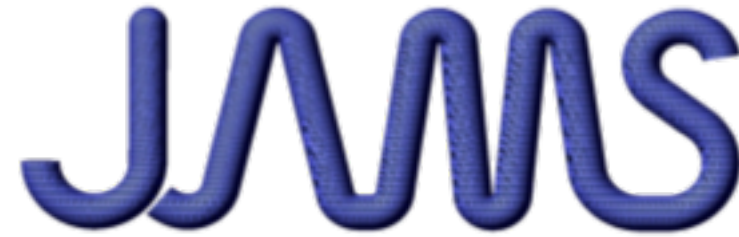




CMH-17
COMPOSITE MATERIALS HANDBOOK



JOINT ADVANCED MATERIALS & STRUCTURES
CENTER OF EXCELLENCE

Analytical Fatigue Life Determination based on Residual Strength Degradation of Composites

Damage Tolerance Testing and Analysis Protocols for Full-Scale Composite Airframe
Structures under Repeated Loading

2018 Technical Review

Waruna Seneviratne, John Tomblin, and Supun Kariyawasam



WICHITA STATE
UNIVERSITY

NATIONAL INSTITUTE
FOR AVIATION RESEARCH



Research Team

WSU/NIAR

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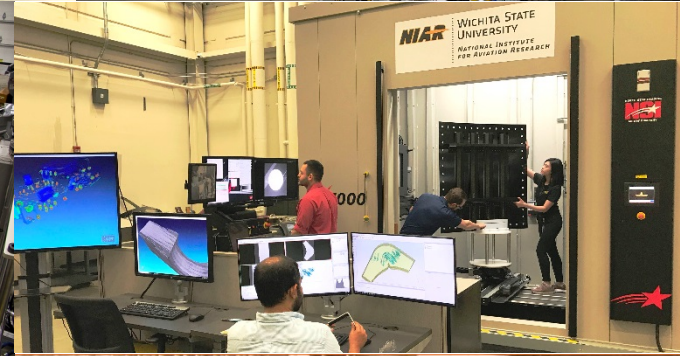
PI: John Tomblin, PhD
Supun Kariyawasam



FAA

Larry Ilcewicz, PhD
(FAA Chief Scientist - Composites)

Lynn Pham
(FAA Technical Monitor)



AFRL

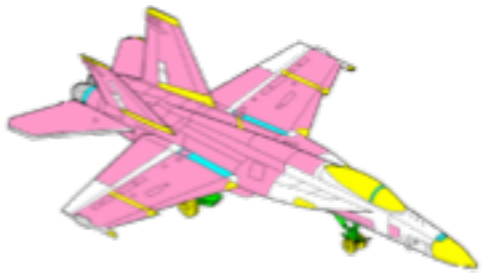
David Mollenhauer, PhD
Kara Storage
Tara Storage





Variable Amplitude Fatigue Damage Growth (Background)

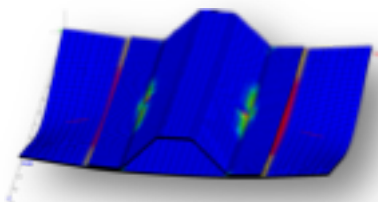
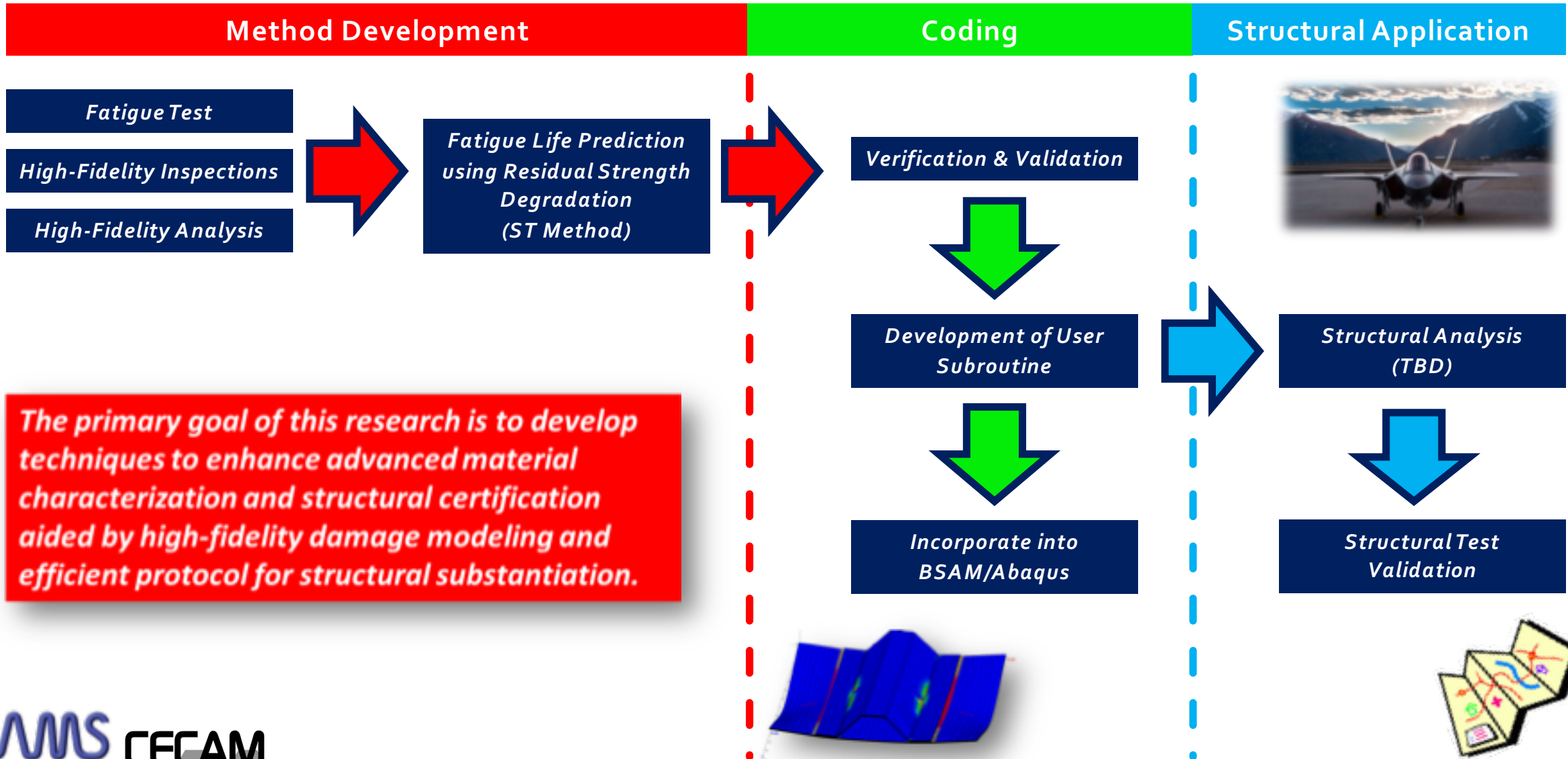
- Due to the anisotropy and heterogeneous nature of composites, **fatigue damage growth characteristics of composites are complex and predictive methodologies are at their infant stages.**
- Therefore, **overly conservative assumptions** are made for fatigue life assessment without taking full advantage of fatigue capabilities of composites.
- In order to design efficient composite structures, a **greater understanding of fundamentals of fatigue damage initiation and growth characteristics** of composite is needed.
- Need to understand the **interaction of high-cycle (low stress) and low-cycle (high stress) fatigue** on the life assessment of composite.



*The primary goal of this research is to investigate the fatigue damage growth of composites under variable amplitude fatigue loading.
The secondary goal of the program is to develop tools for determining the residual strength degradation or wearout.*



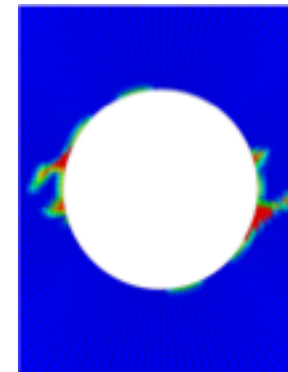
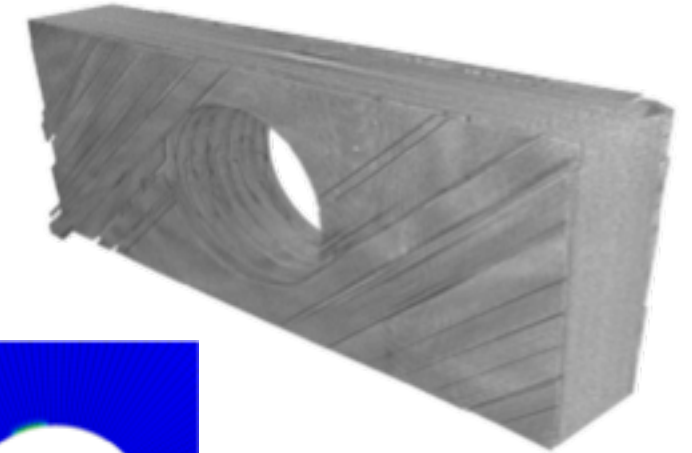
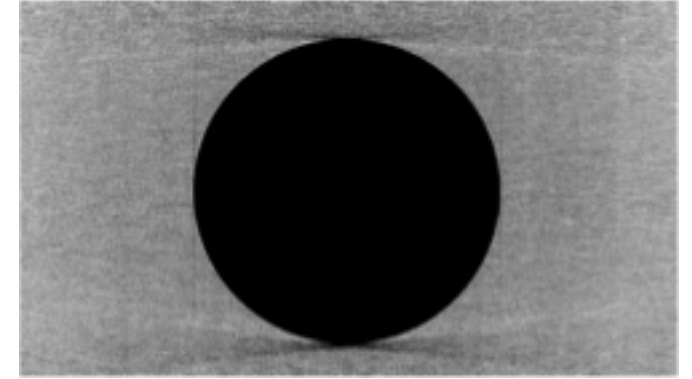
Building-Block Validation Road Map





Overview of the Presentation

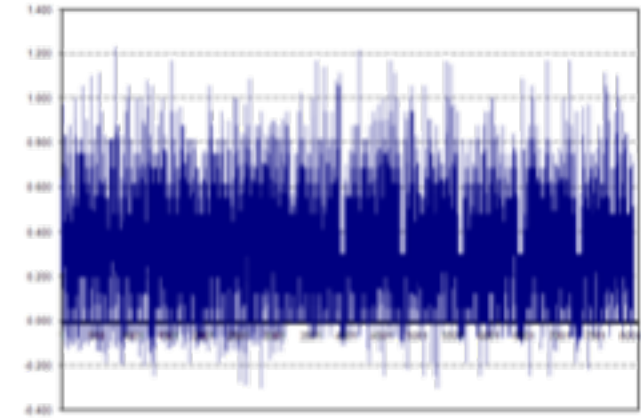
- Development of Strength Tracking (ST) Methodology
 - Variable Amplitude Fatigue Analysis
 - Validation
- High-Fidelity Inspections for Damage Characterization
 - X-Ray Computed Tomography (XCT)
 - High-fidelity inspection database
- High-Fidelity Finite Element Analysis
 - Regularized Extended Finite Element Analysis (Rx-FEM)
 - Validation with XCT and test results





Development of Strength Tracking (ST) Methodology

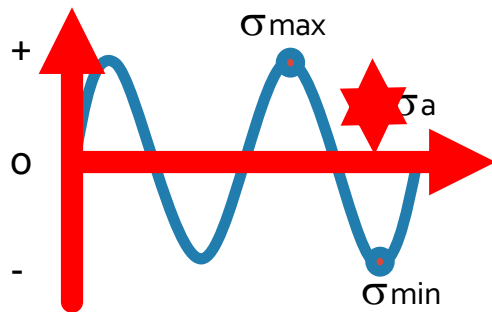
Variable Amplitude Fatigue Testing & Analysis





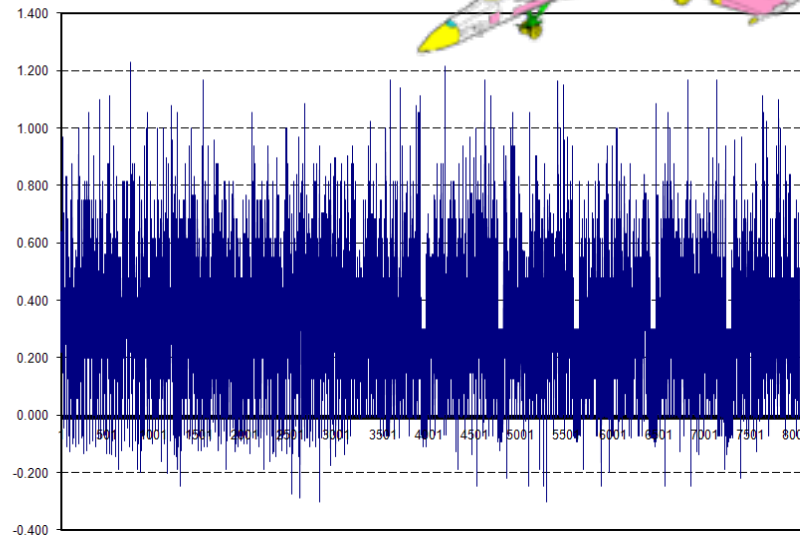
Constant Amplitude vs. Variable Amplitude (Spectrum)

Constant amplitude:



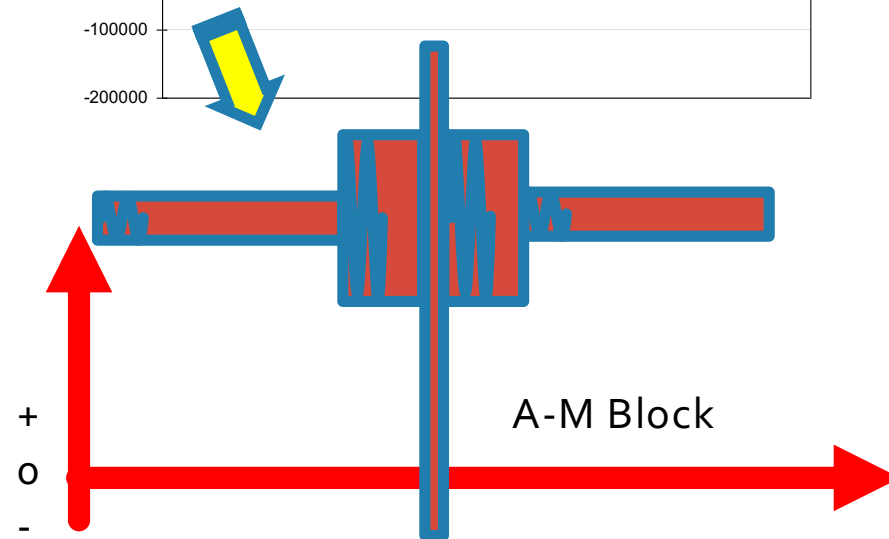
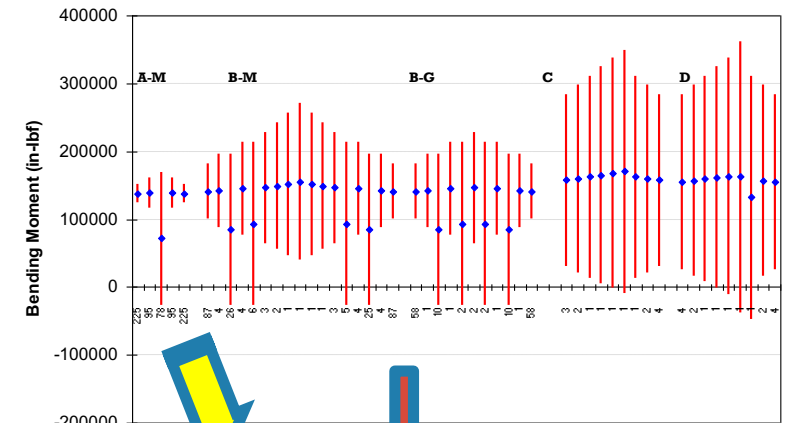
$$A = (\sigma_{\max} + \sigma_{\min})/2$$

Random Spectrum:



REF: Seneviratne, W., *et al.*, "Durability and Residual Strength Assessment of F/A-18 A-D Wing-Root Stepped-Lap Joint," 11th AIAA Aviation Technology, Integration, and Operations (ATIO) Conference and the Centennial of Naval Aviation Forum, September 2011.

