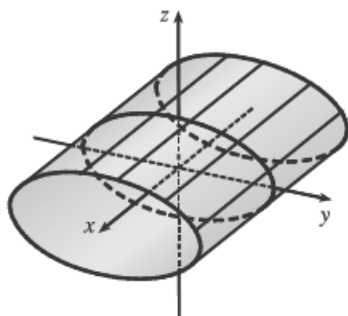
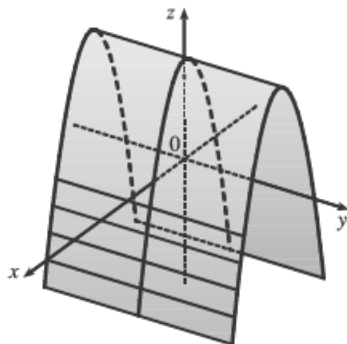


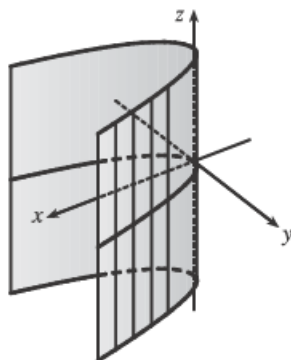
3. Since x is missing from the equation, the vertical traces $y^2 + 4z^2 = 4, x = k$, are copies of the same ellipse in the plane $x = k$. Thus, the surface $y^2 + 4z^2 = 4$ is an elliptic cylinder with rulings parallel to the x -axis.



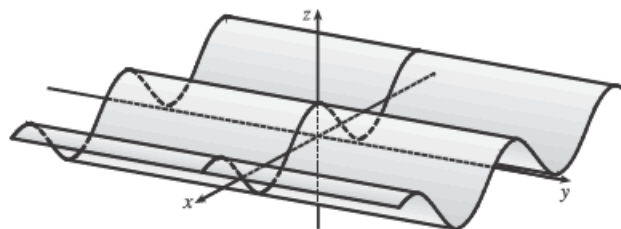
4. Since y is missing from the equation, each vertical trace $z = 4 - x^2, y = k$, is a copy of the same parabola in the plane $y = k$. Thus, the surface $z = 4 - x^2$ is a parabolic cylinder with rulings parallel to the y -axis.



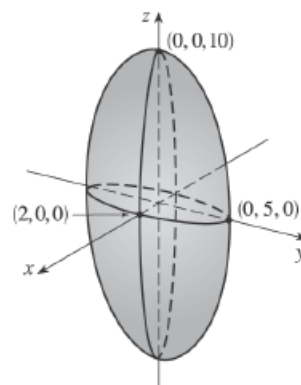
5. Since z is missing, each horizontal trace $x = y^2, z = k$, is a copy of the same parabola in the plane $z = k$. Thus, the surface $x - y^2 = 0$ is a parabolic cylinder with rulings parallel to the z -axis.



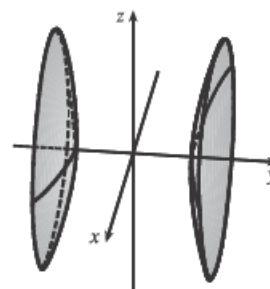
7. Since y is missing, each vertical trace $z = \cos x, y = k$ is a copy of a cosine curve in the plane $y = k$. Thus, the surface $z = \cos x$ is a cylindrical surface with rulings parallel to the y -axis.



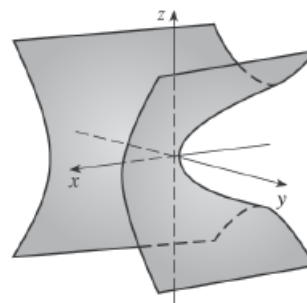
14. $25x^2 + 4y^2 + z^2 = 100$. The traces in $x = k$ are $4y^2 + z^2 = 100 - 25k^2$, a family of ellipses for $|k| < 2$. (The traces are a single point for $|k| = 2$ and are empty for $|k| > 2$.) Similarly, the traces in $y = k$ are the ellipses $25x^2 + z^2 = 100 - 4k^2, |k| < 5$, and the traces in $z = k$ are the ellipses $25x^2 + 4y^2 = 100 - k^2, |k| < 10$. The graph is an ellipsoid centered at the origin with intercepts $x = \pm 2, y = \pm 5, z = \pm 10$.



