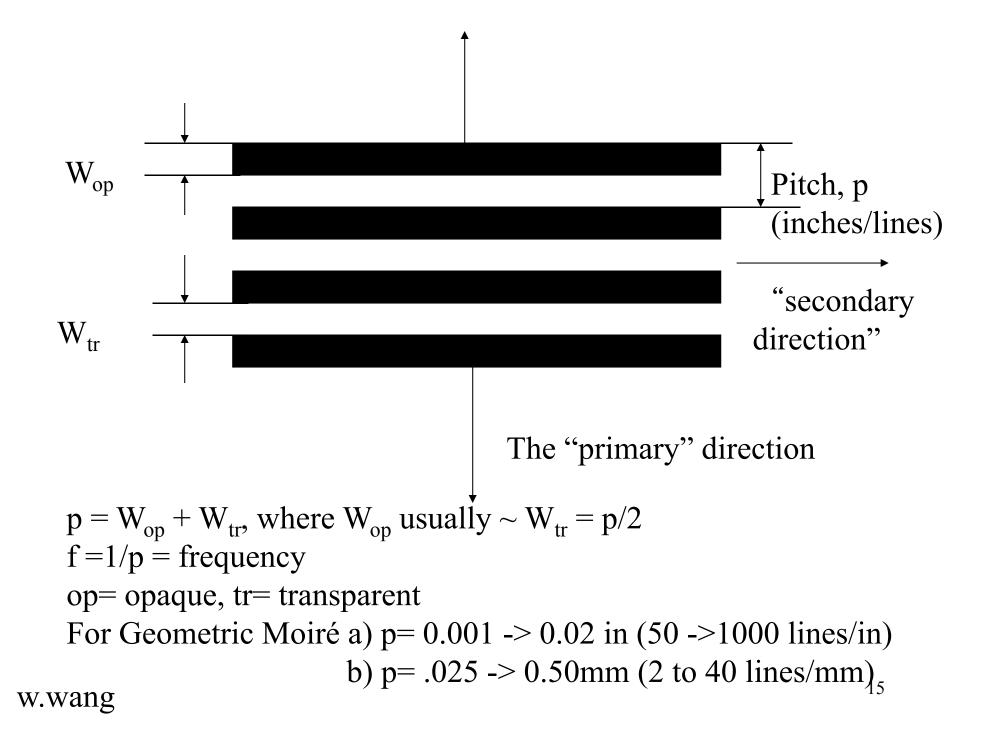
Spatial interference formed by two coherent light separated by an angle θ



1+ (0520 = 2005 CA. 2+ 2 COS KAX = 2 (1+ cos kax) = 4 cos² (kax) KAX = KdSm(9) Since maniner occurs @ 2mm amit = Kdsino amTL = ZTLdSing y = MAD

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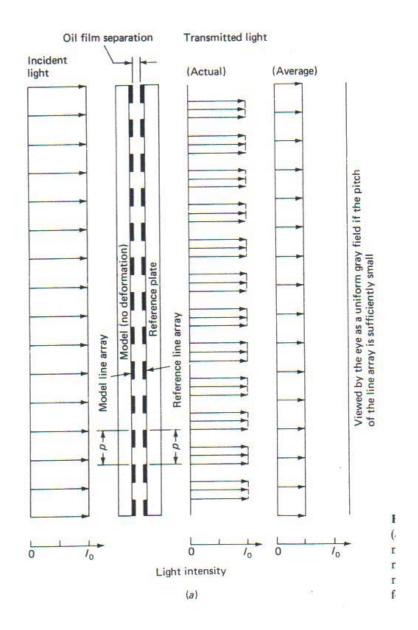




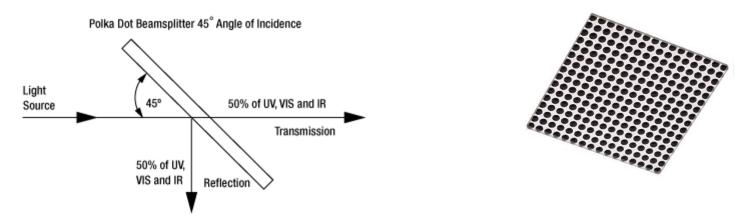
Intensity distribution is due to superposition of two gratings:

* Any region with single line or two superposed lines appears black.

* Any region not covered by either set of lines will appear light.



Polka Dots Beam Splitter



The metal coating is applied in a regularly repeating array, which lends the beamsplitter its "polka dot" appearance, as shown to the right. Light is reflected by the metal-coated portion of the beamsplitter and transmitted through the uncoated portion of the beamsplitter. To maximize the reflected intensity, light should be incident on the coated side of the beamsplitter. The square dots have 0.0040" (100 μ m) [UVFS, B270, and CaF₂] or 0.0042" (107 μ m) [ZnSe] sides. The spacing between the dots is 0.0022" (56 μ m) [UVFS, B270, and CaF₂] or 0.0018" (46 μ m) [ZnSe] in all directions.

Polka dot beamsplitters are typically used at a 45° angle relative to the incident beam as shown in the diagram above. Our polka dot beamsplitters transmit $50\% \pm 5\%$ ($\pm 10\%$ for ZnSe) when a beam is larger than 2 mm in diameter.

Grating and Specimen Preparation

Grating can be formed by holographic interference technique, ebeam writing, X-ray lithography, Phase mask etc.

Grating transferred to metal specimen by lithography using photosensitive coating or photoresist or dichromate gelatin on specimen. (show example on metal specimen)

Gratings are usually 20 to 40 lines/mm (500 to 1000 lines/in) line width is approximately 50% of the pitch (maximum grating strength) (show grating plates)

Sub-micron Lithography

1. Optical Lithography-using lenses to reduce a mask image onto target (smallest feature size~ .25 μ m) Phase shift, phase edge or overexpose/overdevelop – 0.1 μ m

Phase grating mask interference (near-field holography)- minimize 0th order Diffraction and emphasize ± 1 orders interferences. period of standing wave = $\frac{1}{2}$ of period of phase grating mask

2. X -ray lithography – requires mask made by EBL resolution $\sim .25 \mu m$

3. Ion beam lithography- damage from ion bombardment limited on Film thickness, advantages no proximity effect so line width control Is good. Possibility of ion beam assisted etching.

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4. EBL- 50nm (NTU) 20nm (UW)
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A commercial electron beam lithography tool. (courtesy of JEOL Ltd.)

E-beam process

Problem- difficult to achieve accurate pattern placement

Large area patterns are formed by stitching together mosaic of small fields or stripes. Are within each field is accessed by deflecting the focus beam, while successive fields are written by moving the substrate.

Field distortion: Thermal expansion, charging, beam current and focus drift, Stiching error

Solution- spatial phase locked e beam lithography, pre exposed film with interference pattern which generates a spatial reference pattern

Lithographic Techniques for gratings

Interference Lithography:

TraditionalAr ion laser (488nm), AZ1350, az1512– long exposure
He-Cd laser(325nm),Shipley Ultra-123

Thin oxide layer and ARC are needed to prevent reflection from the substrate Honeywell has some ARC materials (free)

Techniques: two arms interference (MachZenhder, Michelson) Lloyd's mirrors problem- small spot, incident waves spherical (collimate light to plane wave) reflection from substrate creates secondary standing waves in orthogonal direction leads to poor line width control and ripple edges

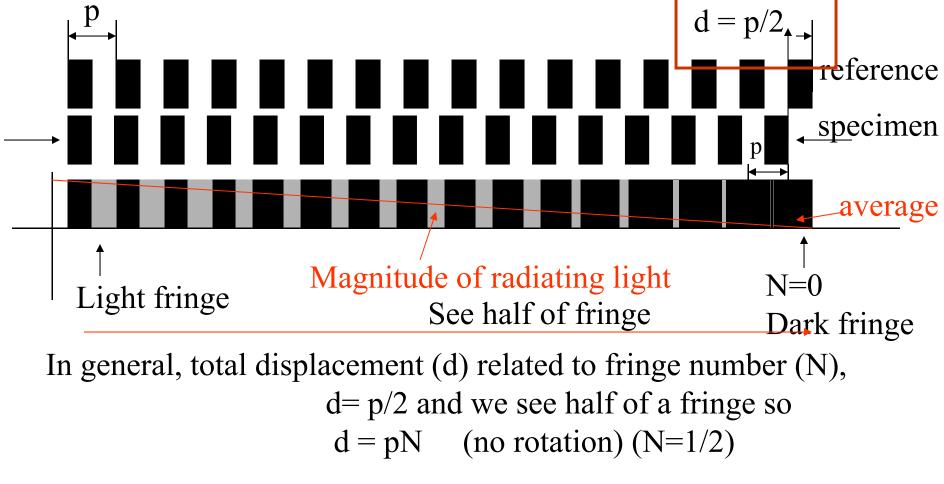
Generating and recording fringe pattern

Direct contact – oil film between specimen and reference gratings

Optical contact- photograph specimen grating before loading, and re-photograph the same specimen grating on the same film creating double exposure. The unloaded specimen grating serve as reference grating. (intensities are different)