Block Spectrum:

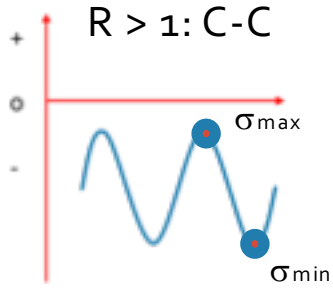


REF: Seneviratne, W. P., "Fatigue Life Determination of a Damage-Tolerant Composite Airframe," Wichita State University, December 2008.

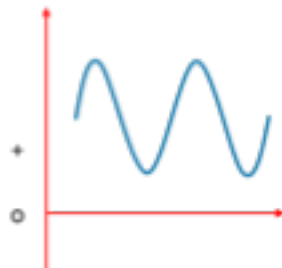


Stress Ratio (R)

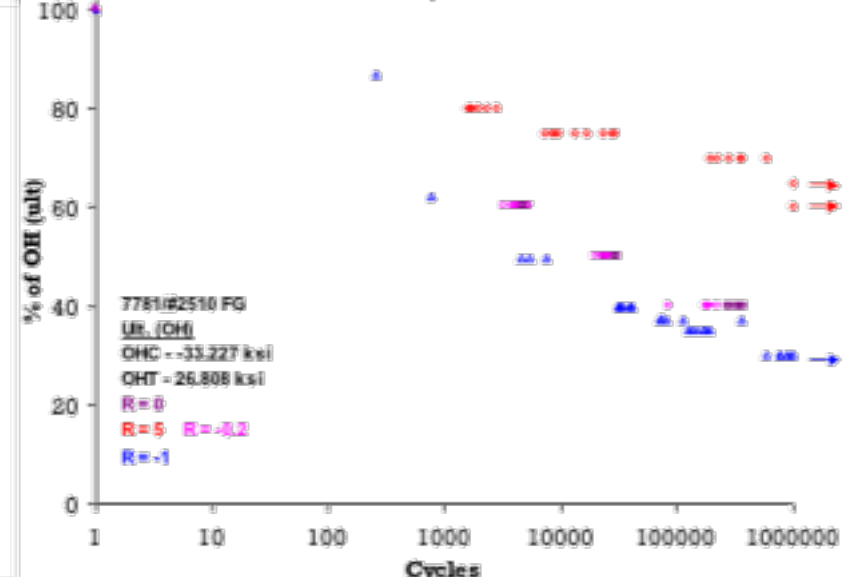
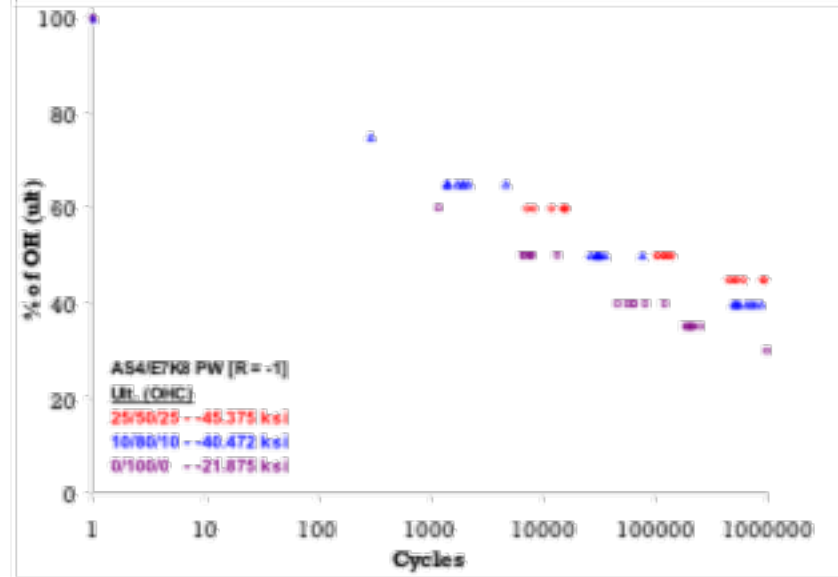
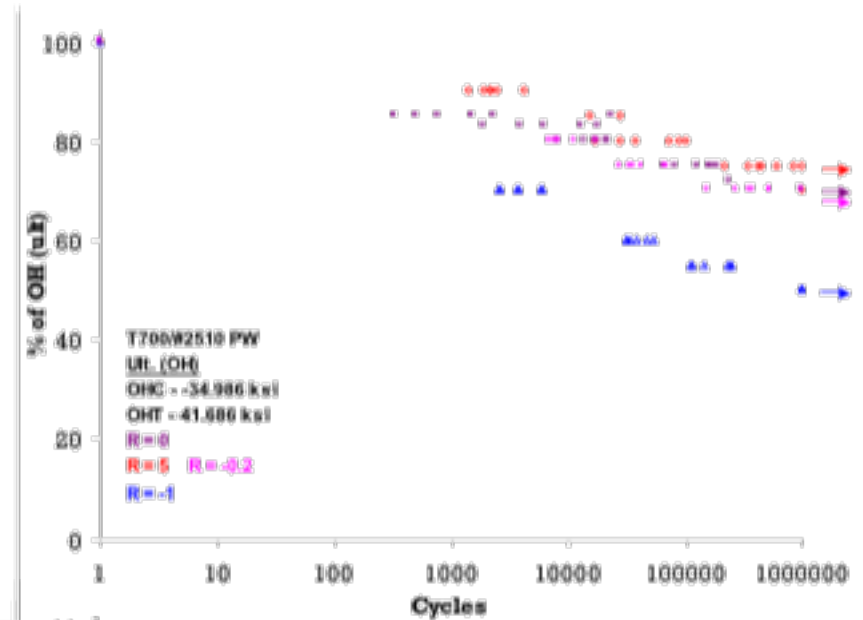
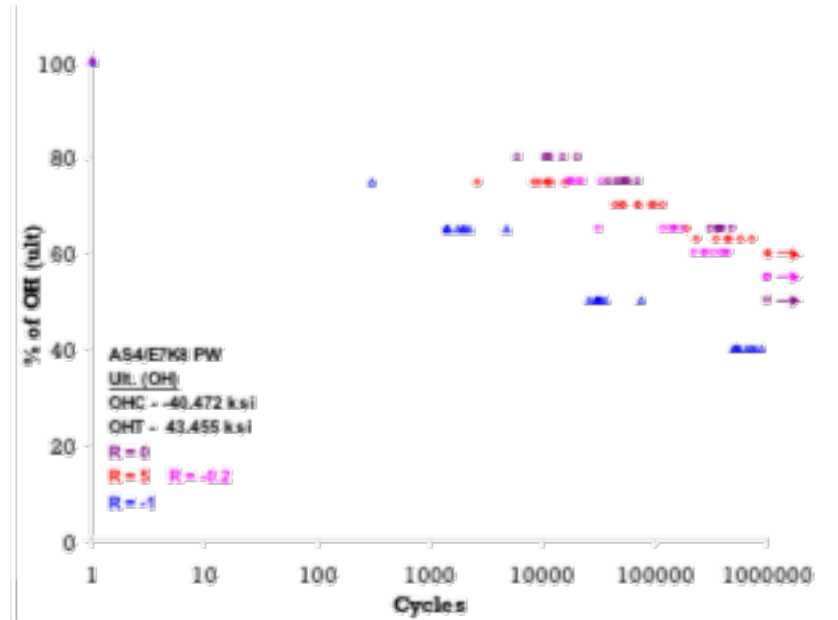
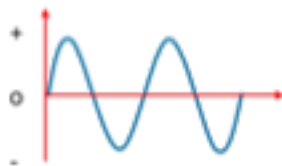
$R = \text{min} / \text{max stress}$



$1 > R > 0$: T-T



$R < 0$: C-T





Fatigue Scatter Analysis Techniques

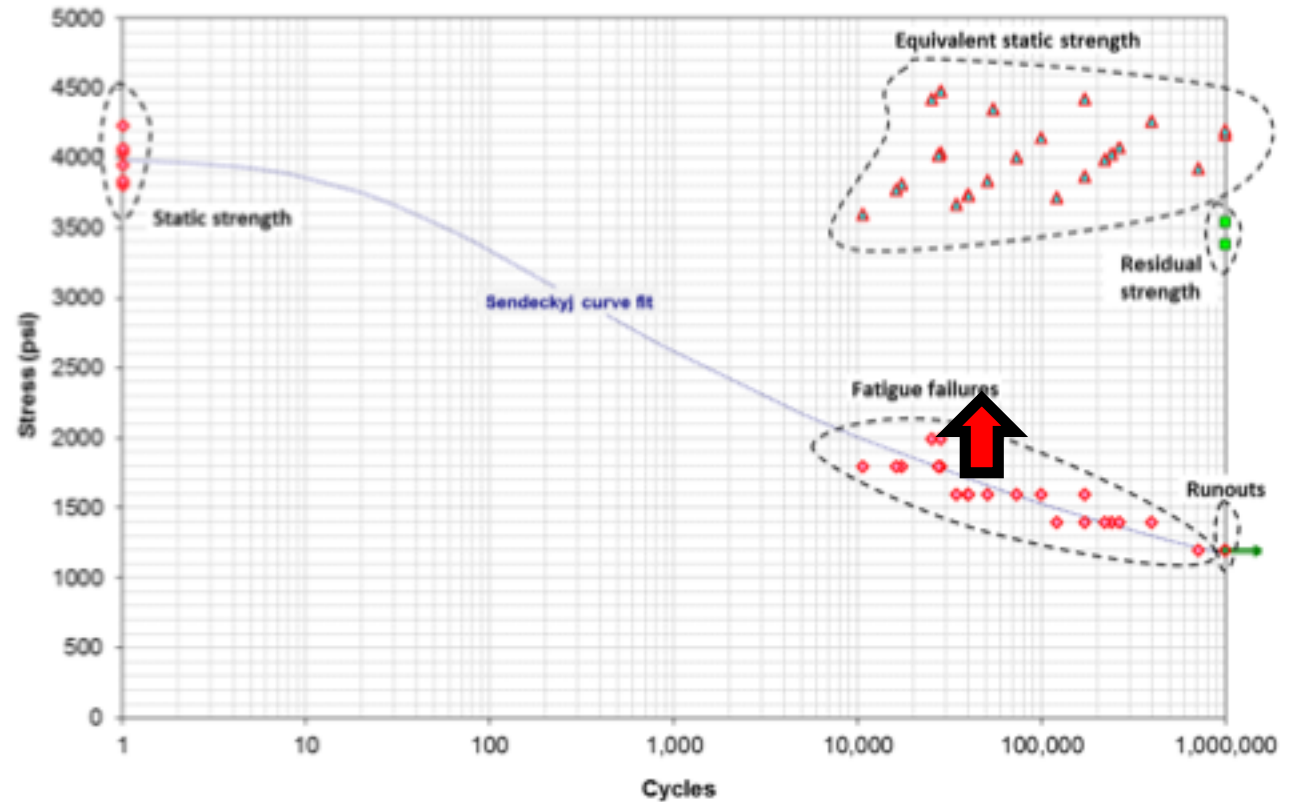
- Individual Weibull
- Joint Weibull

$$\sum_{i=1}^M \left\{ n_{fi} \cdot \left[\frac{\sum_{j=1}^{n_i} x_{ij}^{\hat{\alpha}} \cdot \ln(x_{ij})}{\sum_{j=1}^{n_i} x_{ij}^{\hat{\alpha}}} - \frac{1}{\hat{\alpha}} - \frac{\sum_{j=1}^{n_{fi}} \ln(x_{ij})}{n_{fi}} \right] \right\} = 0$$