15. $-x^2 + 4y^2 - z^2 = 4$. The traces in $x = k$ are the hyperbolas $4y^2 - z^2 = 4 + k^2$. The traces in $y = k$ are $x^2 + z^2 = 4k^2 - 4$, a family of circles for $|k| > 1$, and the traces in $z = k$ are $4y^2 - x^2 = 4 + k^2$, a family of hyperbolas. Thus the surface is a hyperboloid of two sheets with axis the y -axis.

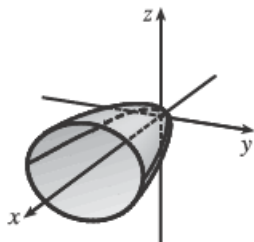


20. $x = y^2 - z^2$. The traces in $x = k$ are $y^2 - z^2 = k$, two intersecting lines when $k = 0$ and a family of hyperbolas for $k \neq 0$ (oriented differently for $k > 0$ than for $k < 0$). The traces in $y = k$ are the parabolas $x = -z^2 + k^2$, opening in the negative x -direction, and the traces in $z = k$ are the parabolas $x = y^2 - k^2$ which open in the positive x -direction. The graph is a hyperbolic paraboloid with saddle point $(0, 0, 0)$.



21. This is the equation of an ellipsoid: $x^2 + 4y^2 + 9z^2 = x^2 + \frac{y^2}{(1/2)^2} + \frac{z^2}{(1/3)^2} = 1$, with x -intercepts ± 1 , y -intercepts $\pm \frac{1}{2}$ and z -intercepts $\pm \frac{1}{3}$. So the major axis is the x -axis and the only possible graph is VII.

22. This is the equation of an ellipsoid: $9x^2 + 4y^2 + z^2 = \frac{x^2}{(1/3)^2} + \frac{y^2}{(1/2)^2} + z^2 = 1$, with x -intercepts $\pm\frac{1}{3}$, y -intercepts $\pm\frac{1}{2}$ and z -intercepts ± 1 . So the major axis is the z -axis and the only possible graph is IV.
23. This is the equation of a hyperboloid of one sheet, with $a = b = c = 1$. Since the coefficient of y^2 is negative, the axis of the hyperboloid is the y -axis, hence the correct graph is II.
24. This is a hyperboloid of two sheets, with $a = b = c = 1$. This surface does not intersect the xz -plane at all, so the axis of the hyperboloid is the y -axis and the graph is III.
25. There are no real values of x and z that satisfy this equation for $y < 0$, so this surface does not extend to the left of the xz -plane. The surface intersects the plane $y = k > 0$ in an ellipse. Notice that y occurs to the first power whereas x and z occur to the second power. So the surface is an elliptic paraboloid with axis the y -axis. Its graph is VI.
26. This is the equation of a cone with axis the y -axis, so the graph is I.
27. This surface is a cylinder because the variable y is missing from the equation. The intersection of the surface and the xz -plane is an ellipse. So the graph is VIII.
28. This is the equation of a hyperbolic paraboloid. The trace in the xy -plane is the parabola $y = x^2$. So the correct graph is V.
31. $x = 2y^2 + 3z^2$ or $x = \frac{y^2}{1/2} + \frac{z^2}{1/3}$ or $\frac{x}{6} = \frac{y^2}{3} + \frac{z^2}{2}$
represents an elliptic paraboloid with vertex $(0, 0, 0)$ and axis the x -axis.



35. Completing squares in all three variables gives

$$(x - 2)^2 - (y + 1)^2 + (z - 1)^2 = 0 \text{ or}$$

$(y + 1)^2 = (x - 2)^2 + (z - 1)^2$, a circular cone with
center $(2, -1, 1)$ and axis the horizontal line $x = 2$,
 $z = 1$.