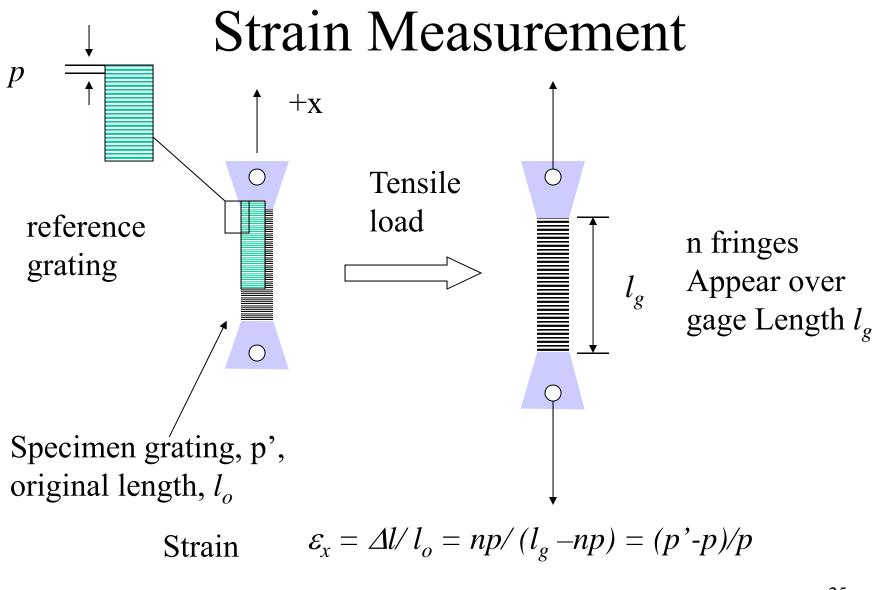
Moiré Fringe Pattern

Case 1. Uniform deformation in primary direction (assume compression)



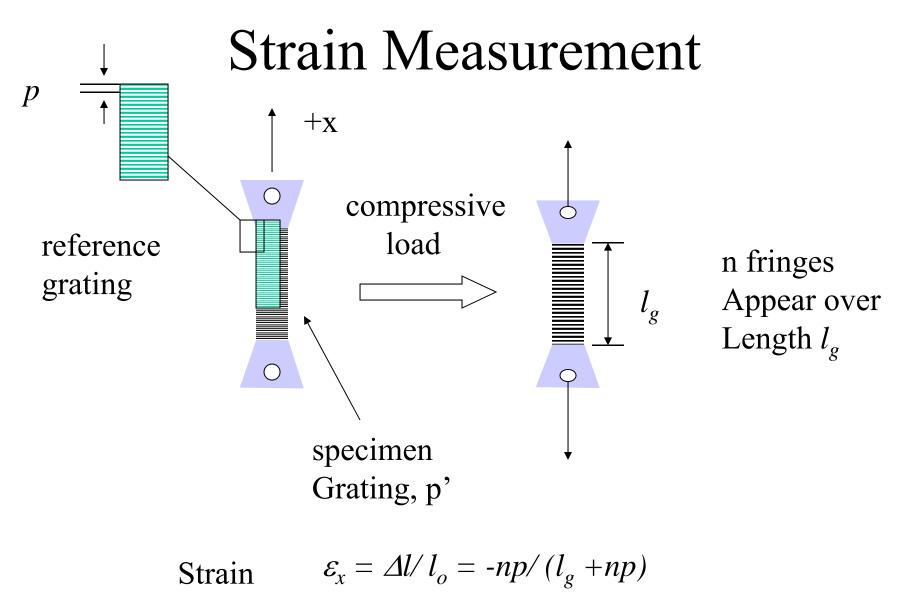
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N = d/p (fix d, N increases p decreases)⁴

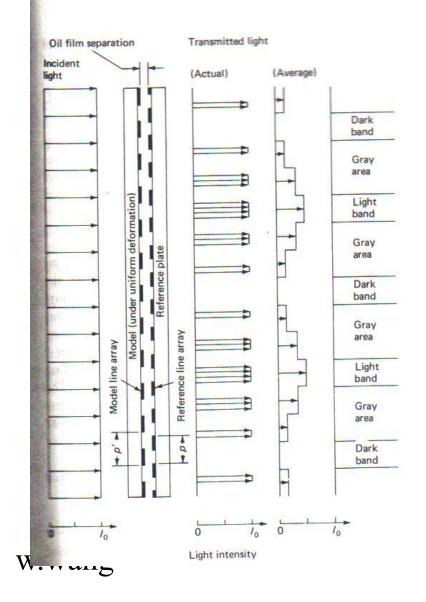


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Apply this in point by point fashion



Example



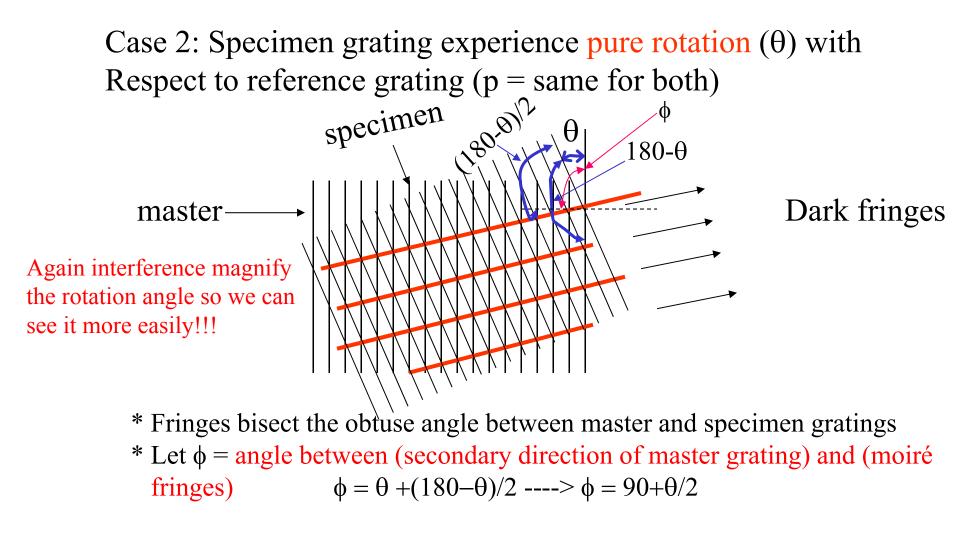
p = 0.025mm and 32 fringes have formed in 25mm gage length indicated on the specimen. Thus the change in length of the specimen in 25mm interval is

$$\Delta l = np = 32 \ (0.025) = 0.8 \ (mm)$$

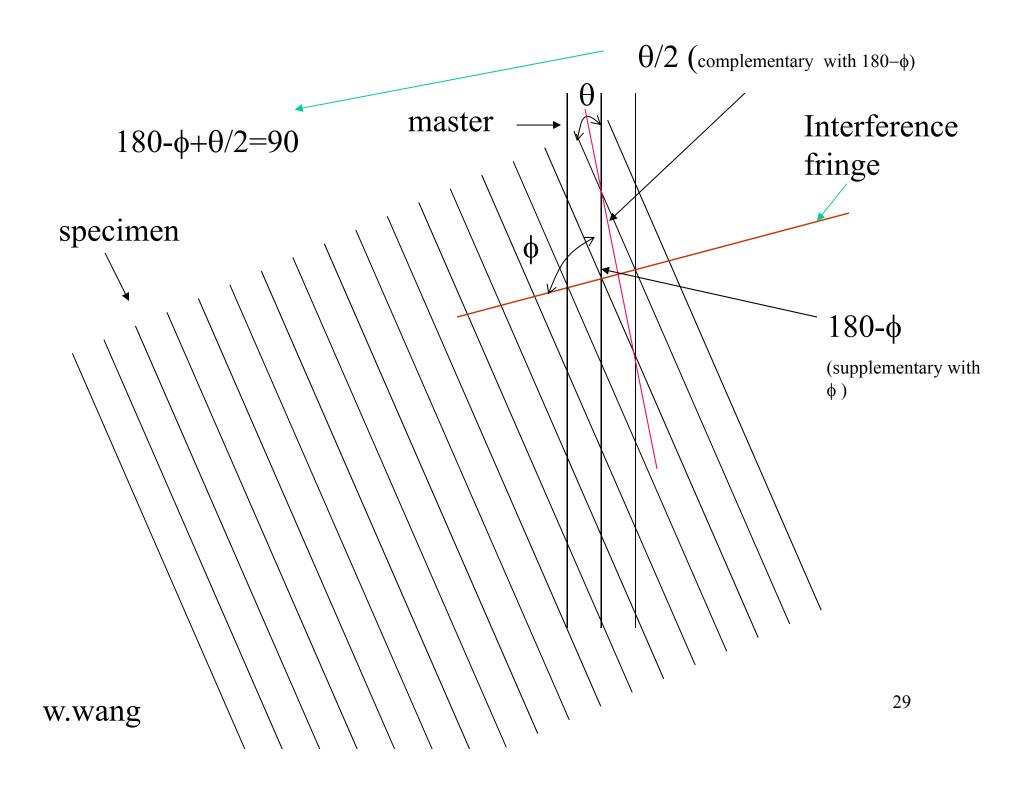
$$\varepsilon = \Delta l/l_o = np/(l_g - np) = 0.8/(25 - 0.8) = 0.033$$