- **Sendeckyj Equivalent Strength Model**

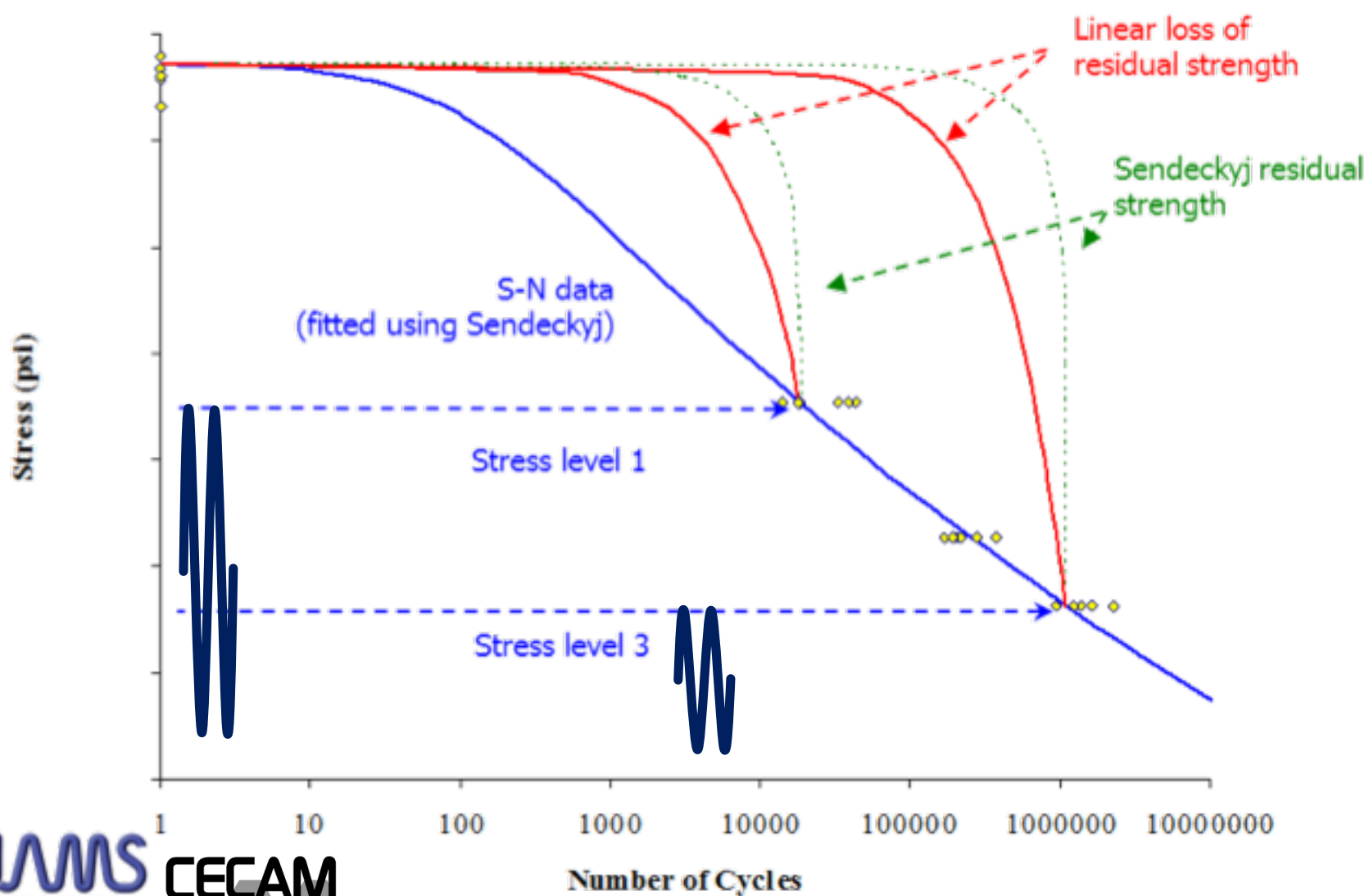
$$\sigma_e = \sigma_a \left[\left(\frac{\sigma_r}{\sigma_a} \right)^{1/S} + (N_f - 1) \cdot C \right]^S$$

Data Pooling Techniques



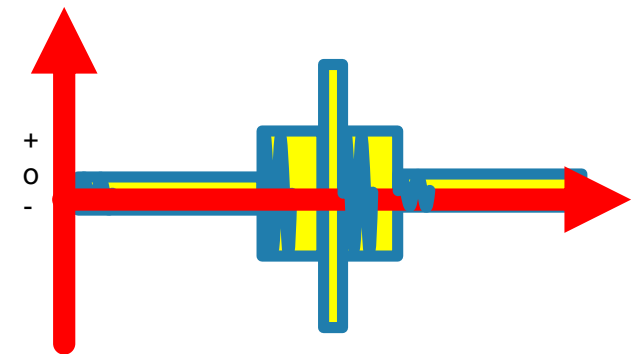


Wearout under Constant Amplitude Fatigue



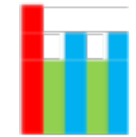
$$\sigma_r = \sigma_e + \left(\frac{\sigma_a - \sigma_e}{N_f(\sigma_a)} \right) \cdot n_f$$

$$\sigma_r = \sigma_a \left[\left(\frac{\sigma_e}{\sigma_a} \right)^{1/S} - C(n_f - 1) \right]^S$$

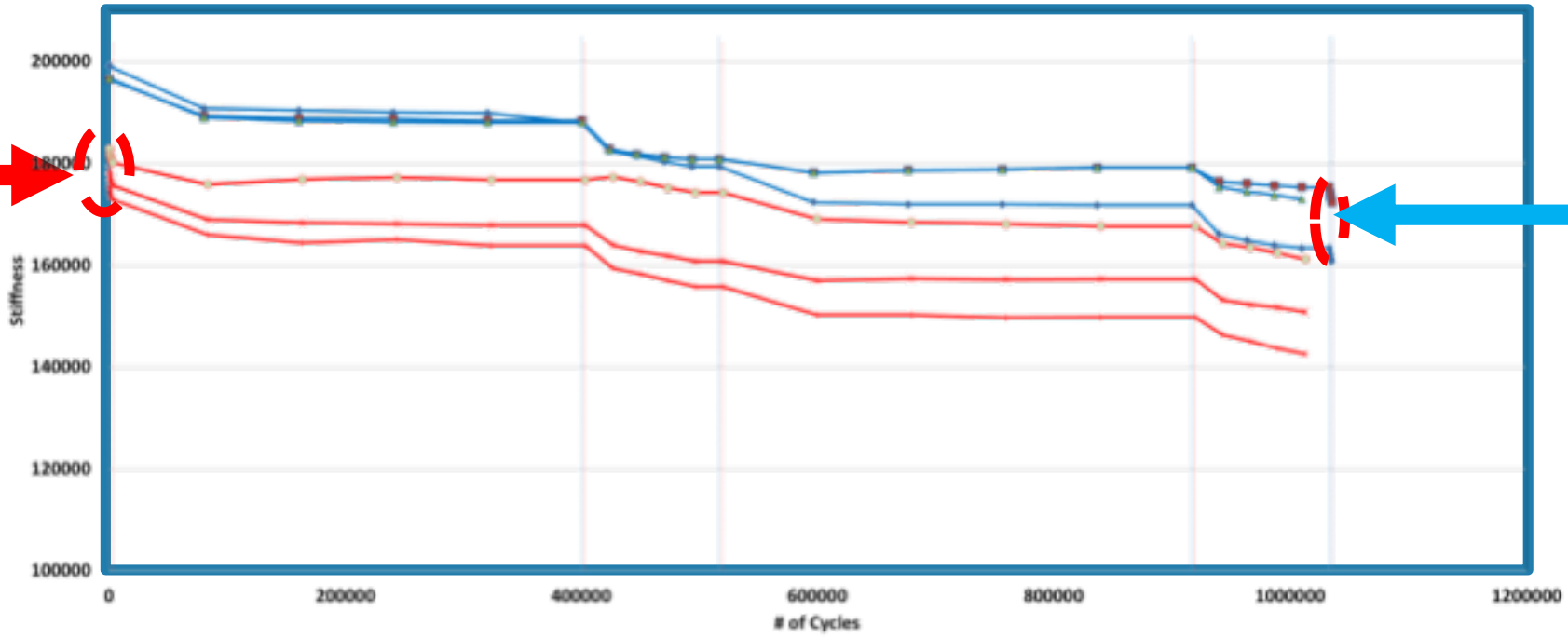




Residual Strength Degradation - Variable Amplitude Fatigue



Fatigue Profile 5	
Stress Level	# of Cycle
70	3000
40	400010
55	116330
40	400010
55	116330



Fatigue Profile 6	
Stress Level	# of Cycle
40	400010
55	116330
40	400010
55	116330
70	3000

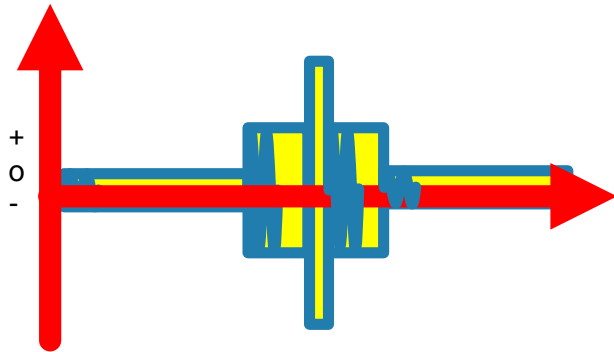


REF: Seneviratne, W., and Tomblin, J., *Load Sequencing Effects and Damage Growth Retardation of Composites*, FAA Joint Advanced Materials & Structures (JAMS), Grapevine, TX, 2016.

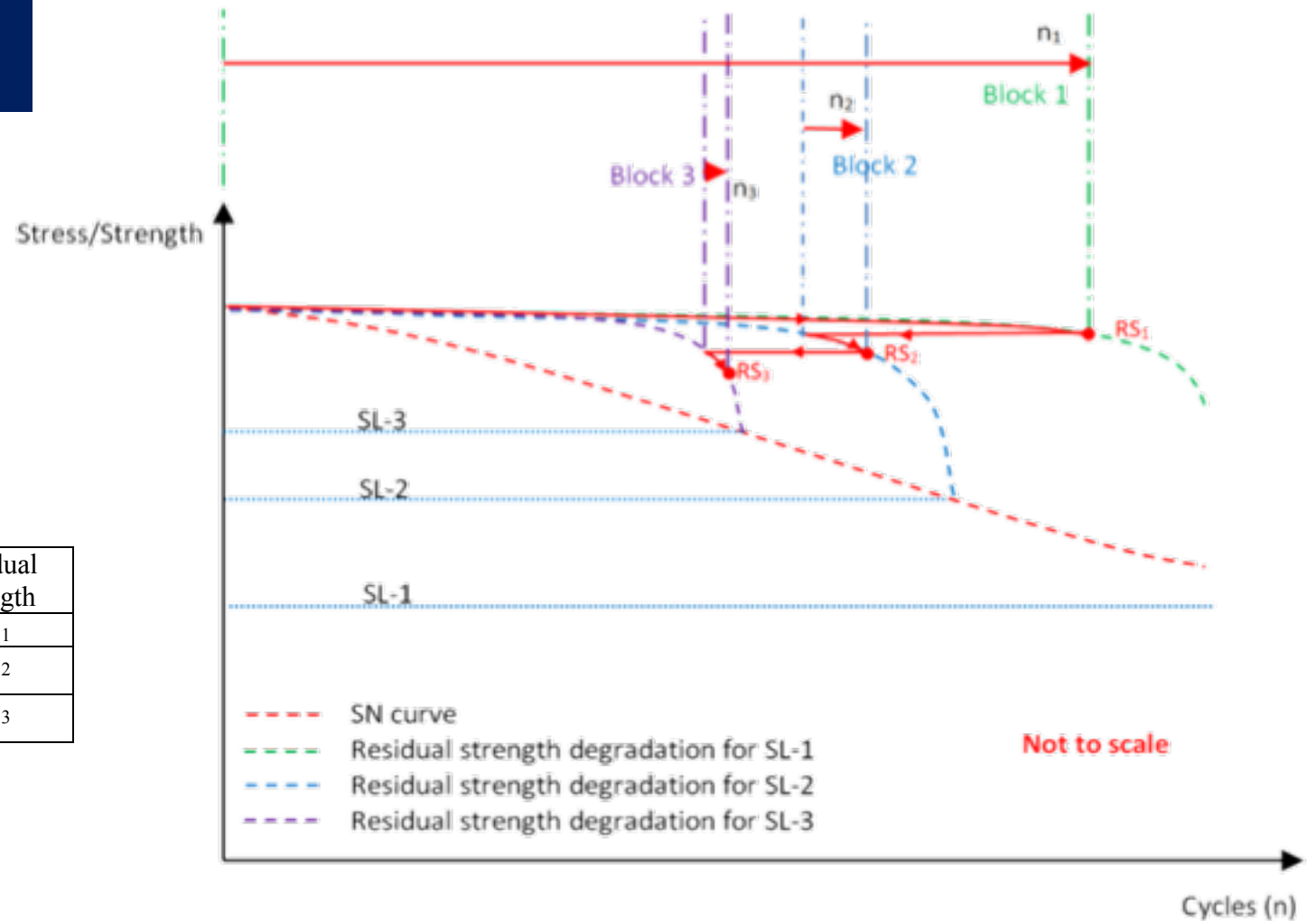


Strength Tracking (ST) Method

Fatigue Model Based on Residual Strength Degradation (Wearout)



