

1.6.18

(a) The graph satisfies the horizontal line test, so it is 1-to-1.
(or the function is always increasing is another good reason.)

(b) Domain of f is $(-3, 3)$
Range of f is $(-1, 3)$ } So Domain of f^{-1} is $(-1, 3)$
Range of f^{-1} is $(-3, 3)$

(c) $f^{-1}(2) \approx 0$

(d) $f^{-1}(0) \approx -1.7$

1.6.25 Find the inverse

$y = \ln(x+3)$ (solve for x).

$e^y = x+3$

$e^y - 3 = x$

So the inverse of $\ln(x+3)$

is the function $e^x - 3$

1.6.26 Find inverse

$y = \frac{e^x}{1+2e^x}$

$y(1+2e^x) = e^x$

$y + 2ye^x = e^x$

$y = e^x - 2ye^x$

$y = e^x(1-2y)$

$\frac{y}{1-2y} = e^x$

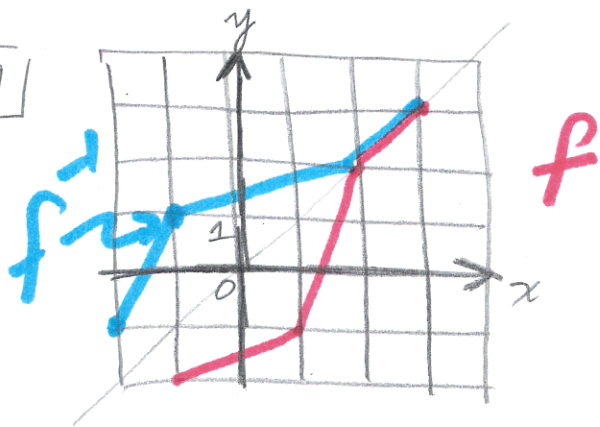
$\ln\left(\frac{y}{1-2y}\right) = x$

$\ln(y) - \ln(1-2y) = x$

So the inverse of $\frac{e^x}{1+2e^x}$ is the

function $\ln x - \ln(1-2x)$

1.6.29



1.6.35 Exact value of

$$(a) \log_2 6 - \log_2 15 + \log_2 20 = \log_2 \left(\frac{6 \cdot 20}{15} \right) = \log_2 (8) = 3$$

$$(b) \log_3 100 - \log_3 18 - \log_3 50 = \log_3 \left(\frac{100}{18 \cdot 50} \right) = \log_3 \left(\frac{1}{9} \right) = -2$$

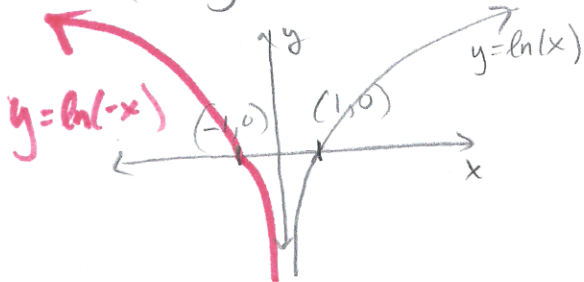
1.6.36 Exact value of

$$(a) e^{-2 \ln 5} = e^{\ln 5^{-2}} = 5^{-2} = \frac{1}{25}$$

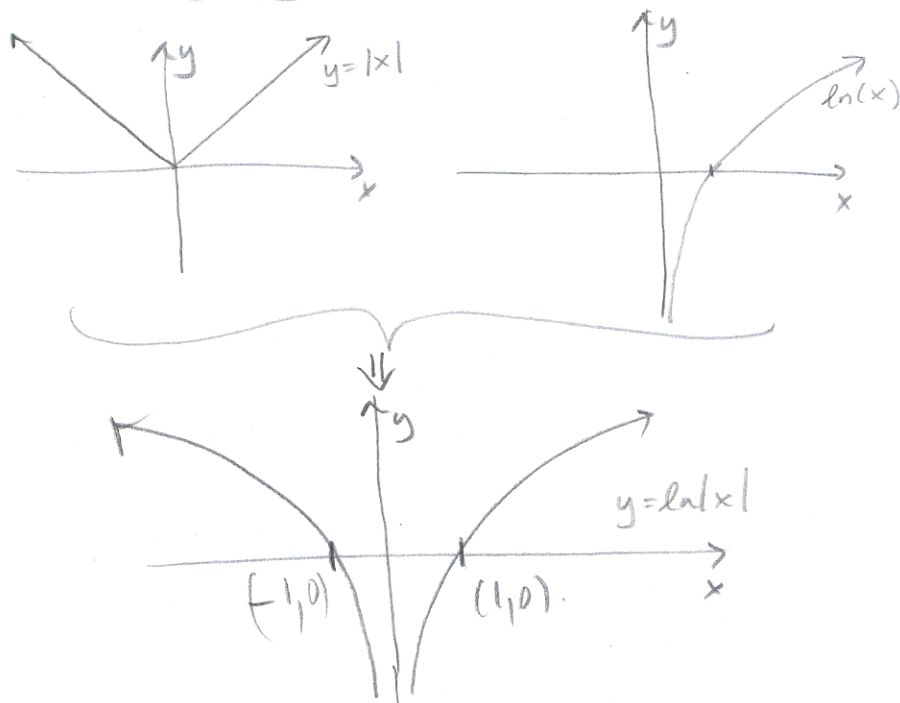
$$(b) \ln(\ln e^{e^{10}}) = \ln(e^{10}) = 10$$

1.6.46 Rough sketch

(a) $y = \ln(-x)$



(b) $y = \ln|x|$



1.6.49 Solve for x.

$$(a) 2^{x-5} = 3$$

$$\ln 2^{x-5} = \ln 3$$

$$(x-5) \ln 2 = \ln 3$$

$$x-5 = \frac{\ln 3}{\ln 2}$$

$$x = 5 + \frac{\ln 3}{\ln 2}$$

$$(b) \ln x + \ln(x-1) = 1$$

$$\ln(x(x-1)) = 1$$

$$x(x-1) = e^1$$

$$x^2 - x - e = 0$$

$$x = \frac{1 \pm \sqrt{1+4e}}{2}$$

1.6.50 Solve for x.

$$(a) \ln(\ln x) = 1$$

$$\ln x = e$$

$$x = e^e$$

$$(b) e^{ax} = C e^{bx} \quad a \neq b$$

$$\ln(e^{ax}) = \ln(C e^{bx})$$

$$ax = \ln C + \ln e^{bx}$$

$$ax = \ln C + bx$$

$$ax - bx = \ln C$$

$$(a-b)x = \ln C$$

$$x = \frac{\ln C}{a-b}$$