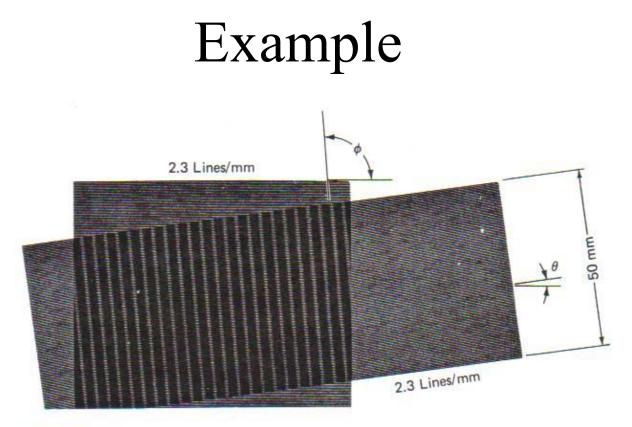
Gage length is l_g

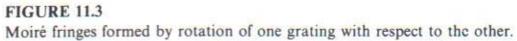
Moiré Fringe Pattern



 $\theta = 2 \phi - 180$ (gives orientation of specimen grating)





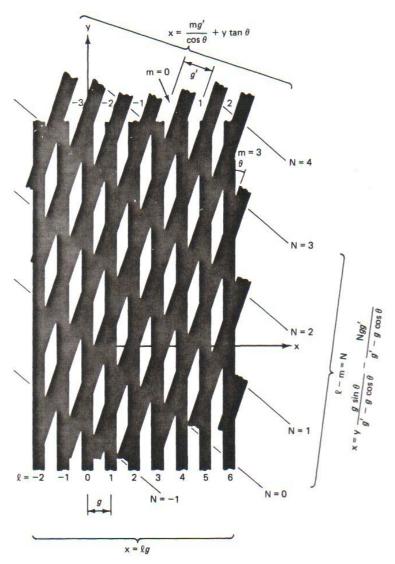


pure rotation

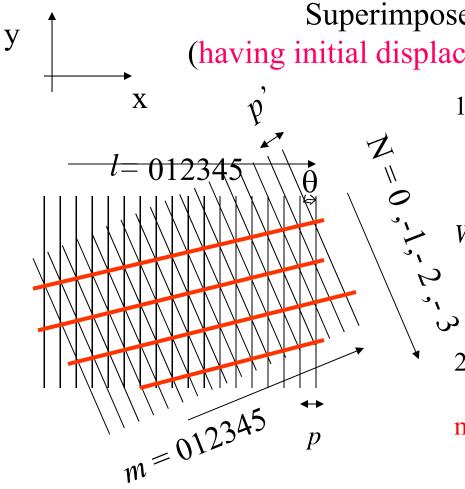
Find ϕ solve θ

Moiré Fringe Pattern

Case 3. Specimen grating experiences an unknown deformation $(p \rightarrow p')$ and unknown rotation (θ) causing fringe pattern







Superimposed gratings (having initial displacement and rotation)

1st Family of lines along x direction

x = lp

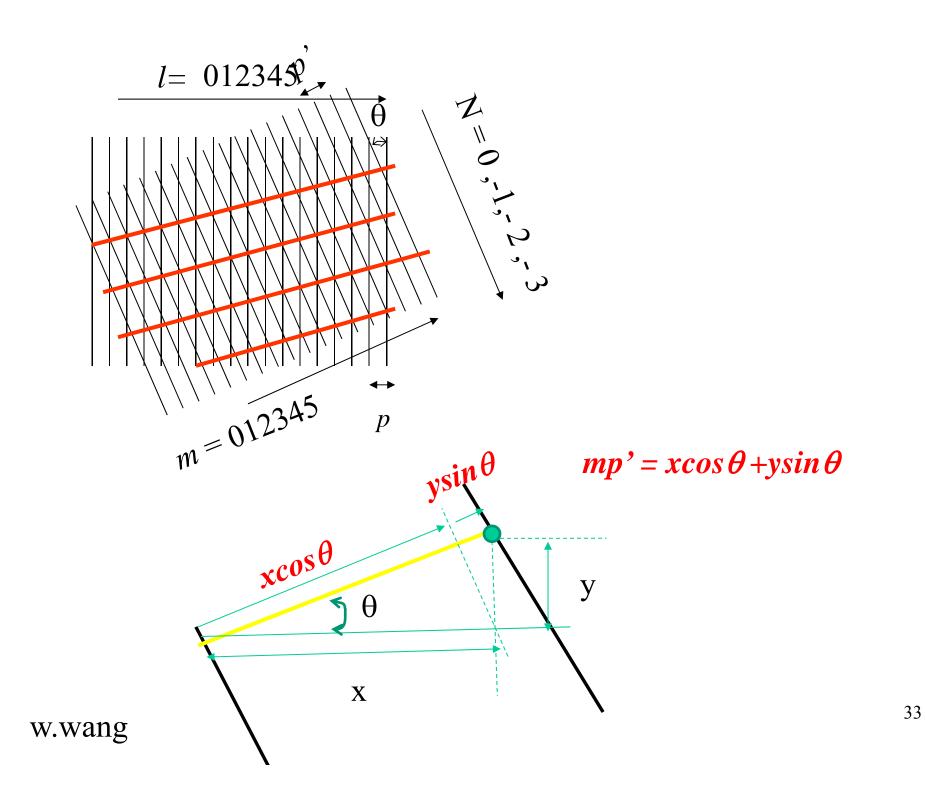
Where l = integer*p*= *pitch for specimen grating* in x direction

 2^{nd} Family of lines at a small angle θ

mp' as a function of x and y :

 $mp' = x\cos\theta + y\sin\theta$ or $x\cos\theta = mp' - y\sin\theta$

$$m - l = N$$
 (moiré fringe number)



Small angle rotation and approximation approach

$$m-l = N \longrightarrow (x\cos\theta + y\sin\theta)/p' - x/p = N$$

--->
$$((pcos\theta m - p')x + pysin\theta)/pp' = N$$

If rotation is kept small,

$$(p-p')x + p\theta y = Npp'$$

(remember $\cos\theta \sim 1$ also the whole reason is to measure small θ)

Or

$$x(p-p')/p + \theta y = Np'$$

 $(p-p')/p = \text{length change}/\text{ original length} = \varepsilon_x$ (strain in x direction)

$$\varepsilon_{x} x + \theta y = Np'$$

Equation implies N depends on the initial pitches of the the gratings, and their initial relative position and orientation.

Fringe shift can be used to measure the change of pitch (strain), change in relative position (translation) and orientation (rotation)

Knowing p, we can measure d (distance between two interference fringes), ϕ (angle between fringe and x axis) based on θ and find pitch on specimen p'. How?

Moiré Fringe Patterns

* Two approaches: "geometric approach" and "calculus approach" (also called "displacement field" approach)

Knowing p, we can measure d (distance between two interference fringes), ϕ (angle between fringe and x axis) based on θ and find pitch on specimen p'.

