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## Section 3.3 (Part A)

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1.  $f(x) = 3x^2 - 2 \cos x \Rightarrow f'(x) = 6x - 2(-\sin x) = 6x + 2 \sin x$

2.  $f(x) = \sqrt{x} \sin x \Rightarrow f'(x) = \sqrt{x} \cos x + \sin x \left(\frac{1}{2}x^{-1/2}\right) = \sqrt{x} \cos x + \frac{\sin x}{2\sqrt{x}}$

5.  $g(t) = t^3 \cos t \Rightarrow g'(t) = t^3(-\sin t) + (\cos t) \cdot 3t^2 = 3t^2 \cos t - t^3 \sin t$  or  $t^2(3 \cos t - t \sin t)$

8.  $y = e^u(\cos u + cu) \Rightarrow y' = e^u(-\sin u + c) + (\cos u + cu)e^u = e^u(\cos u - \sin u + cu + c)$

10.  $y = \frac{1 + \sin x}{x + \cos x} \Rightarrow$

$$y' = \frac{(x + \cos x)(\cos x) - (1 + \sin x)(1 - \sin x)}{(x + \cos x)^2} = \frac{x \cos x + \cos^2 x - (1 - \sin^2 x)}{(x + \cos x)^2}$$
$$= \frac{x \cos x + \cos^2 x - (\cos^2 x)}{(x + \cos x)^2} = \frac{x \cos x}{(x + \cos x)^2}$$

13.  $y = \frac{\sin x}{x^2} \Rightarrow y' = \frac{x^2 \cos x - (\sin x)(2x)}{(x^2)^2} = \frac{x(x \cos x - 2 \sin x)}{x^4} = \frac{x \cos x - 2 \sin x}{x^3}$

22.  $y = e^x \cos x \Rightarrow y' = e^x(-\sin x) + (\cos x)e^x = e^x(\cos x - \sin x) \Rightarrow$  the slope of the tangent line at  $(0, 1)$  is  $e^0(\cos 0 - \sin 0) = 1(1 - 0) = 1$  and an equation is  $y - 1 = 1(x - 0)$  or  $y = x + 1$ .

33.  $f(x) = x + 2 \sin x$  has a horizontal tangent when  $f'(x) = 0 \Leftrightarrow 1 + 2 \cos x = 0 \Leftrightarrow \cos x = -\frac{1}{2} \Leftrightarrow$

$x = \frac{2\pi}{3} + 2\pi n$  or  $\frac{4\pi}{3} + 2\pi n$ , where  $n$  is an integer. Note that  $\frac{4\pi}{3}$  and  $\frac{2\pi}{3}$  are  $\pm \frac{\pi}{3}$  units from  $\pi$ . This allows us to write the solutions in the more compact equivalent form  $(2n + 1)\pi \pm \frac{\pi}{3}$ ,  $n$  an integer.