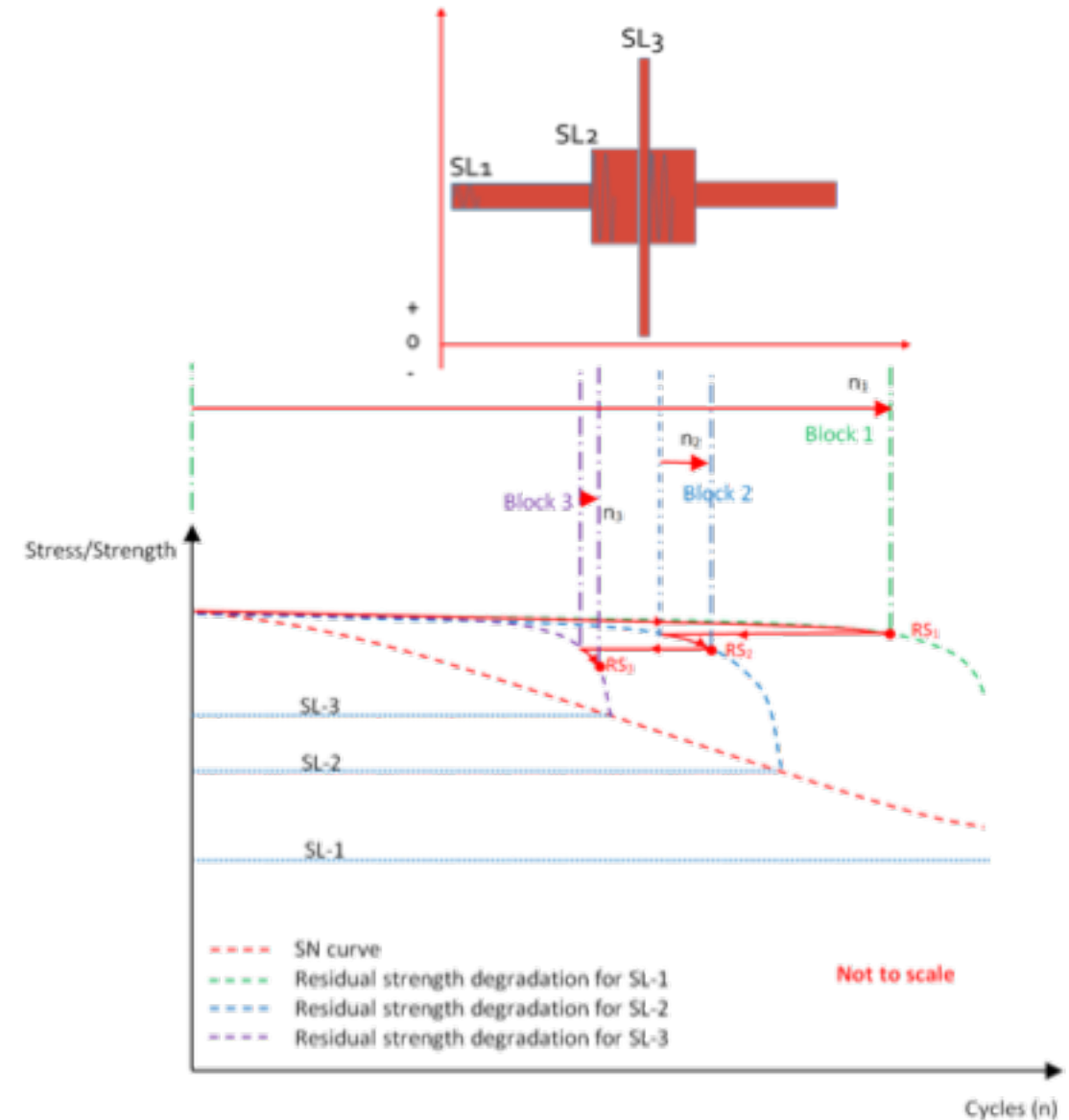
Block No.	Stress Ratio	Stress Level	Number of Cycles in Block	Cumulative Cycles	Residual Strength
1	$R = -1$	SL-1	n_1	n_1	RS_1
2	$R = -1$	SL-2	n_2	$n_1 + n_2$	RS_2
3	$R = -1$	SL-3	n_3	$n_1 + n_2 + n_3$	RS_3





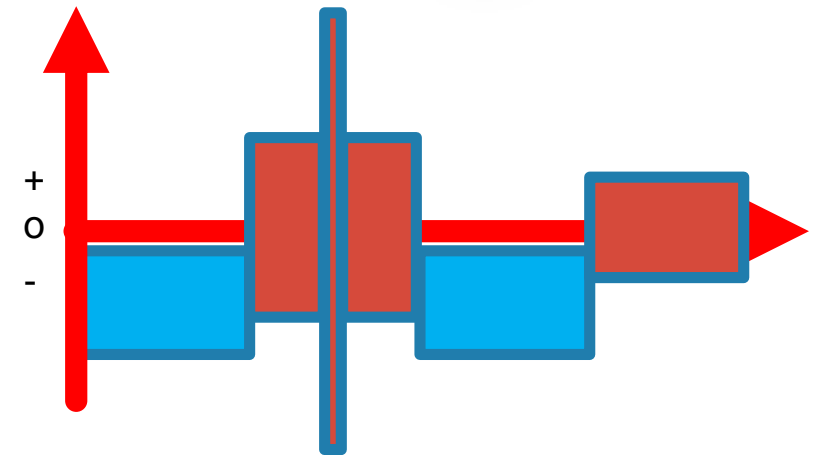
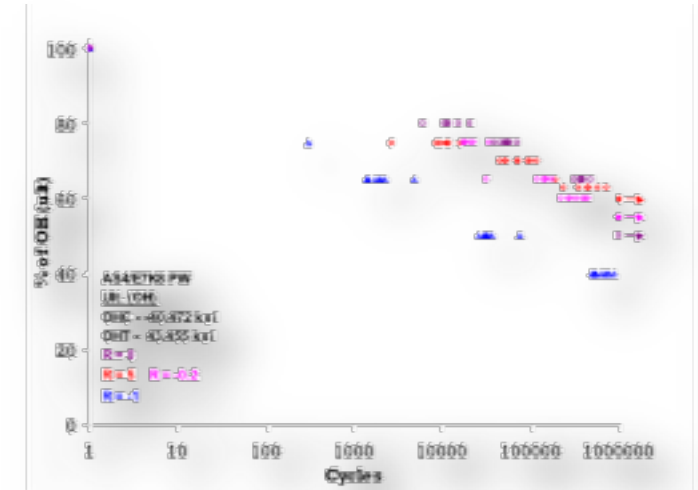
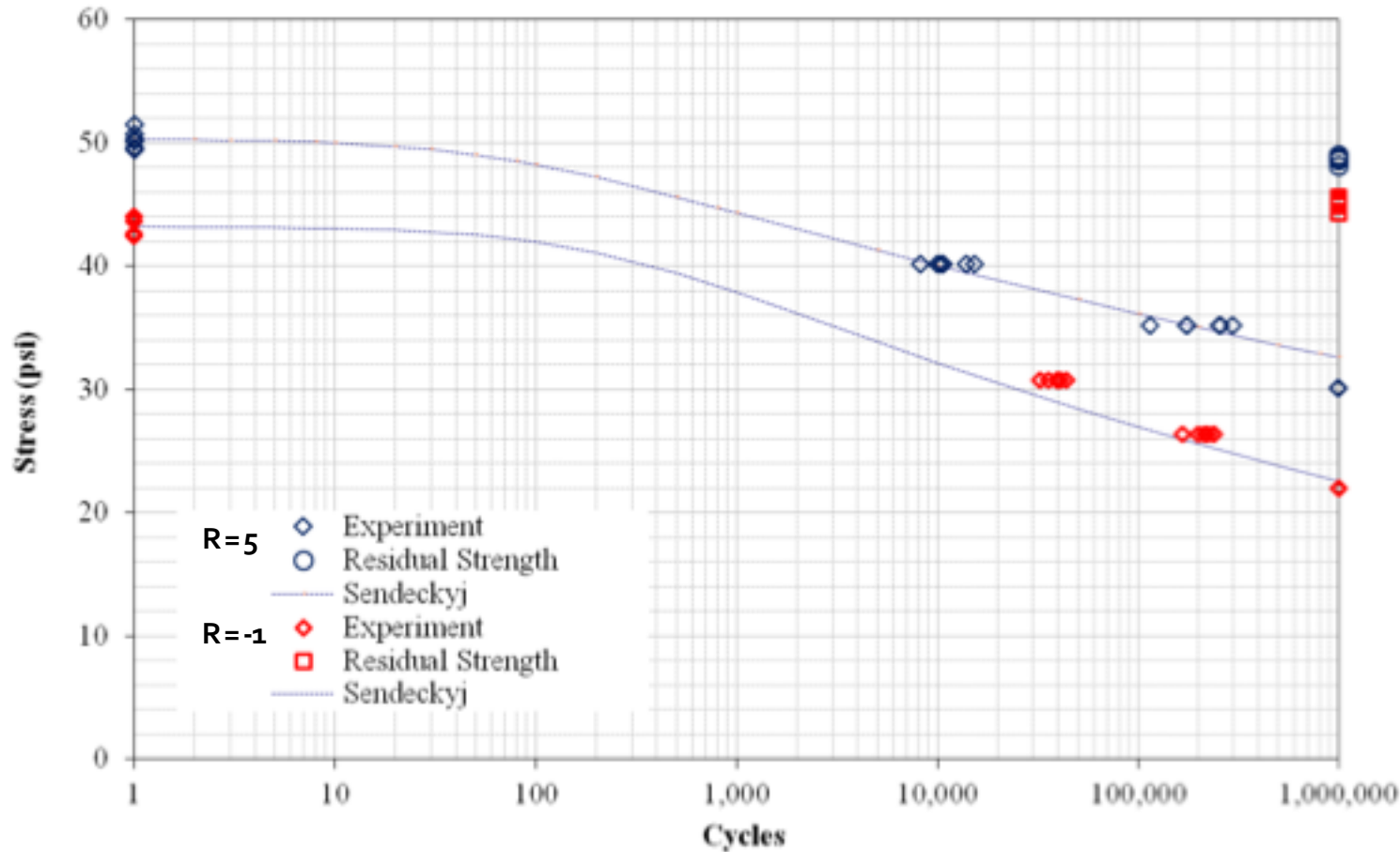
ST Method - Application

1. Fatigue testing and generate SN data
2. Fatigue data scatter analysis of SN data
 - Generate fitting parameters for Sendeckyj analysis
 - Fatigue data scatter is considered (reliability!)
3. Generate residual strength degradation models
4. Use the residual strength degradation for each block
 - Sequencing effects are considered
5. Predict residual strength degradation or fatigue life
 - Applied stress \geq Residual strength \rightarrow Fatigue failure



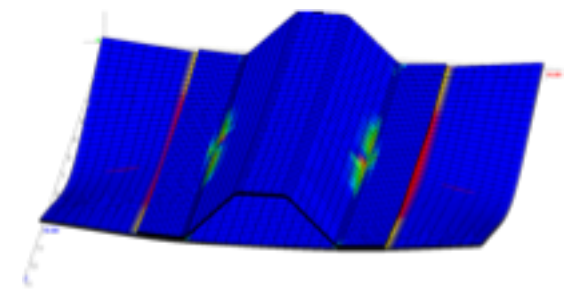
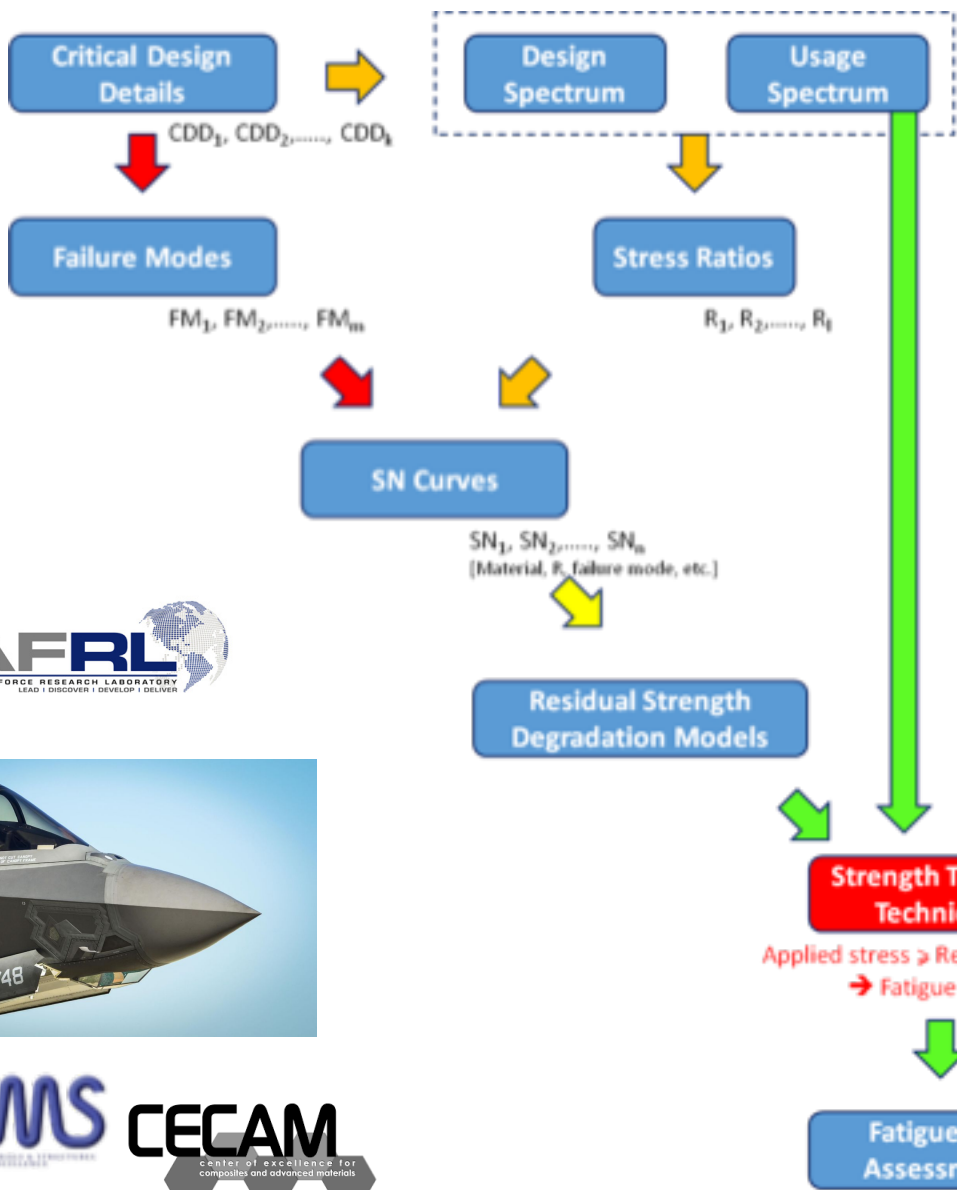