In-plane displacement field using Moiré fringe analysis (exact solution)

Geometrical approach (point by point measurement):

(uses measurement of fringe spacing and inclination at points of interested to determine strain)

- 1. Define x-y coordinate system, with x-axis = primary direction
- 2. Reference (master) grating thought as a "family" of lines given by;

$$x = lp' \tag{1}$$

l is integer increasing in $+\theta$ direction, order number of each line

3. Specimen grating thought of as 2nd "family" of straight lines, given by,

 $x = mp/cos\theta + ytan\theta$ (2) m is integer increasing in + θ direction, p is the pitch of specimen

4. Moiré fringes occur wherever:

$$l - m = N \tag{3}$$

N is integer moiré fringe order

In-plane displacement field using Moiré fringe analysis

Combine equation 1 to 3,

$$(p'-p\cos\theta)x + (p\sin\theta)y - Npp' = 0$$
(4)

This is the form of a third family of straight lines, of the general form:

[A]x + [B]y + [C] = 0

Look at my note and slide 31.. We see the two values in x nd y axes and the hyptenue is d fringe spacing so rotation angle is phi and magnitude of fringe displacement is d (Linear equation)

The distance between two moiré fringes (interference), d is

$$d = \frac{C}{(A^2 + B^2)^{0.5}} = \frac{pp'}{(p^2 \sin^2 \theta + (p' - p \cos \theta)^2)^{0.5}}$$
(5)

The slope of the fringe, ϕ is also easily measured, from equation 4:

$$tan \phi = -psin\theta / (p' - pcos\theta)$$
(6)

In-plane displacement field using Moiré fringe analysis

Equation 5 and 6 can be rearrange to give:

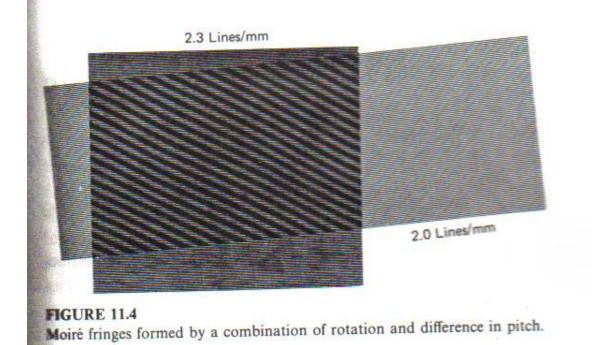
 $p = d / (1 + (d/p')^{2} + 2(d/p') \cos \phi)^{0.5}$ (7) $\theta = tan^{-1} (\sin \phi / ((d/p') + \cos \phi))$ (8)

Allows calculation of the pitch p and orientation θ of the specimen grating in terms of the reference grating pitch p' and easily measure feature of the moiré fringes distance (d) and angle (ϕ)

Limit is 300 rotation and 30% strain

Looking at large area
 displacement

Example



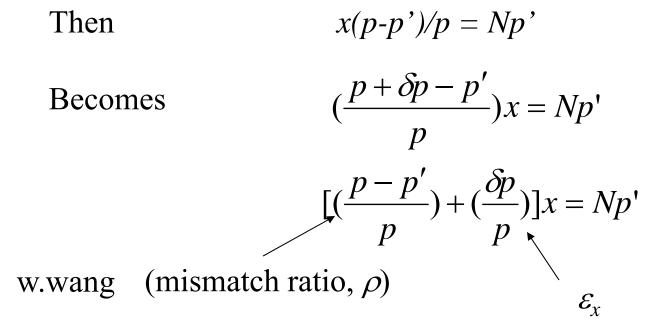
Mathematica Program

C:\Users\victor\Desktop\NTHU_PME_201
 6/moire generator-2-23 18/MoirePatterns.cdf

Pitch Mismatch

Difference of pitch between the model and master grills will cause Moiré fringes to form even though the model is unstrained.

Let $\theta = 0$, p = original pitch for the model grating, p' =pitch of master Grating, δp = change in p caused by strain

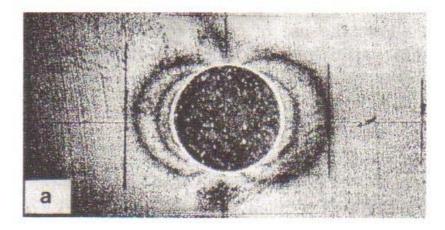


$$\rho + \varepsilon_x x = Np'$$
$$\varepsilon_x = \frac{Np'}{x} - \rho$$

This equation eliminates the effects of initial pitch mismatch.

 ρ is essentially the pacing of moire fringes in the initial pattern observed before straining the model

 $\rho x = N_i$ = initial fringe order



Pitch mismatch Creating more fringes For same displacement

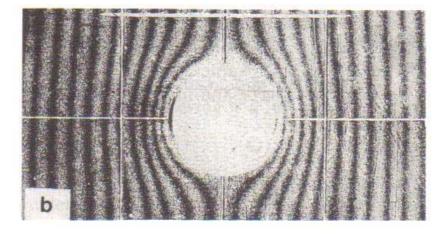


Figure 8.13. Sample geometrical moire pattern for a deformed body taken (a) without mismatch and (b) with a small pitch mismatch (patterns optically filtered) (Cloud 1980).

Whole field analysis

-Whole field as rotations and displacements of a large number of small portions

-moiré fringes will vary in a complicated but continuous way over the extend of the field

-At any point , the fringe order will indicate appropriate mixture of displacement and rotation

-it is not essential the fringes be numbered beginning from zero because <u>only the</u> <u>spacing of the fringes</u> (the partial derivative with respect to position) is of any consequence

Moiré basically just another transformation from Cartesian Coordinate into another coordinate. <u>A and B are transformation</u> <u>Factor</u> d is resulting magnitude and ϕ is the resulting angle (i,e. Z transform or Fourier transformation...)

Calculus Approach

In theory of elasticity, strain is relate to displacement u_x and u_y as,

$$\varepsilon_{xx} = \frac{\partial u_x}{\partial x} \qquad \varepsilon_{yy} = \frac{\partial u_y}{\partial y}$$

(strain in x and y direction)

$$\varepsilon_{xy} = \frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial x}$$

shear strain

$$\omega_{xy} = \frac{1}{2} \left(\frac{\partial u_x}{\partial y} - \frac{\partial u_y}{\partial x} \right)$$

(average rotation of the x and y Coordinates)

Above equations can be used

- when load is small and rotations are neglected

or – where Cartesian coordinates need to be reorient where there is wwang rigid body rotation due to the load

General form of strain displacement relation

$$\varepsilon_{xx} = \sqrt{1 + 2\frac{\partial u_x}{\partial x} + (\frac{\partial u_x}{\partial x})^2 + (\frac{\partial u_y}{\partial x})^2} - 1$$

$$\varepsilon_{yy} = \sqrt{1 + 2\frac{\partial u_y}{\partial y} + (\frac{\partial u_y}{\partial y})^2 + (\frac{\partial u_x}{\partial y})^2} - 1$$

$$\varepsilon_{xy} = \arcsin\frac{\frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial x} + \frac{\partial u_x}{\partial x}\frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial x}\frac{\partial u_y}{\partial y}}{(1 + \varepsilon_{xx})(1 + \varepsilon_{yy})} \qquad (\text{radians})$$

Applies to large strain and rotations, no u_z since moiré method is restricted in that direction.

If Cartesian strain ε_{xx} , ε_{yy} , ε_{xy} are small, the principle strains can be obtained from

$$\varepsilon_{1,2} = \frac{1}{2} [\varepsilon_{xx} + \varepsilon_{yy} \pm \sqrt{(\varepsilon_{xx} - \varepsilon_{yy})^2 + \varepsilon_{xy}^2}]$$

Moiré pattern is limited to strain ε of 30% and rotation θ of \pm 30°

Calculus Approach to Displacement Measurement

To apply 'calculus approach':

Load specimen/obtain Moiré patterns representing $u_{x, v}$

- cross grating used as specimen
- line gratings used as reference grating ()

a) Plot fringe orders (N_x, N_y) along lines originally in the x and y direction, -> note: coordinate locations must be adjusted:

$$x_{act} = x_{meas} - N_x p$$
$$y = y - N_x p$$

 $y_{act} - y_{meas} - iv_y P$ Location maybe insignificant if p is small

b) Plot fringes versus position

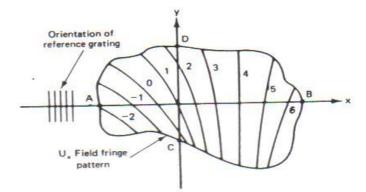
c) Take the slope of the plot at each point at which strain is required

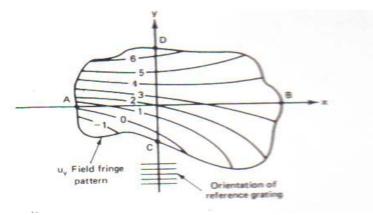
$$\frac{\partial u_x}{\partial x} = p \frac{\partial N_x}{\partial x} \quad \frac{\partial u_x}{\partial y} = p \frac{\partial N_x}{\partial y}$$
$$\frac{\partial u_y}{\partial y} = p \frac{\partial N_y}{\partial y} \quad \frac{\partial u_y}{\partial x} = p \frac{\partial N_y}{\partial x}$$

