

$$1. \int_0^5 \frac{x}{x+10} dx = \int_0^5 \left(1 - \frac{10}{x+10}\right) dx = [x - 10 \ln(x+10)]_0^5 = 5 - 10 \ln 15 + 10 \ln 10$$

$$= 5 + 10 \ln \frac{10}{15} = 5 + 10 \ln \frac{2}{3}$$

$$2. \int_0^5 ye^{-0.6y} dy \quad \left[\begin{array}{l} u = y, \quad dv = e^{-0.6y} dy, \\ du = dy \quad v = -\frac{5}{3} e^{-0.6y} \end{array} \right] = \left[-\frac{5}{3} ye^{-0.6y}\right]_0^5 - \int_0^5 \left(-\frac{5}{3} e^{-0.6y}\right) dy = -\frac{25}{3} e^{-3} - \frac{25}{9} [e^{-0.6y}]_0^5$$

$$= -\frac{25}{3} e^{-3} - \frac{25}{9} (e^{-3} - 1) = -\frac{25}{3} e^{-3} - \frac{25}{9} e^{-3} + \frac{25}{9} = \frac{25}{9} - \frac{100}{9} e^{-3}$$

$$3. \int_0^{\pi/2} \frac{\cos \theta}{1 + \sin \theta} d\theta = [\ln(1 + \sin \theta)]_0^{\pi/2} = \ln 2 - \ln 1 = \ln 2$$

$$4. \int_1^4 \frac{dt}{(2t+1)^3} \quad \left[\begin{array}{l} u = 2t+1, \\ du = 2 dt \end{array} \right] = \int_3^9 \frac{\frac{1}{2} du}{u^3} = \frac{-1}{4} \left[\frac{1}{u^2} \right]_3^9 = -\frac{1}{4} \left(\frac{1}{81} - \frac{1}{9} \right) = -\frac{1}{4} \left(-\frac{8}{81} \right) = \frac{2}{81}$$

$$5. \int_0^{\pi/2} \sin^3 \theta \cos^2 \theta d\theta = \int_0^{\pi/2} (1 - \cos^2 \theta) \cos^2 \theta \sin \theta d\theta = \int_1^0 (1 - u^2) u^2 (-du) \quad \left[\begin{array}{l} u = \cos \theta, \\ du = -\sin \theta d\theta \end{array} \right]$$

$$= \int_0^1 (u^2 - u^4) du = \left[\frac{1}{3} u^3 - \frac{1}{5} u^5 \right]_0^1 = \left(\frac{1}{3} - \frac{1}{5} \right) - 0 = \frac{2}{15}$$

$$6. \frac{1}{y^2 - 4y - 12} = \frac{1}{(y-6)(y+2)} = \frac{A}{y-6} + \frac{B}{y+2} \Rightarrow 1 = A(y+2) + B(y-6). \text{ Letting } y = -2 \Rightarrow B = -\frac{1}{8} \text{ and}$$

$$\text{letting } y = 6 \Rightarrow A = \frac{1}{8}. \text{ So } \int \frac{1}{y^2 - 4y - 12} dy = \int \left(\frac{1/8}{y-6} + \frac{-1/8}{y+2} \right) dy = \frac{1}{8} \ln |y-6| - \frac{1}{8} \ln |y+2| + C.$$

$$7. \text{ Let } u = \ln t, \quad du = dt/t. \text{ Then } \int \frac{\sin(\ln t)}{t} dt = \int \sin u \, du = -\cos u + C = -\cos(\ln t) + C.$$

$$8. \text{ Let } u = \sqrt{e^x - 1}, \text{ so that } u^2 = e^x - 1, \quad 2u \, du = e^x \, dx, \text{ and } e^x = u^2 + 1. \text{ Then}$$

$$\int \frac{1}{\sqrt{e^x - 1}} dx = \int \frac{1}{u} \frac{2u \, du}{u^2 + 1} = 2 \int \frac{1}{u^2 + 1} du = 2 \tan^{-1} u + C = 2 \tan^{-1} \sqrt{e^x - 1} + C.$$

$$9. \int_1^4 x^{3/2} \ln x \, dx \quad \left[\begin{array}{l} u = \ln x, \quad dv = x^{3/2} dx, \\ du = dx/x \quad v = \frac{2}{5} x^{5/2} \end{array} \right] = \frac{2}{5} [x^{5/2} \ln x]_1^4 - \frac{2}{5} \int_1^4 x^{3/2} dx = \frac{2}{5} (32 \ln 4 - \ln 1) - \frac{2}{5} \left[\frac{2}{5} x^{5/2} \right]_1^4$$

$$= \frac{2}{5} (64 \ln 2) - \frac{4}{25} (32 - 1) = \frac{128}{5} \ln 2 - \frac{124}{25} \quad \left[\text{or } \frac{64}{5} \ln 4 - \frac{124}{25} \right]$$

$$10. \text{ Let } u = \arctan x, \quad du = dx/(1+x^2). \text{ Then}$$

$$\int_0^1 \frac{\sqrt{\arctan x}}{1+x^2} dx = \int_0^{\pi/4} \sqrt{u} \, du = \frac{2}{3} [u^{3/2}]_0^{\pi/4} = \frac{2}{3} \left[\frac{\pi^{3/2}}{4^{3/2}} - 0 \right] = \frac{2}{3} \cdot \frac{1}{8} \pi^{3/2} = \frac{1}{12} \pi^{3/2}.$$