ST Method - Spectra with Multiple Stress Ratios

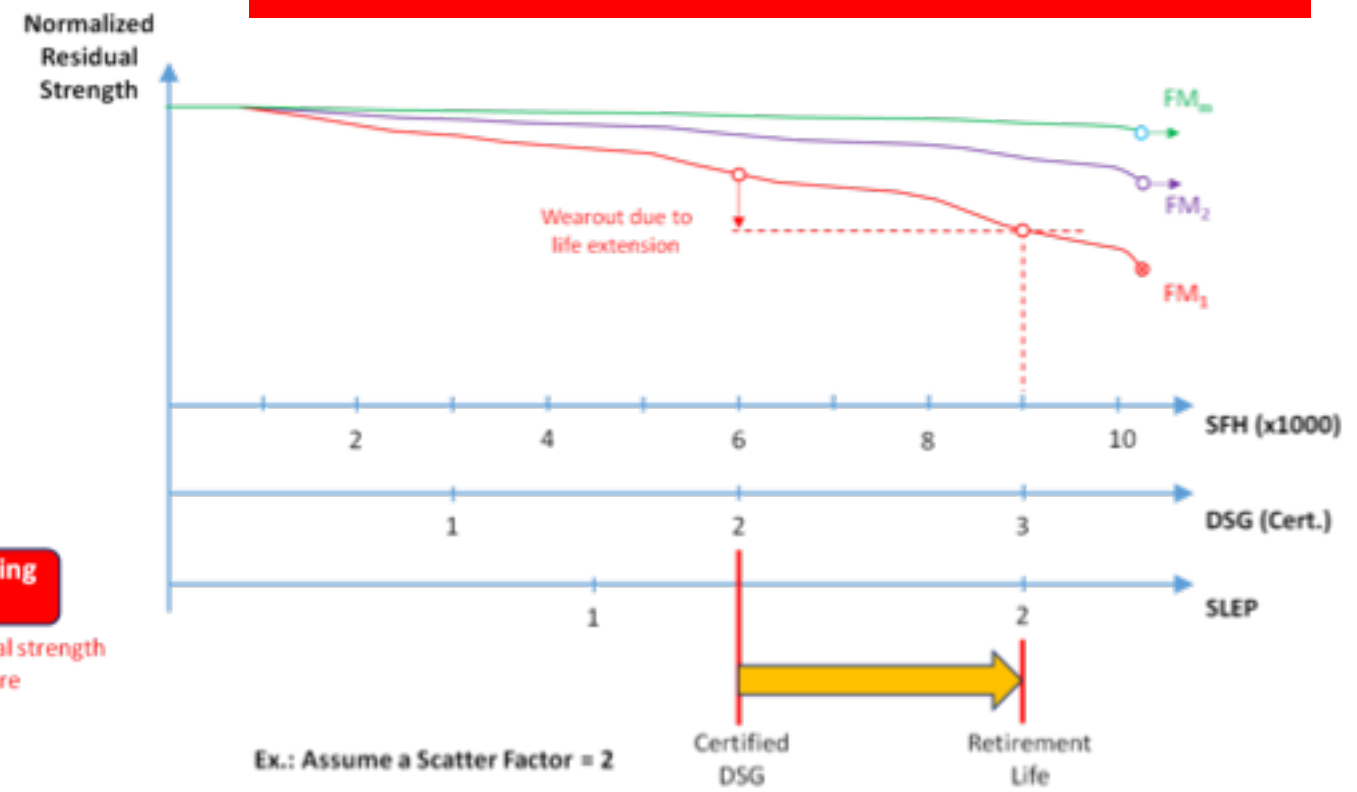




ST Method for Structural Applications



Service Life Assessment & Service Life Extension





Spectrum Fatigue Test Results (25/50/25 PW)

SPECIMEN #	R-Ratio	Load Block 1			Load Block 2			Load Block 3			Load Block 4			Load Block 5			Total # of Cycles Survived
		Max Stress [ksi]	Min Stress [ksi]	Cycles Survived	Max Stress [ksi]	Min Stress [ksi]	Cycles Survived	Max Stress [ksi]	Min Stress [ksi]	Cycles Survived	Max Stress [ksi]	Min Stress [ksi]	Cycles Survived	Max Stress [ksi]	Min Stress [ksi]	Cycles Survived	
25-50-25-P1-OH-4	5	-6	-30	300000	-7	-35	50000	-8	-40	5000	-7	-35	50000	-6	-30	300000	705000
25-50-25-P1-OH-6	5	-6	-30	300000	-7	-35	50000	-8	-40	5000	-7	-35	50000	-6	-30	70210	475210
25-50-25-P1-OH-S	5	-6	-30	300000	-7	-35	50000	-8	-40	2423	-7	-35	-	-6	-30	-	352423
25-50-25-P2-OH-A	5	-6	-30	300000	-7	-35	50000	-8	-40	1936	-7	-35	-	-6	-30	-	351936
25-50-25-P2-OH-B	5	-6	-30	300000	-7	-35	50000	-8	-40	5000	-7	-35	50000	-6	-30	300000	705000
25-50-25-P2-OH-C	5	-6	-30	300000	-7	-35	50000	-8	-40	5000	-7	-35	7621	-6	-30	-	362621
25-50-25-P1-OH-7	-1	25	-25	200000	30	-30	10000	35	-35	43	30	-30	-	25	-25	-	210043
25-50-25-P1-OH-8	-1	25	-25	200000	30	-30	10000	35	-35	558	30	-30	-	25	-25	-	210558
25-50-25-P1-OH-9	-1	25	-25	200000	30	-30	10000	35	-35	125	30	-30	-	25	-25	-	210125
25-50-25-P1-OH-T	-1	25	-25	174580	30	-30	-	35	-35	-	30	-30	-	25	-25	-	174580
25-50-25-P1-OH-U	-1	25	-25	200000	30	-30	190	35	-35	-	30	-30	-	25	-25	-	200190
25-50-25-P1-OH-V	-1	25	-25	200000	30	-30	1477	35	-35	-	30	-30	-	25	-25	-	201477
25-50-25-P2-OH-7	-1	25	-25	200000	30	-30	5000	35	-35	83	30	-30	-	25	-25	-	205083
25-50-25-P2-OH-8	-1	25	-25	200000	30	-30	5000	35	-35	70	30	-30	-	25	-25	-	205070
25-50-25-P2-OH-9	-1	25	-25	200000	30	-30	5000	35	-35	533	30	-30	-	25	-25	-	205533
25-50-25-P2-OH-D	-1 & 5	-6	-30	200000	25	-25	200000	-7	-35	20000	30	-30	-				420000
25-50-25-P2-OH-E	-1 & 5	-6	-30	200000	25	-25	200000	-7	-35	5122	30	-30	-				405122
25-50-25-P2-OH-F	-1 & 5	-6	-30	200000	25	-25	200000	-7	-35	20000	30	-30	1213				421213



Validation of ST Method – 25/50/25 PW Preliminary Results

Fatigue Analysis

Fatigue Test Results

25/50/25												
Block	Σn	σ_e	S	C	R	σ_a	σ_{max}	σ_{min}	n_i	n_{eqv}	n_{tot}	$\sigma_r(n,R,\sigma)$
1	0	50.254	0.045	0.015	5	30	-6.000	-30.000	300000	0	300000	50.143
2	300000	50.254	0.045	0.015	5	35	-7.000	-35.000	50000	9760	59760	49.470
3	350000	50.254	0.045	0.015	5	40	-8.000	-40.000	5000	3075	8075	46.992
4	355000	50.254	0.045	0.015	5	35	-7.000	-35.000	45517	156963	202480	35.007
									<u>400517</u>			
Block	Σn	σ_e	S	C	R	σ_a	σ_{max}	σ_{min}	n_i	n_{eqv}	n_{tot}	$\sigma_r(n,R,\sigma)$
1	0	44.923	0.077	0.005	-1	25	25.000	-25.000	200000	0	200000	42.930
2	200000	44.923	0.077	0.005	-1	30	30.000	-30.000	10000	18623	28623	41.101
3	210000	44.923	0.077	0.005	-1	35	35.000	-35.000	1000	3847	4847	38.537
4	211000	44.923	0.077	0.005	-1	30	30.000	-30.000	4609	36065	40674	33.878
									<u>215609</u>			
Block	Σn	σ_e	S	C	R	σ_a	σ_{max}	σ_{min}	n_i	n_{eqv}	n_{tot}	$\sigma_r(n,R,\sigma)$
1	0	50.254	0.045	0.015	5	30	-6.000	-30.000	200000	0	200000	50.180
2	200000	44.923	0.077	0.005	-1	25	25.000	-25.000	200000	-1445345	-1245345	49.752
3	400000	50.254	0.045	0.015	5	35	-7.000	-35.000	20000	40512	60512	49.458
4	420000	44.923	0.077	0.005	-1	30	30.000	-30.000	12373	-104239	-91866	49.123
									<u>432373</u>			

R = 5

705000

475210 475210

352423 352423

351936 351936

705000

362621 362621

492032 385548

R = -1

1 210043

1 210558

1 210125

2 174580

2 200190

2 201477

2 205083

2 205070

2 205533

202518

R = 5 & -1

420000

405122

421213

415445





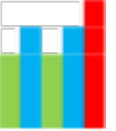
Validation of ST Method – 25/50/25 PW Load Sequencing

70-40-55-40-55 (High-Low)

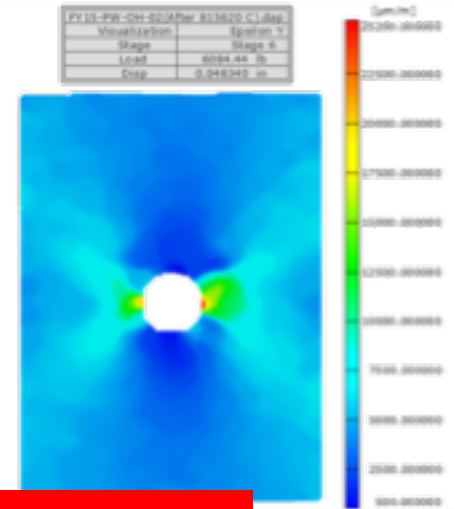


NAME	n=0 Reference	70% - n=1,040 Load Block 1	40% - n=401,050 Load Block 2	55% - n=415,610 Load Block 3	40% - n=815,620 Load Block 4	55% - n=830,180 Load Block 5
	PW-OH-27					
PW-OH-1						Failed at 823,523 cycles
PW-OH-2						Failed at 827,830 cycles

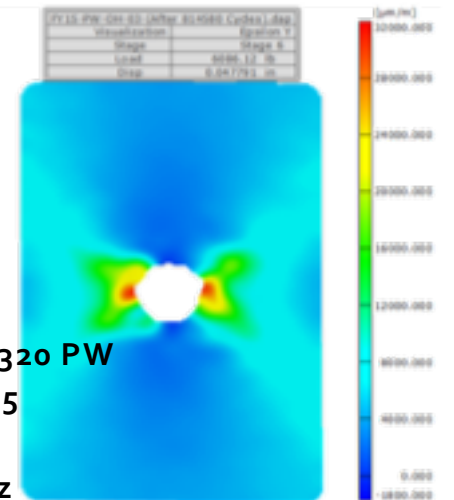
40-55-40-55-70 (Low-High)



NAME	n=0 Reference	40% - n=400,010 Load Block 1	55% - n=414,570 Load Block 2	40% - n=814,580 Load Block 3	55% - n=429,140 Load Block 4	70% - n=430180 Load Block 5
	PW-OH-3					Failed at 815,550 cycles
PW-OH-4					Failed at 822,849 cycles	
PW-OH-6					Failed at 816,002 cycles	



ST Predictions
n = 830,180



T650/5320 PW
25/50/25
R = -1
F = 5 Hz



Validation of ST Method – 40/20/40 PW Preliminary Results

Fatigue Analysis

Fatigue Test Results

40/20/40		[0/90/0/90/45/-45/90/0/90/0]s											
Block	Σn	σ_e	S	C	R	σ_a	σ_{max}	σ_{min}	n_i	n_{eqv}	n_{tot}	$\sigma_r(n,R,\sigma)$	
1	0	50.847	0.035	0.209	5	30	-6.000	-30.000	500000	0	500000	50.798	
2	500000	50.847	0.035	0.209	5	35	-7.000	-35.000	50000	5961	55961	50.327	
3	550000	50.847	0.035	0.209	5	40	-8.000	-40.000	3000	1207	4207	47.066	
4	553000	50.847	0.035	0.209	5	35	-7.000	-35.000	23766	195134	218900	35.217	
									576766				
Block	Σn	σ_e	S	C	R	σ_a	σ_{max}	σ_{min}	n_i	n_{eqv}	n_{tot}	$\sigma_r(n,R,\sigma)$	
1	0	51.298	0.080	0.006	-1	25	25.000	-25.000	500000	0	500000	49.503	
2	500000	51.298	0.080	0.006	-1	30	30.000	-30.000	50000	50465	100465	46.374	
3	550000	51.298	0.080	0.006	-1	35	35.000	-35.000	3000	14452	17452	43.663	
4	553000	51.298	0.080	0.006	-1	30	30.000	-30.000	18240	121320	139560	30.013	
									571240				
Block	Σn	σ_e	S	C	R	σ_a	σ_{max}	σ_{min}	n_i	n_{eqv}	n_{tot}	$\sigma_r(n,R,\sigma)$	
1	0	50.847	0.035	0.209	5	30	-6.000	-30.000	500000	0	500000	50.798	
2	500000	51.298	0.080	0.006	-1	25	25.000	-25.000	500000	160578	660578	48.721	
3	1000000	50.847	0.035	0.209	5	35	-7.000	-35.000	50000	154754	204754	46.224	
4	1050000	47.509	0.070	0.038	-1	30	30.000	-30.000	12334	5893	18227	30.071	
									1062334				

3 Specimens of R = 5 survived 1,103,00 cycles

R = -1

550,165

539,141

523,164

521,419

533,781

522,465

531,689

R = 5 & -1

1,015,810

1,046,541

1,050,001

1,037,451

R = -1 & 5

1,000,190

1,006,941

1,035,966

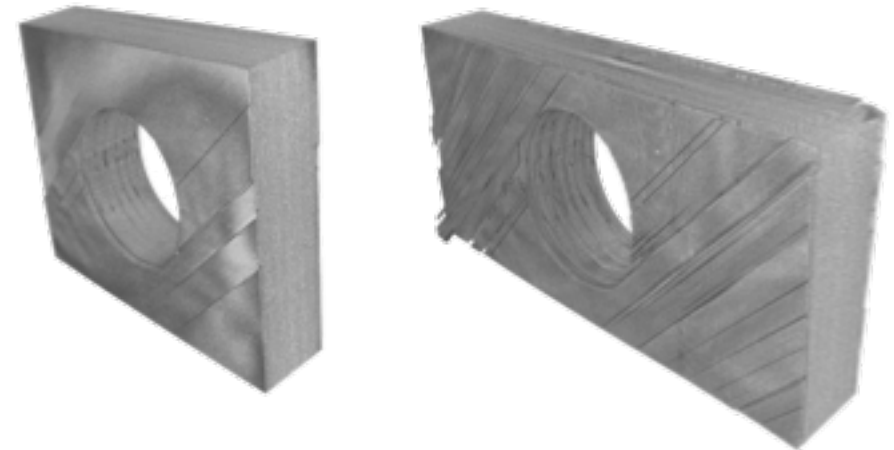
1,014,366





High-Fidelity Inspections for Damage Characterization

X-Ray Computed Tomography (XCT)