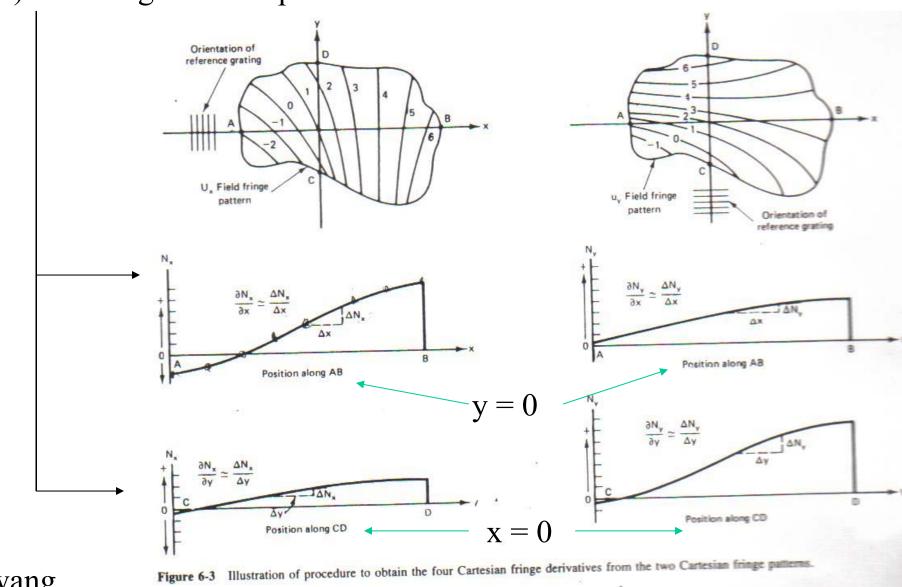
w.wang^d *Calculate strains using* general form of strain displacement relation 50 *This approach easily implemented using modern digital image process*



a) Record fringe orders along lines originally in the x and y direction







b) Plot fringes versus position

c) Take the slope of the plot at each point at which strain is required $\frac{\partial N_x}{\partial x}$ etc...

d) Plot back into general solution for strain displacement

$$\varepsilon_{xx} = \sqrt{1 + 2\frac{\partial u_x}{\partial x} + (\frac{\partial u_x}{\partial x})^2 + (\frac{\partial u_y}{\partial x})^2 - 1}$$

$$\varepsilon_{yy} = \sqrt{1 + 2\frac{\partial u_y}{\partial y} + (\frac{\partial u_y}{\partial y})^2 + (\frac{\partial u_x}{\partial y})^2} - 1$$

$$\varepsilon_{xy} = \arcsin\frac{\frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial x} + \frac{\partial u_x}{\partial x}\frac{\partial u_x}{\partial y} + \frac{\partial u_y}{\partial x}\frac{\partial u_y}{\partial y}}{(1 + \varepsilon_{xx})(1 + \varepsilon_{yy})}$$

Problem in displacement field approach

In practice, when *u* and *v* moiré fringe patterns are obtained from $\frac{\partial u_x}{\partial x}$ and $\frac{\partial u_y}{\partial y}$, but the cross derivatives $\frac{\partial u_x}{\partial y}$ and $\frac{\partial u_y}{\partial x}$ can not provide the acceptable accuracy because of the slight errors in alignment of either the specimen or master grating with x and y axes. Misalignment produces a fringe pattern due to rotation in addition to the load-induced pattern

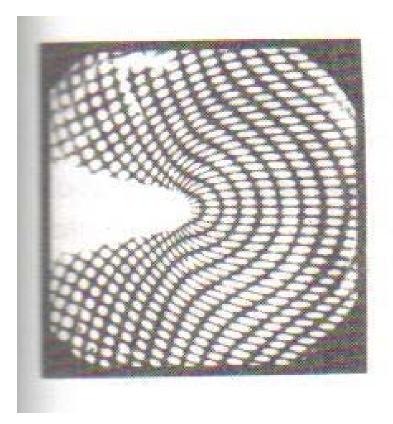
Solutions to shear-strain error

1. To eliminate shear-strain error by using crossed gratings on both the specimen and master to obtain simultaneous displays of the *u* and *v* displacement fields.

(rotation misalignment is then equal for the two fields, It contribution to the cross derivatives is equal in magnitude But opposite in sign and thus cancels in the shear-strain Determination)

Use slightly different pitches on the specimen and master (see Figure on page 41)

2. Using strain-rosette concept employ both perpendicular to x and 45° with respects to x axis. Then ε_{xx} , $\varepsilon_n \varepsilon_{yy}$ can be determined. Then use rosset equation to calculate the strain and stress w.wang ⁵⁵



You can Clearly see the difference in fringe pattern in x and y direction

Moire fringe pattern with crossed gratings of different Pitch on the mater and specimen

Ways to increase resolution

- Super Moire
- Fringe Multiplication
- Sharpening and Multiplication

Super Moiré

Superimpose of two identical moiré patterns

To apply 'moiré of moiré:

a) Load specimen/obtain Moiré patterns representing $u_{x_y} u_y$

Superimposed two identical moiré patterns (N_{xx} , N_{yy} , N_{yy} , N_{yy} are superfringe orders)

One pattern shifted to a known amount in x or y directions $(s_{xx}, s_{yy}, s_{yy}, s_{yy})$

- b) Plot fringes versus position
- c) Take the slope of the plot at each point at which strain is required

 $\begin{array}{ll} du_x/dx = p \; N_{xx} \, / \, S_{xx} & du_x/dy = p \; N_{xy} \, / \, S_{xy} \\ du_y/dy = p \; N_{yy} \, / \, S_{yy} & du_y/dx = p \; N_{yx} \, / \, S_{yx} \\ First subscript represents the direction perpendicular to the grating lines and the second to the direction of the shift \end{array}$

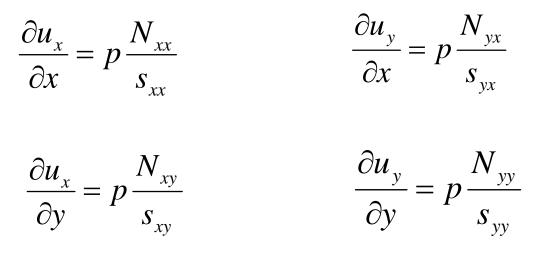
d) Calculate strains using general form of strain displacement relation

- Resolution is higher than other methods
- Fringes are harder to see

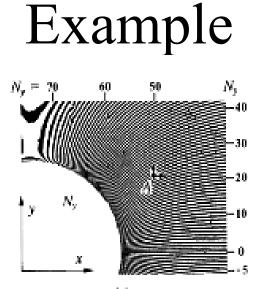
Super Moiré

Calculus approach can also be implemented using

Displacement derivatives are obtained using superfringes with the equations,



Where N_{xx} , N_{xy} , N_{yx} , N_{yy} are superfringe orders s_{xx} , s_{xy} , s_{yx} , s_{yy} , are respective shifts





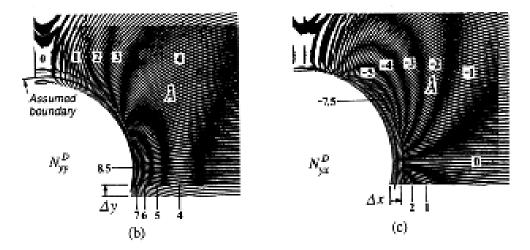


Fig. 4.51 Demonstration of the mechanical differentiation technique: (a) fringe pattern of N_y ; (b) super-moiré pattern obtained by superimposing two transparencies of the fringe pattern with a shift Δy ; (c) super-moiré pattern with a shift Δx . The numbers are fringe orders N_{yy}^D and N_{yz}^D , which depict the $\delta N_y/\delta y$ and $\delta N_y/\delta x$ fields, respectively.

w.wang

60

Fringe multiplication (increase fringe formation)

by having <u>two different frequency gratings</u>, we can increase the number of the moiré fringes produced by the same loading if original gratings were same period

i.e. If original gratings are both 10lnes/mm and gets 4 fringes after loading, then one of the gratings increases its frequency to 50lines/mm, we will get 20 fringes. 5 times the original gratings configuration

Sharpening and Multiplication

- Fringe pattern is sharpen by using complementary grating (where <u>opaque part</u> <u>and transparent spaces are not equal width</u> i.e. different intensity in interference)
- Using <u>diffraction effect</u> from the line pattern to increase resolution

In plane Moiré summary

Basically an interferometer.... Using shadow

Counting fringes: Fringes representing the difference of pair of grating lines

Calculus method: Fringe derivative is difference of two fringe orders over a specific distance

Moiré of Moiré method: Super fringe will be proportional to the fringe difference per unit shift and in the direction of the shift

Advantages: Simple concept, white light (broad band) source Disadvantages: Why anted fringes due to slight mismatch gratings

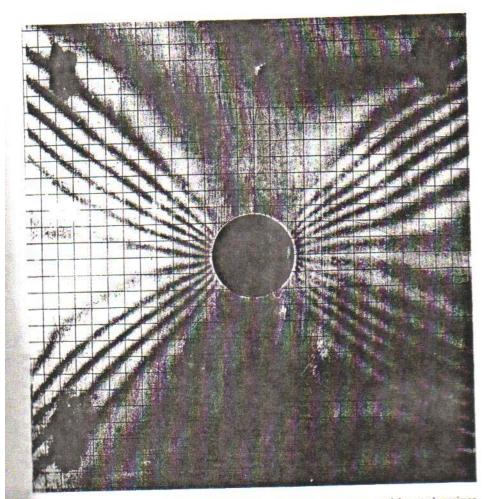
Creep Residual stress Fracture Dynamic loading Thermal deformation in electronic packaging

