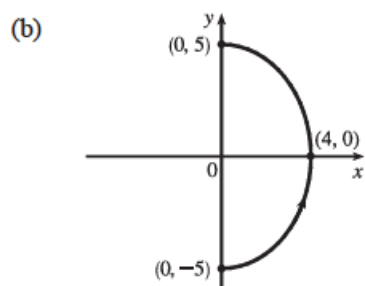


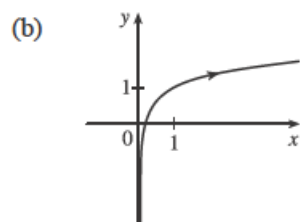
12. (a)  $x = 4 \cos \theta, y = 5 \sin \theta, -\pi/2 \leq \theta \leq \pi/2$ .

$(\frac{x}{4})^2 + (\frac{y}{5})^2 = \cos^2 \theta + \sin^2 \theta = 1$ , which is an ellipse with  $x$ -intercepts  $(\pm 4, 0)$  and  $y$ -intercepts  $(0, \pm 5)$ . We obtain the portion of the ellipse with  $x \geq 0$  since  $4 \cos \theta \geq 0$  for  $-\pi/2 \leq \theta \leq \pi/2$ .



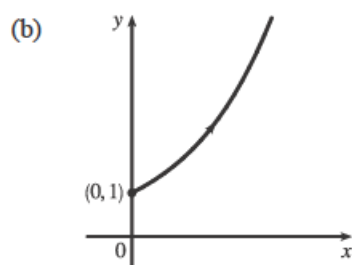
15. (a)  $x = e^{2t} \Rightarrow 2t = \ln x \Rightarrow t = \frac{1}{2} \ln x$ .

$$y = t + 1 = \frac{1}{2} \ln x + 1.$$

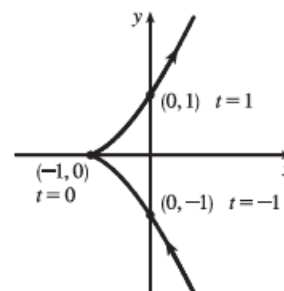


16. (a)  $x = \ln t, y = \sqrt{t}, t \geq 1$ .

$$x = \ln t \Rightarrow t = e^x \Rightarrow y = \sqrt{t} = e^{x/2}, x \geq 0.$$



25. When  $t = -1, (x, y) = (0, -1)$ . As  $t$  increases to 0,  $x$  decreases to  $-1$  and  $y$  increases to 0. As  $t$  increases from 0 to 1,  $x$  increases to 0 and  $y$  increases to 1. As  $t$  increases beyond 1, both  $x$  and  $y$  increase. For  $t < -1$ ,  $x$  is positive and decreasing and  $y$  is negative and increasing. We could achieve greater accuracy by estimating  $x$ - and  $y$ -values for selected values of  $t$  from the given graphs and plotting the corresponding points.



28. (a)  $x = t^4 - t + 1 = (t^4 + 1) - t > 0$  [think of the graphs of  $y = t^4 + 1$  and  $y = t$ ] and  $y = t^2 \geq 0$ , so these equations are matched with graph V.

(b)  $y = \sqrt{t} \geq 0$ .  $x = t^2 - 2t = t(t - 2)$  is negative for  $0 < t < 2$ , so these equations are matched with graph I.

(c)  $x = \sin 2t$  has period  $2\pi/2 = \pi$ . Note that

$$y(t + 2\pi) = \sin[t + 2\pi + \sin 2(t + 2\pi)] = \sin(t + 2\pi + \sin 2t) = \sin(t + \sin 2t) = y(t), \text{ so } y \text{ has period } 2\pi.$$

These equations match graph II since  $x$  cycles through the values  $-1$  to  $1$  twice as  $y$  cycles through those values once.

(d)  $x = \cos 5t$  has period  $2\pi/5$  and  $y = \sin 2t$  has period  $\pi$ , so  $x$  will take on the values  $-1$  to  $1$ , and then  $1$  to  $-1$ , before  $y$  takes on the values  $-1$  to  $1$ . Note that when  $t = 0$ ,  $(x, y) = (1, 0)$ . These equations are matched with graph VI.

(e)  $x = t + \sin 4t$ ,  $y = t^2 + \cos 3t$ . As  $t$  becomes large,  $t$  and  $t^2$  become the dominant terms in the expressions for  $x$  and  $y$ , so the graph will look like the graph of  $y = x^2$ , but with oscillations. These equations are matched with graph IV.

(f)  $x = \frac{\sin 2t}{4 + t^2}$ ,  $y = \frac{\cos 2t}{4 + t^2}$ . As  $t \rightarrow \infty$ ,  $x$  and  $y$  both approach  $0$ . These equations are matched with graph III.