High-Fidelity Inspections: NSI X7000 X-Ray CT System

- **Dual X-ray Tubes**

- 225kV Micro-focus (6 μm) for low attenuating/low density materials, e.g. Carbon Fiber Composites.
- 450 kV Mini-focus for high attenuating/high density materials, e.g. Metals

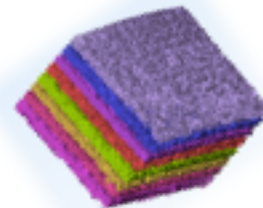
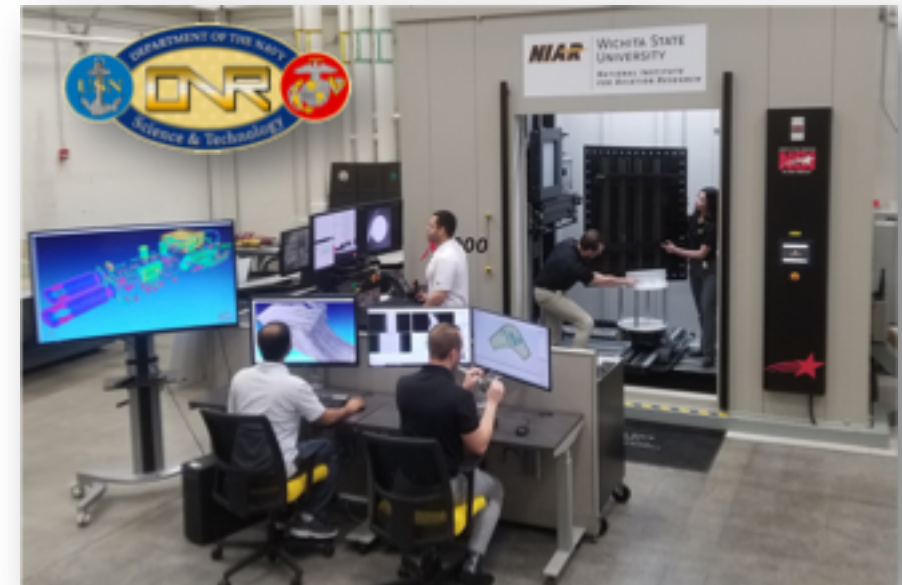
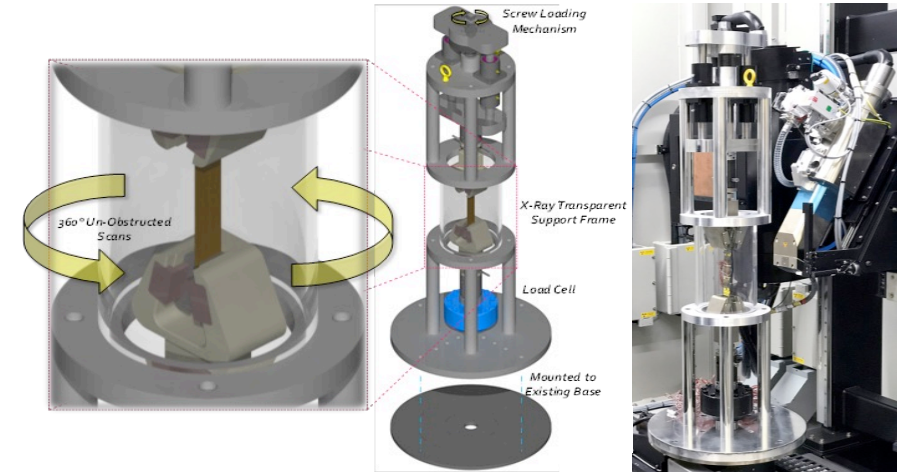
- **Dual Detectors**

- Perkin Elmer flat panel detector 16" \times 16"
- Linear Diode Array (LDA) allows high precision data acquisition

- **Software**

- NSI proprietary software for reconstruction of 3D volume
- Materialise Mimics and 3Matic is used for data segmentation and data export into formats conducive for analysis

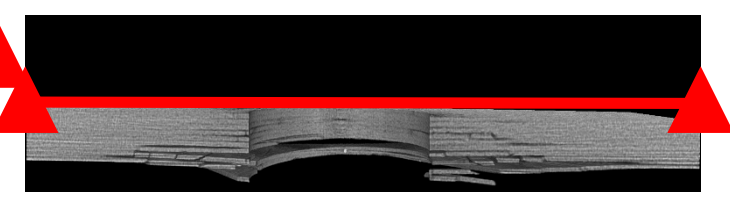
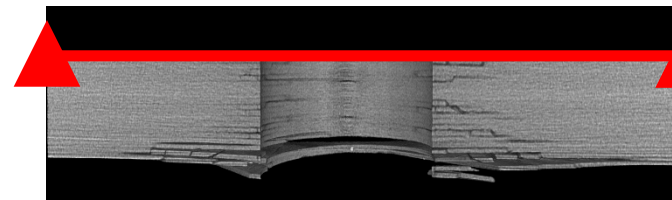
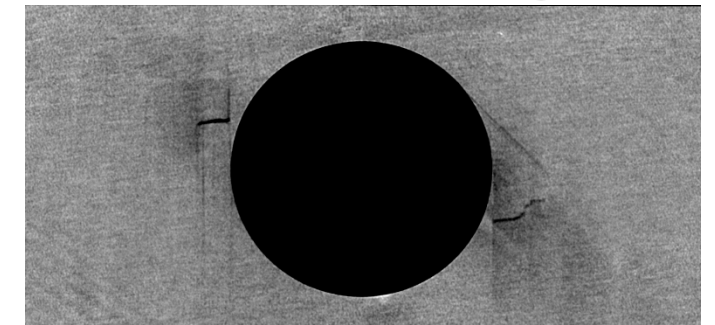
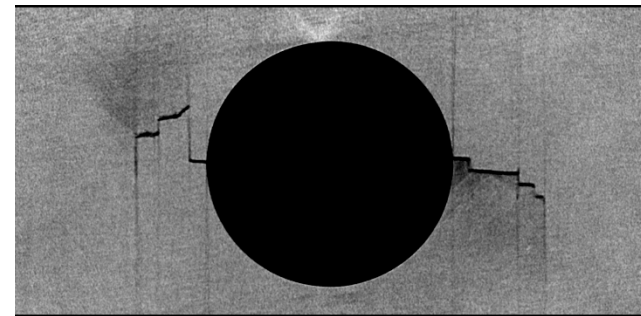
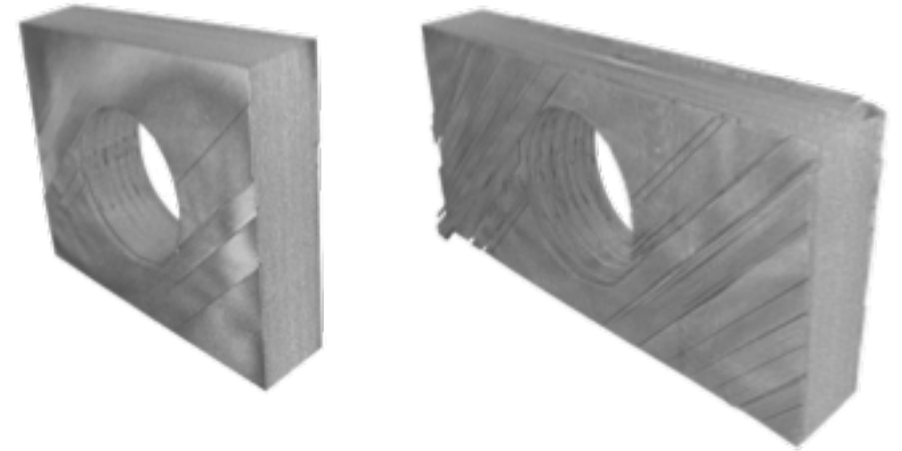
- **Portable Load Fixture**





X-Ray CT: Damage Monitoring

- High-fidelity ply-by-ply damage information
- Initiation site(s) detection and propagation details
- Interaction of different failure modes
- Multi-site damage interactions

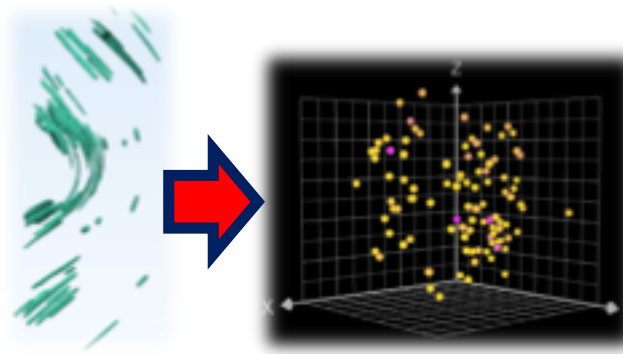
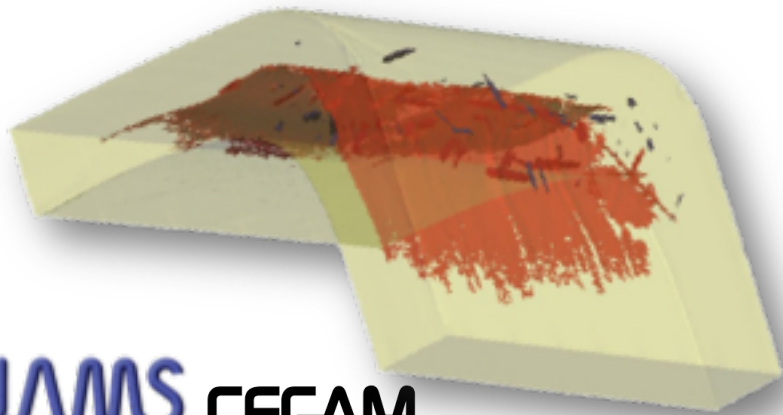
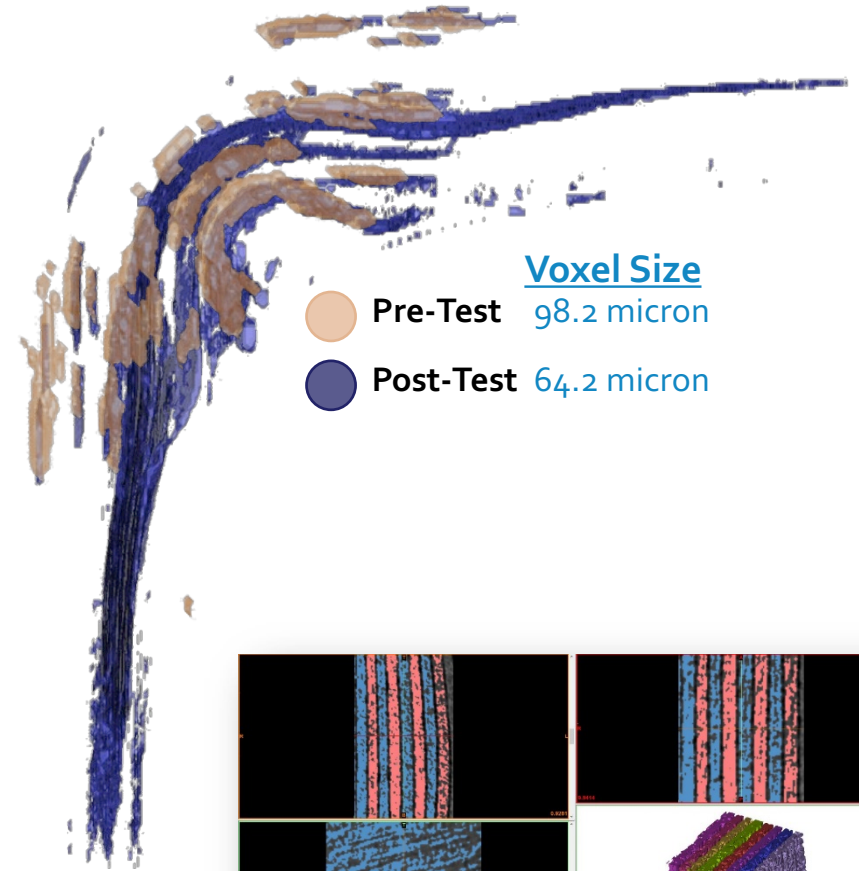


Fatigue damaged open-hole test specimen

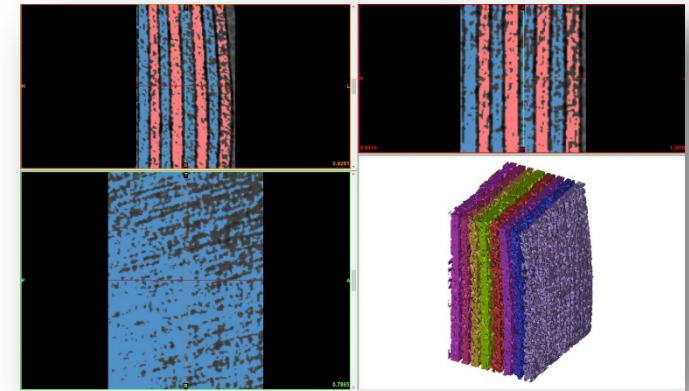


Feature Segmentation – Effects of Defects

- Segment and isolate the features of interest in Mimics
- These features can be meshed and exported as STL files for further analysis
- This information can be used as input parameters for damage modeling



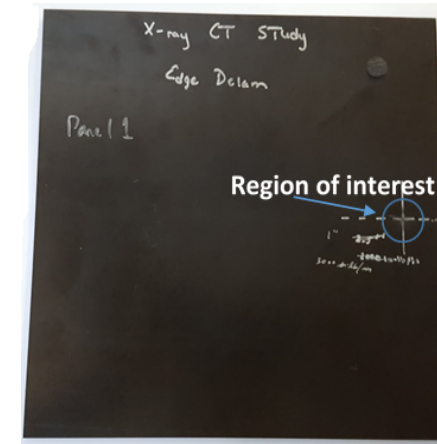
Spatial distribution of defects



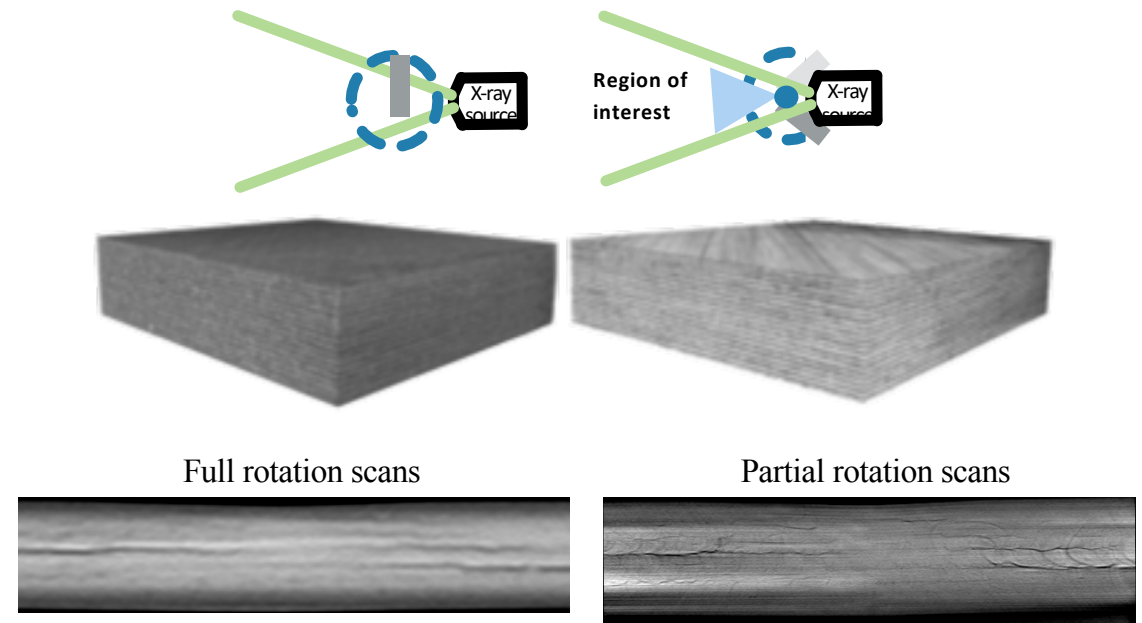


Technique Development

- Partial Rotation vs Full Rotation
 - Usually CT captures images from 360° around the object.
 - Using partial rotation scans it is possible to obtain higher resolution images of a smaller area.
 - This is a useful option to have when the object dimensions are larger than the area of interest.
 - Number of projections can be increased.