Direct grating deposition Laminating grating sheet on specimen



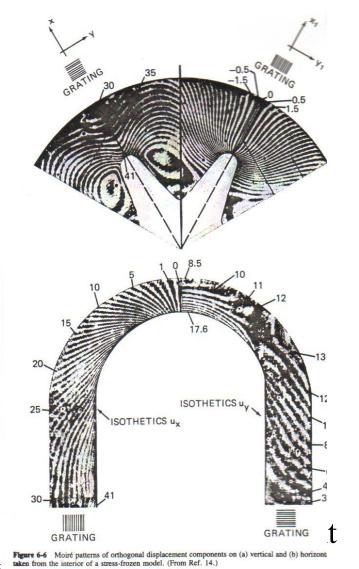
Rubber w.wang

Figure 6-4 Mismatched moiré pattern of displacement components on a rubber specimen (g = 1/312 in.).



metal

Figure 6-5 Moiré pattern multiplication of vertical displacement components on a stainless steel specimen etched with a 20-line/mm cross grating.



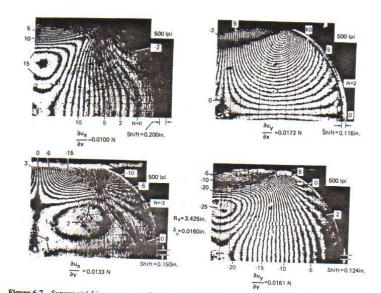


Figure 6-7 Supermoiré fringes corresponding to the four derivatives of displacements in the meridian plane at a sphere subjected to a large compression: lpi = lines/in. (From Ref. 13.)

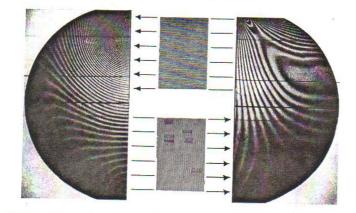
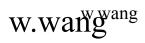


Figure 6-8 Dynamic moiré fringe patterns of vertical and horizontal displacement components on a disk shortly after an impact at the top (g = 0.025 mm). (From Ref. 23.)

Week 15

- Course Website: http://courses.washington.edu/me557/optics
- Reading Materials:
 - Week 15 reading materials are from:
- http://courses.washington.edu/me557/readings/
- Proposal due today!
- Individual meeting with me on final project tomottow afternoon.
- Continue Prims Project presentation (later after the lecture)
- Make sure you finish Lab 2 this week
- Final project presentation (6/11 afternoon).
- Final report due 6/18 5PM electronic copy must send to me not TA (abong@uw.edu)



Why Moire

- Moiré is one the most commonly used free space optical interferometric technique in mechanical measurement
- Nondestructive and noninvasive technique
- Distributive sensing (able to measure large area strain stress distribution without large number of sensors)

In plane Moiré summary

Basically an interferometer.... Using shadow (nearfield)

Counting fringes: Fringes representing the difference of pair of grating lines

Calculus method: Fringe derivative is difference of two fringe orders over a specific distance

Moiré of Moiré method: Super fringe will be proportional to the fringe difference per unit shift and in the direction of the shift

Advantages: Simple concept, white light (broad band) source Disadvantages: Unwanted fringes due to slight mismatch gratings Reqires physical grating on the specimen or sample

Creep Residual stress Fracture Dynamic loading Thermal deformation in electronic packaging

Direct grating deposition Laminating grating sheet on specimen

Out of plane Moiré



Techniques for using geometric moiré to measure out of plane displacement and slope

Shadow Moiré – utilizes superimposition of a reference grating and its own shadow. the fringes are loci of points of constant out of plane elevation, so they are essentially a contour map of the object being studied.

Method can be used to measure out-of-plane displacements or changes in displacement.

Example of applications: contour mapping of human body with objective of detecting asymmetries that indicates certain infirmities (illness).

Reflection Moiré – Superposition of shift in the reflected grating due to a bend on the specimen, thereby producing a moiré pattern.

Method for measuring <u>slope or rotation or the change of slope</u> of structural components. Approach used in study of plates in bending (direct measurement of slope)

Example of applications:

Quantify the movement of the scapular (shoulder area)

Flow field mapping

Noncontacting, remote, nontraumatic and nonstressful

Projection Moiré – Out-of-plane displacement measurement or contour mapping involves projection of reference grating on the specimen by means of a slide projector.

Application:

use of moiré fringes to acquire 3D surface shape information Topography of human scapular mechanism with muscular effort

Shadow Moiré

Geometrical moire

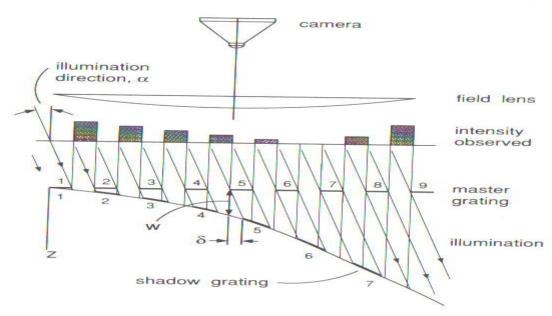


Figure 9.1. Formation of fringes in shadow moire.

- Illumination creates a shadow of grating on the surface of the specimen.
- Grating shadows are elongated on specimen by a fact depends on the inclination of the surface, and they are shifted by the amount depends on the incident angle α and distance ω from the master grating to specimen. Apparent lateral shift of a grating shadow is given by:

$$\delta = \omega \tan \alpha$$
 7

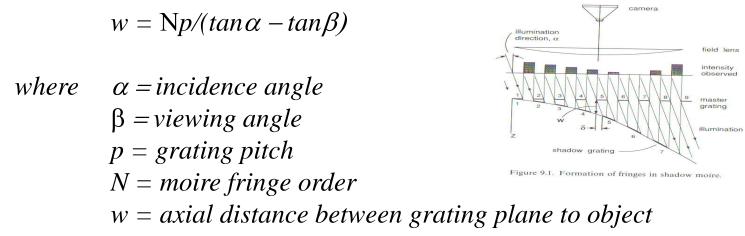
The shadow of m_{th} order lines are spread over the expanse of m+1th lines of grating, Let ω be the z distance between the master and specimen over the same expanse,

$$[(m+1)-m]p = \omega \tan \alpha \rightarrow \omega = p/\tan \alpha$$

If there are N moiré fringes between the same expanse, where fringes are observed at normal incidence,

 $w = Np/tan\alpha$

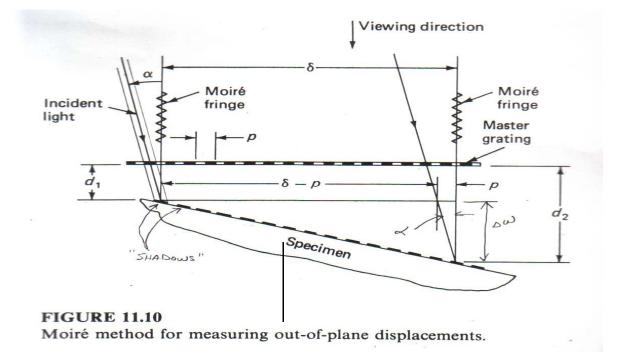
A more general form where viewing angle (β) is other than the normal,



Geometrical moire

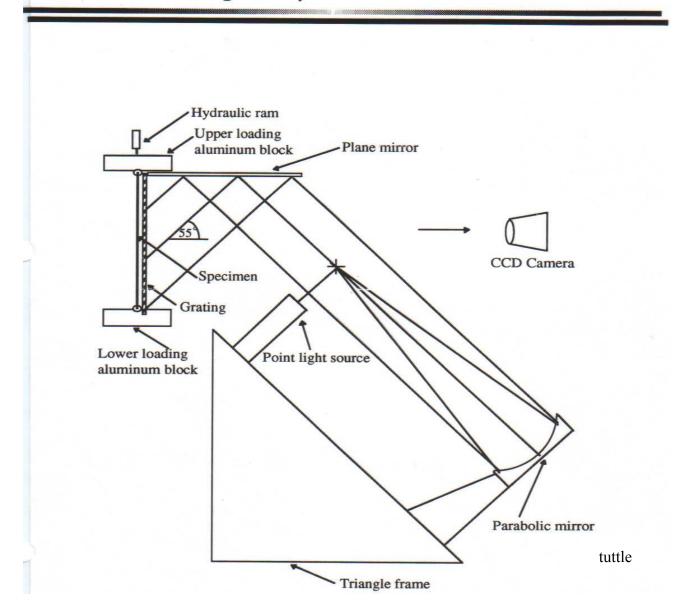
12 1010 observed Vertital at normal position (d. splant) & D= W ton d Let 5=P=> P= W tand LO S=NP=> NP= Wtond W = NP /tand if observed at \$ Sangle W = NP / (tan x - tan B)

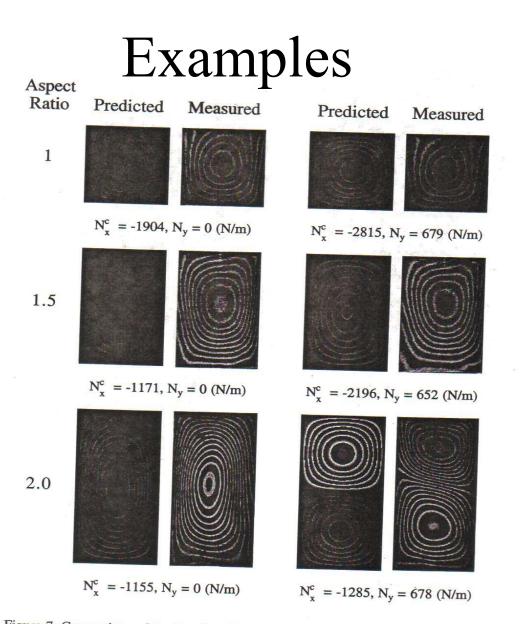
Optical Setup for Shadow Moiré



Experimental Methods

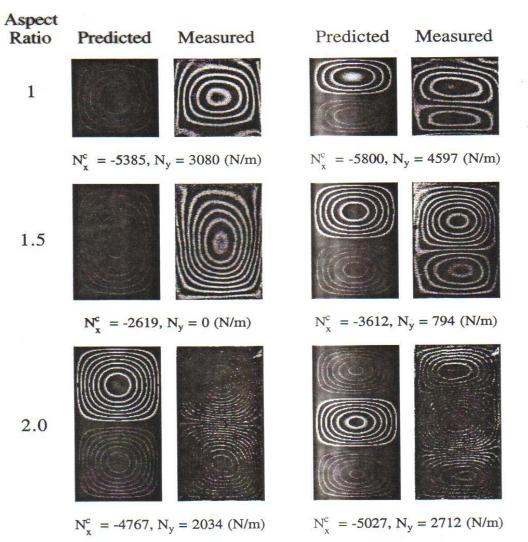
Optical Arrangment for Shadow Moire





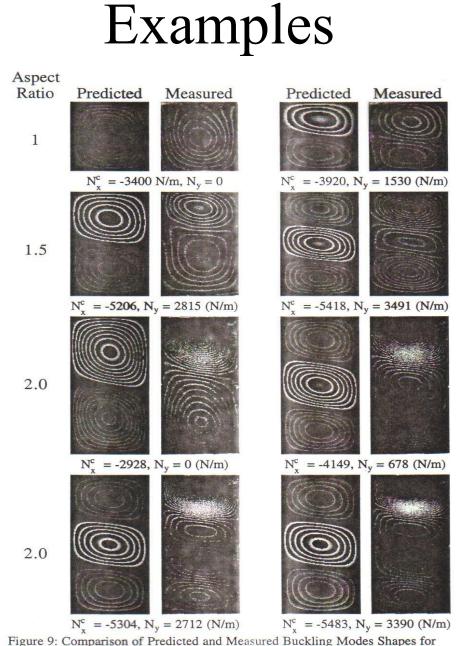


Examples



w.wang

Figure 8: Comparison of Predicted and Measured Buckling Modes Shapes for Specially-Orthotropic [0/90]_{2s} Panels



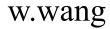
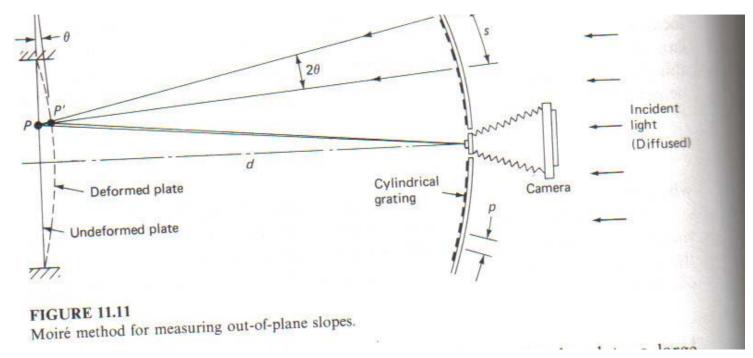


Figure 9: Comparison of Predicted and Measured Buckling Modes Shapes for Generally-Orthotropic [±45]_{2s} Panels

Reflection Moiré



- -The plate to be studied is polished on one side so as to act as a mirror.
- At some distance d from the plate a moiré master grating is erected.
- The cylinder segment with coarse grating is fabricated from a transparency sheet of plastic and the incident light passes through this shell
- The grating has a hole at its center and the camera is set up behind the aperture.
- Camera is aimed at the plate, but focused on the virtual image of the grating as it is reflected in the polished plate. Double exposure photography is used for the superposition of images W.Wang

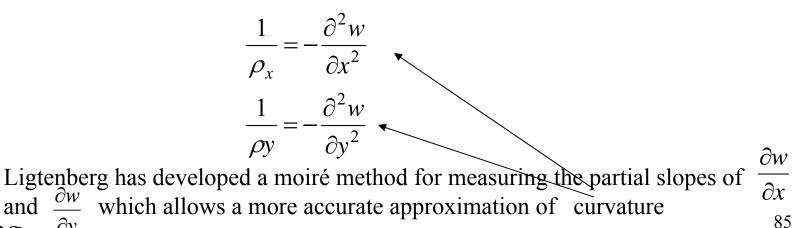
Out-of-plane slope measurement

From the theory of elasticity, it is known that stress at a point in the plate due to bending moments can be expressed in terms of local curvature of plate as

$$\sigma_x = \frac{E_z}{1 - v^2} \left(\frac{1}{\rho_x} + v \frac{1}{\rho_y}\right)$$
$$\sigma_y = \frac{E_z}{1 - v^2} \left(\frac{1}{\rho_y} + v \frac{1}{\rho_x}\right)$$

Where $1/\rho_x$ and $1/\rho_y$ are curvatures with respect to x and y axes

The deflections are related to the curvatures by,



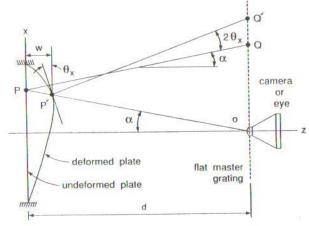
which allows a f w.wang $\frac{\partial y}{\partial y}$

Moiré Method measuring out-of-plane slopes

- 1. First exposure is made with specimen at its initial state which taken at unloaded position. Grating Q is reflected from point P
- 2. Plate is then deformed, now point P on plate has moved to point P', which approximately the same location on the film as point P.Because of the curvature, grating element Q' is now superimposed on this image point in the second exposure.
- The moiré pattern formed by superposition of the two images provide a measure of the shift. The shift in terms of local slope of the plate is given as,

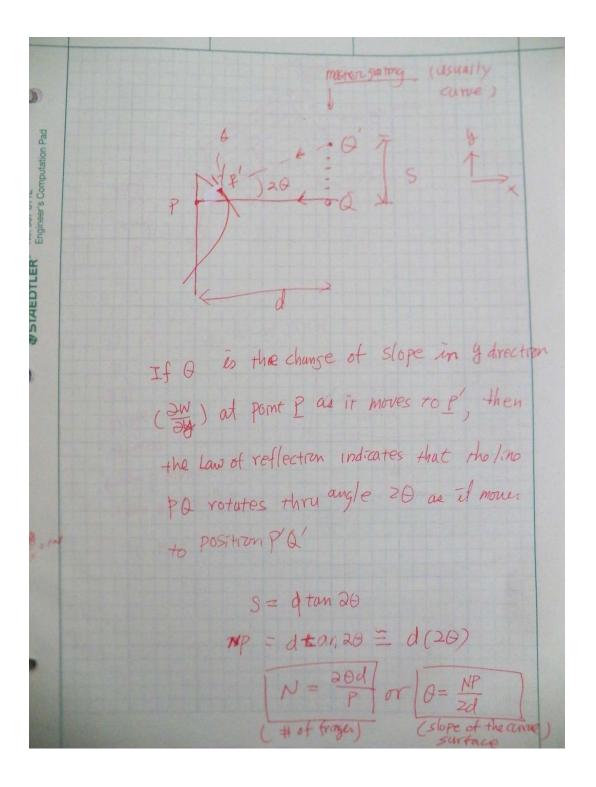
 $s = 2\theta d$ Where s = magnitude of shift θ = local slope of plate at P' d= distance between plate and grating The order of moiré fringe can be expressed as