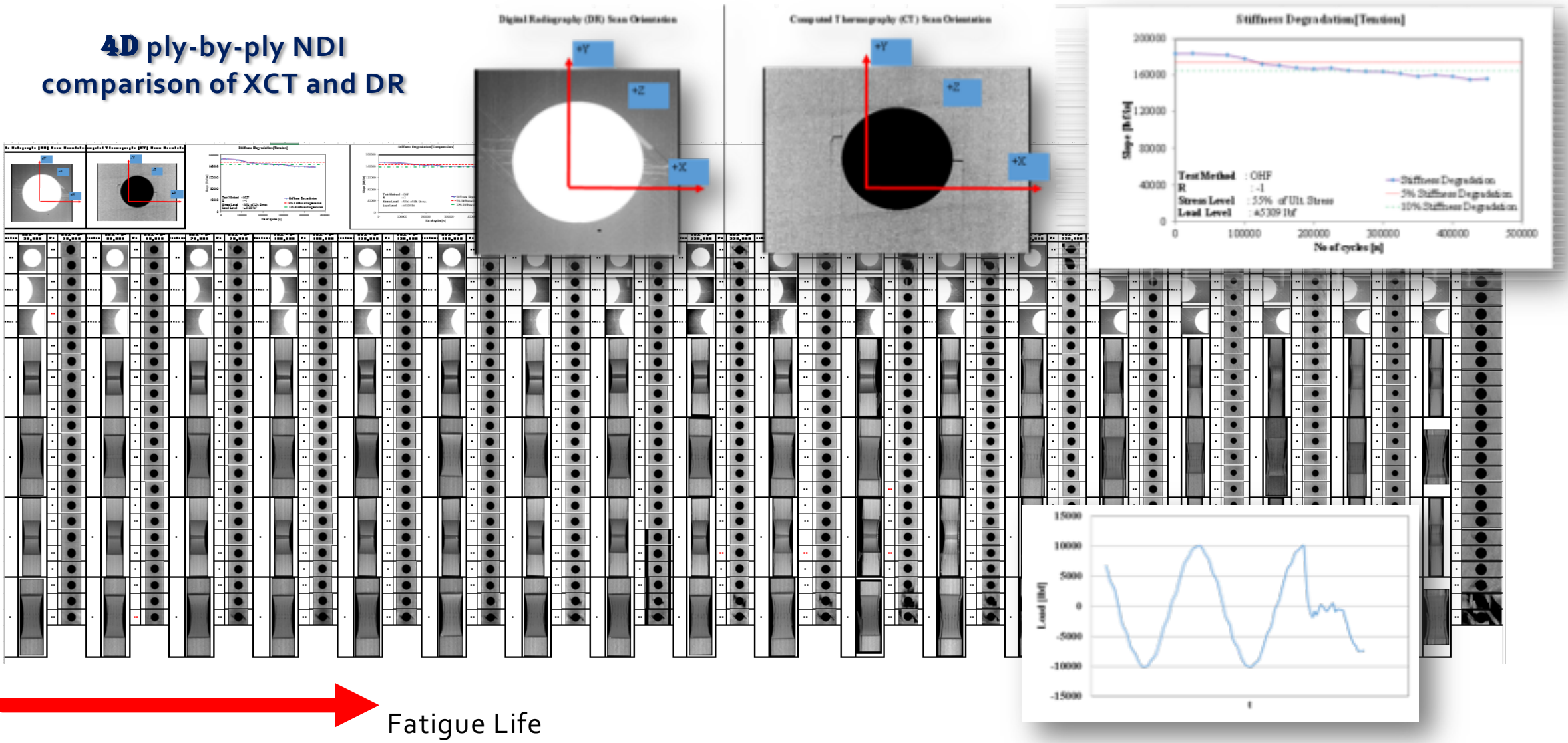
Area of interest can be moved closer to the source improving resolution.





High-Fidelity NDI for Damage Characterization (Database)

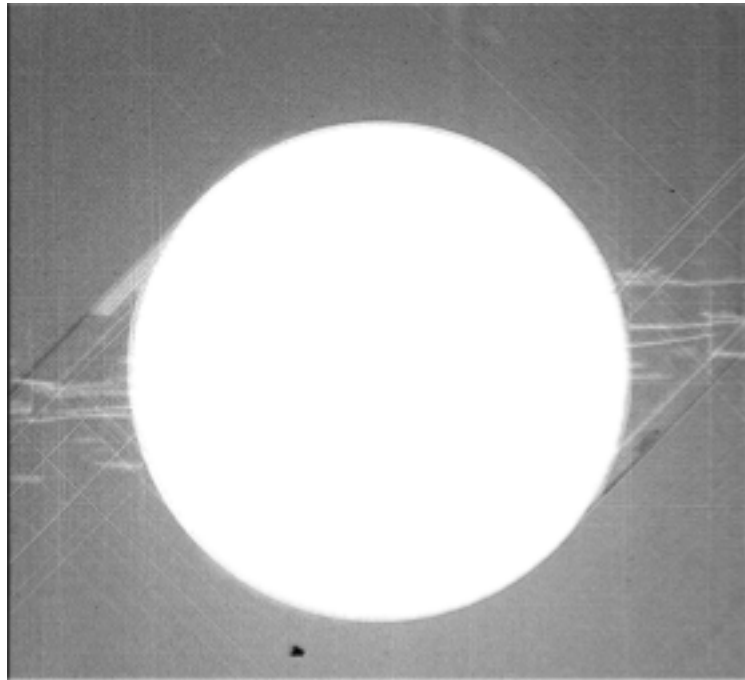
4D ply-by-ply NDI comparison of XCT and DR





DR vs. CT for Characterizing Fatigue Damage

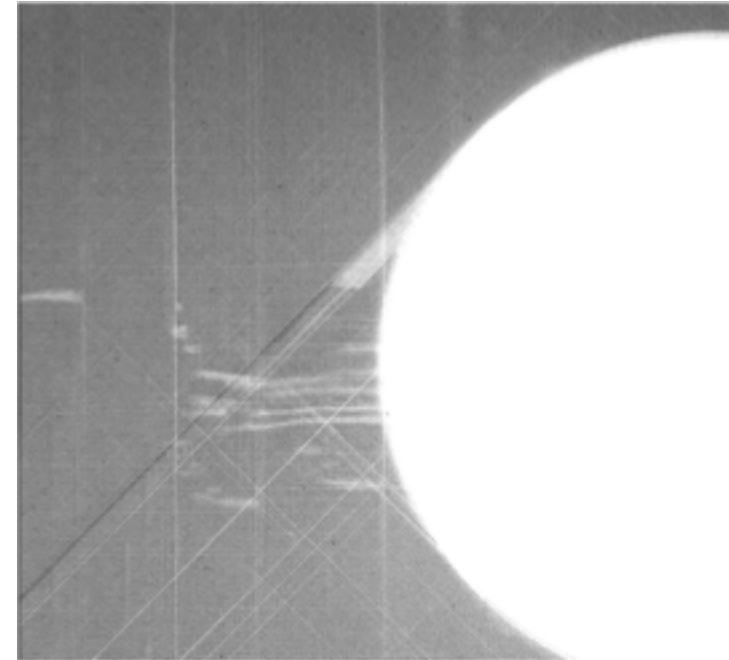
DR



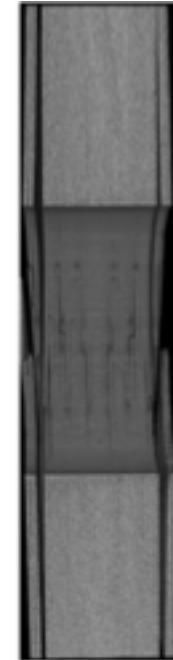
CT



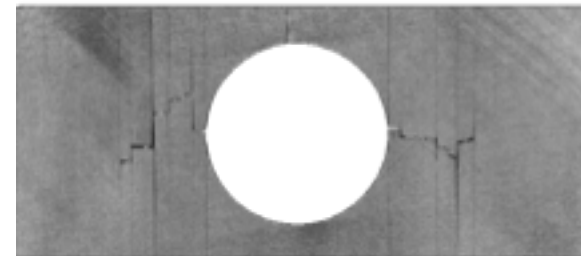
DR



CT



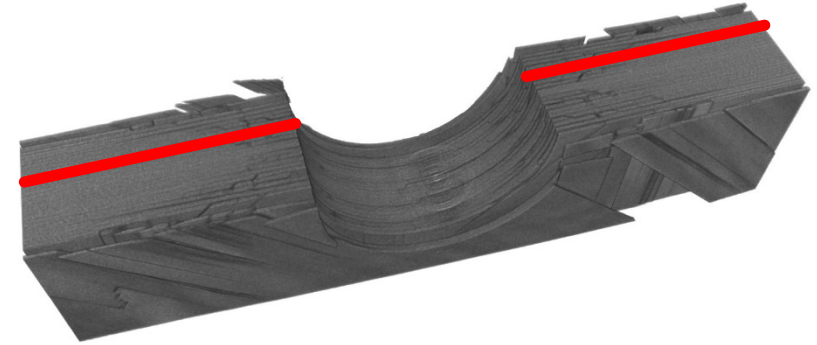
CT





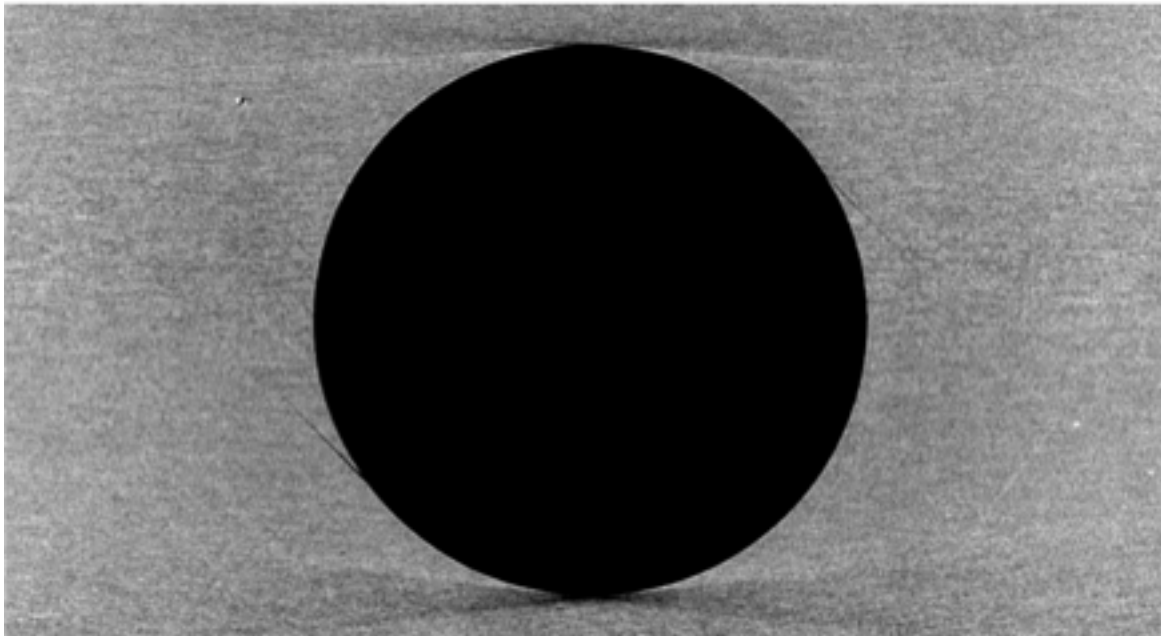
4D XCT - Fatigue Damage Progression (Ply-by-Ply)