 $N = 2\theta d/\rho$ or $\theta = Np/2d$

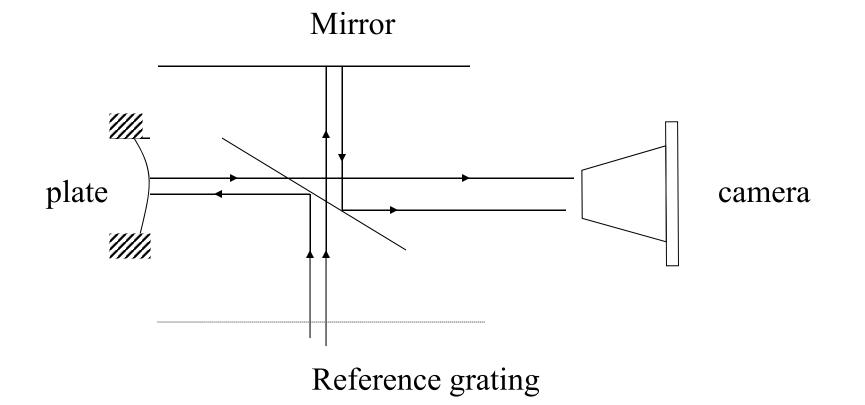


d should be large to minimize the effects of out-of-plane displacement W on the shift distance s

Reflectron use double exposurer 9 20 d tan 20= 5 they shif np 0 = Like $\pi p = d \tan 2\theta$ $= d^{2}\theta$ Real time reflection eliminates the need for double exposure



Real –time reflection moiré analysis of slope



Double exposure moiré tends to be marginal.

Avoid viewing the plate through gratings.

Allows for angular adjustments (without having to use curve gratings)

Examples

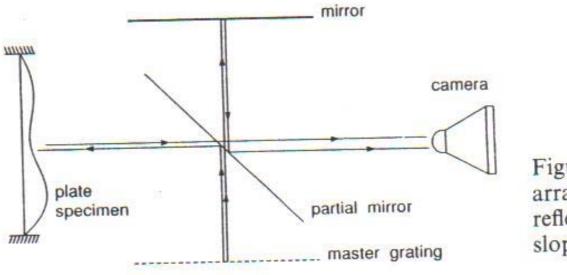
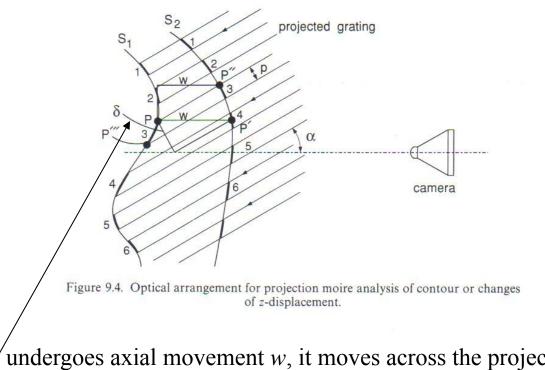


Figure 9.3. Optical arrangement for real-time reflection moire analysis of slope.

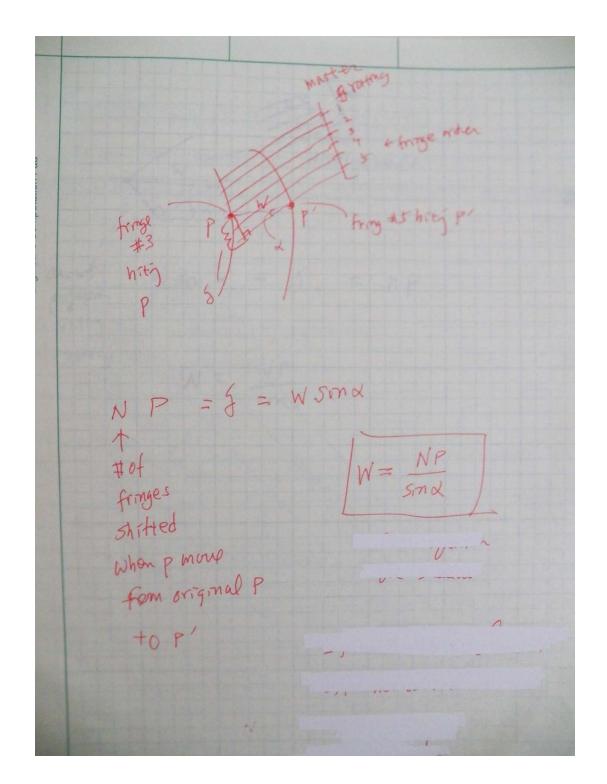
Projection Moiré



Similar to Projecting interference Pattern in Moiré interferometer

P undergoes axial movement w, it moves across the projected grating by the amount $\delta = w \sin \alpha$, where α is incident angle of the projected grating, The fringe order at point P in final moiré will be N= δ/p , where p is grating pitch The axial displacement w is therefore,

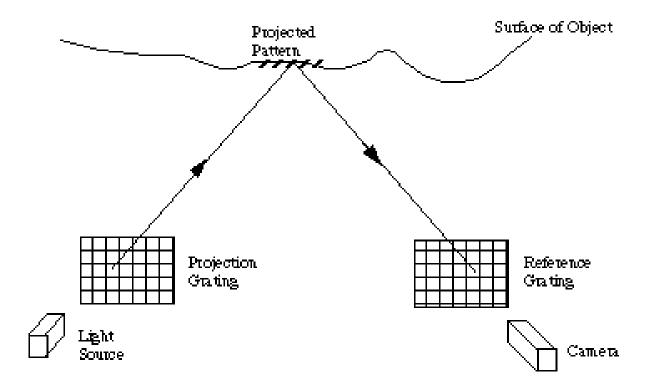
$$w = \frac{Np}{\sin \alpha}$$



~ axial d splacement W d 9 WSINX = 5 = MP amoud projectra query moved NP W= sind X

93

Projection Technique



The essence of the method is that a grating is projected onto an object and an image is formed in the plane of some reference grating.

Project Moiré

$$w_d = w_o + \frac{Np}{\sin\alpha} \left[\left(1 - \frac{2w}{s} \cos\alpha - \frac{Np}{s\tan\alpha}\right) - \frac{x}{s\sin\alpha} \left(\frac{s}{d} \cos\alpha - \cos 2a\right) \right]$$

Where N =fringe number

P= grating pitch

s= distance from projector to subject reference plane d=distance from camera to subject reference plane x=x coorinate of point P observed by camera plnes α = angle between camera and projector optical axis Xa = x coordinate of point P' X_{a0} is x coordinate of point P X = Xa N=number of line in cone OSP

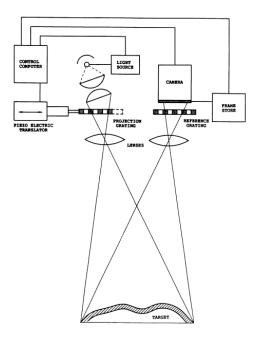
Projection Technique



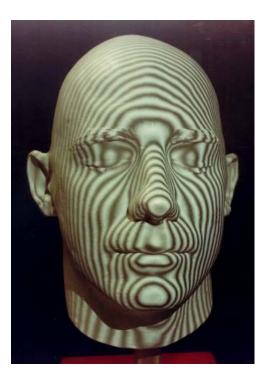
The image then interferes with the reference grating to form Moiré fringe contour patterns which appear as dark and light stripes. Analysis of the patterns then gives accurate descriptions of changes in depth and hence shape.

Moiré Fringe Contouring

The use of moiré fringes to acquire 3D surface shape information is well established. Their application to the measurement of areas of the human body began with the work of Hiroshi Takasaki as early as 1973



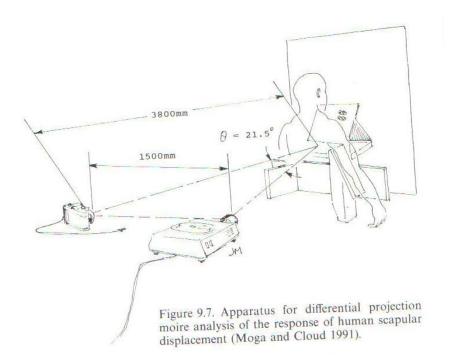
Schematic Diagram of Auto-MATE System



University of Glasgow

Moiré Fringes Superimposed on Model Head

Example



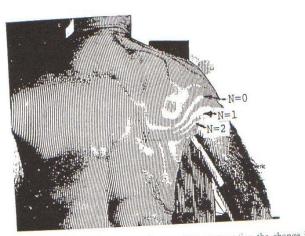


Figure 9.8. Differential projection moire fringe pattern representing the change in topography of the human scapular mechanism with muscular effort; result for 20% adduction of upper arm (Moga and Cloud 1991).