- OH-UNI-10 [45/0/-45/90]_{3s}
 - Stress level – 55% (27.3 ksi)
 - R = -1



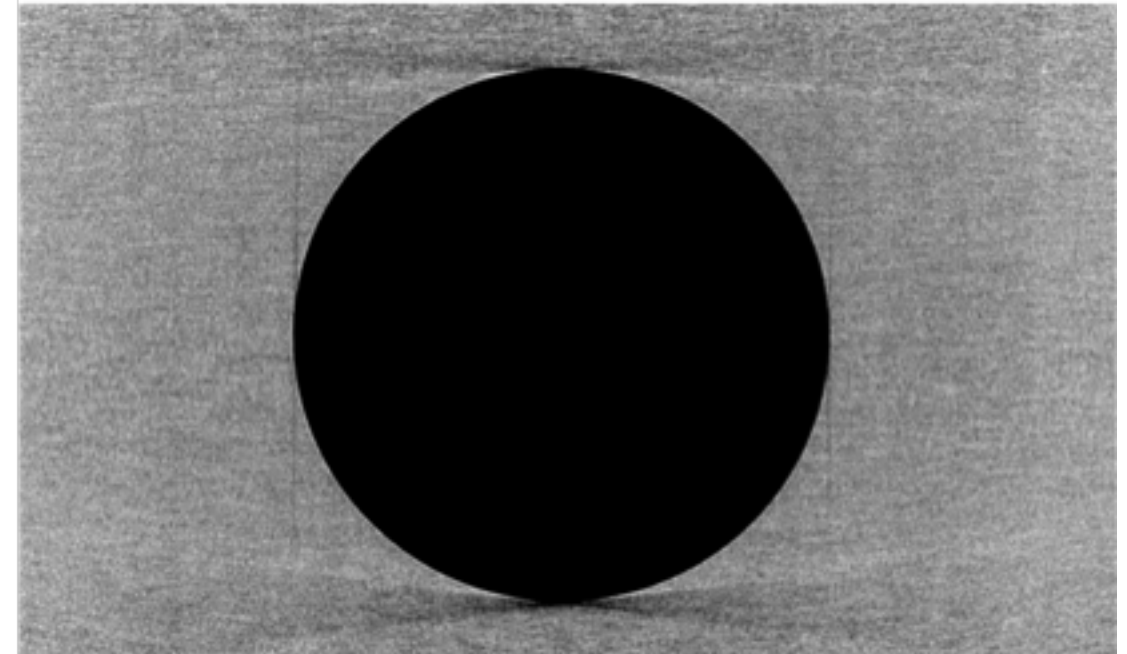
Ply #5/24 [45°]

N = 25,000



Ply #6/24 [0°]

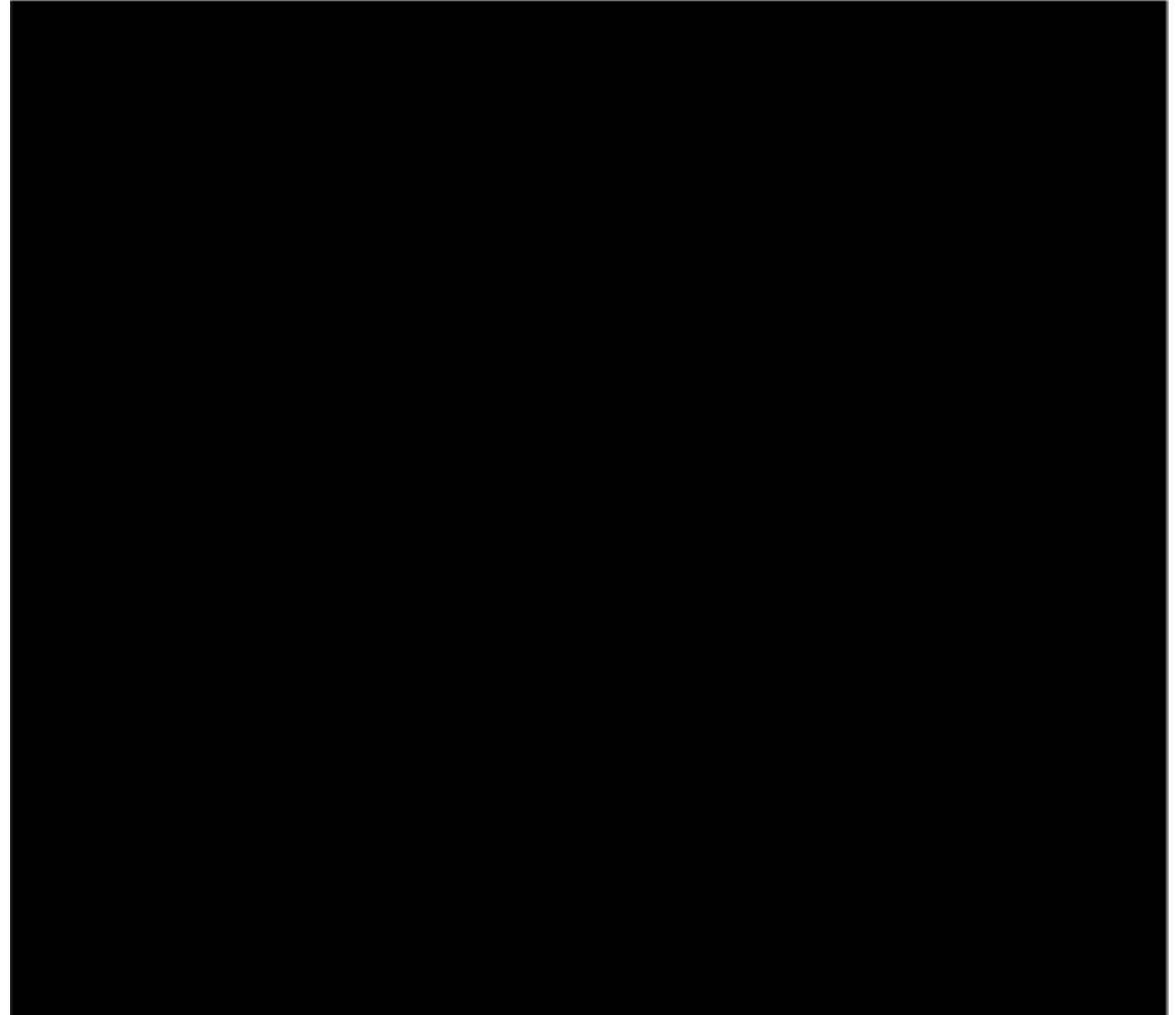
N = 25,000





3D XCT - Open-Hole (Plain Weave fabric)

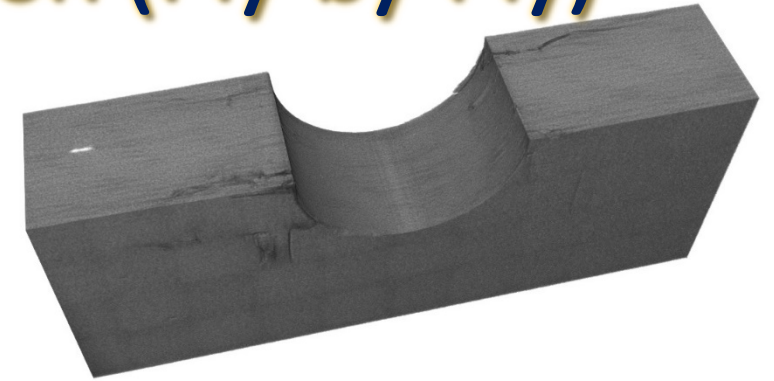
T650/5320-1 PW
PW-OHC-8 (40/20/40)
Quasi-Isotropic
Constant Amplitude (R = -1)
Stress Level = 35 ksi
n = 22,250



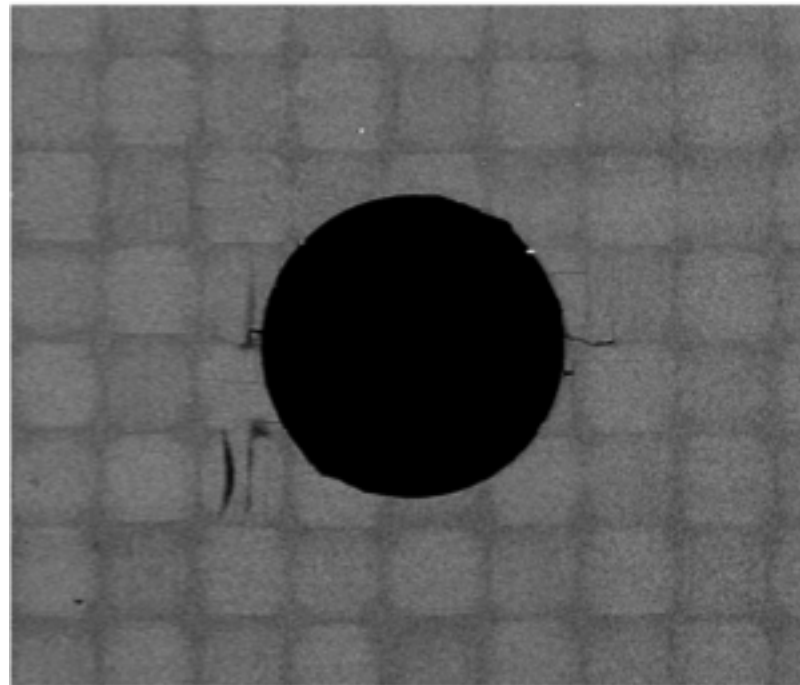


4D XCT - Fatigue Damage Progression (Ply-by-Ply)

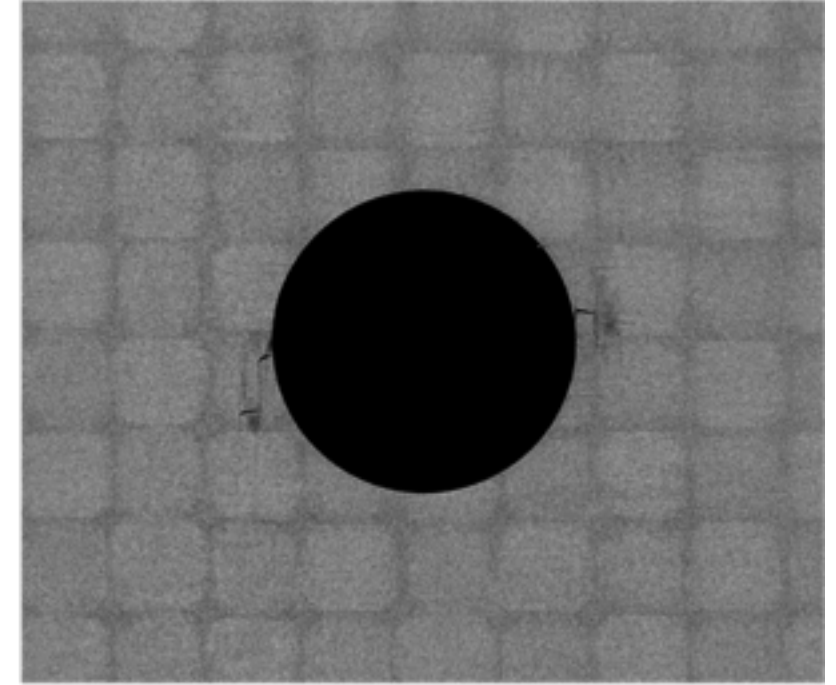
- OH-PW-8 [0/90/0/90/45/-45/90/0/90/0]_s
 - Stress = 35 ksi
 - R = -1
 - n = 25630



Ply #1/20 [0°/90°] N = 5,000



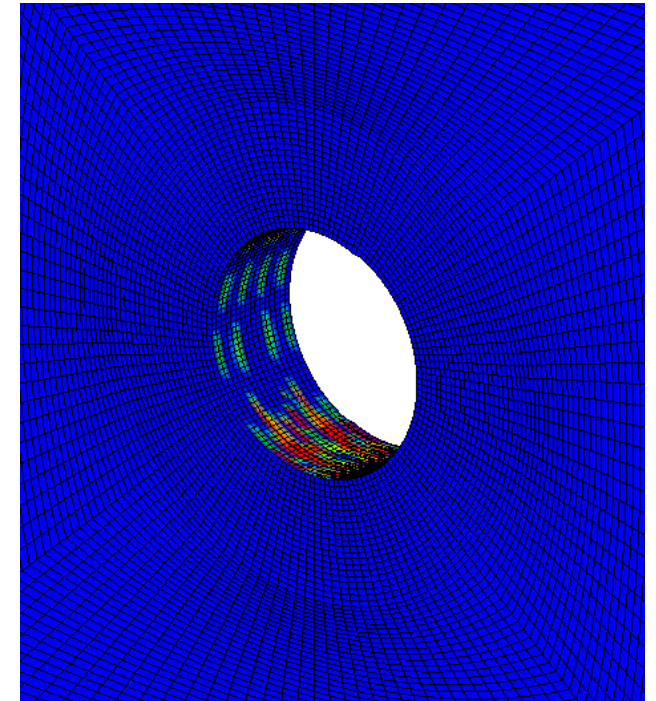
Ply #2/20 [0°/90°] N = 5,000





High-Fidelity Finite Element Analysis

Regularized Extended Finite Element Analysis (Rx-FEM)





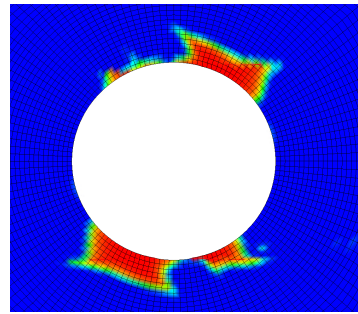
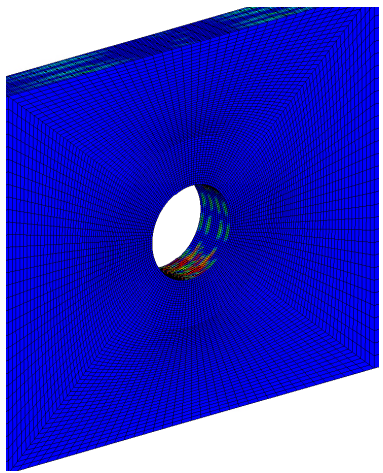
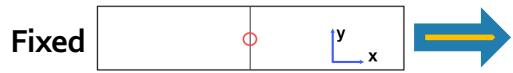
High-Fidelity Analysis

Delamination and open matrix cracks

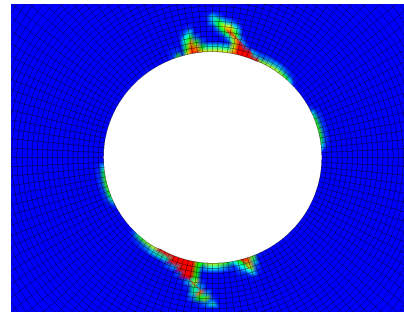
@ predicted failure strength of 375MPa

Mesh-independent regularized extended finite element modeling (Rx-FEM)

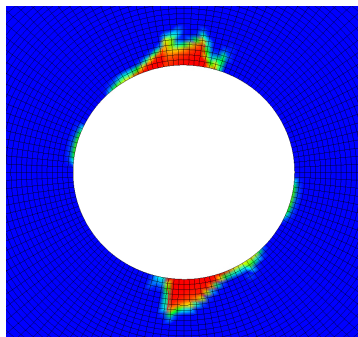
[45/90/-45/0/45/90/-45/0/0/-45/90/45/0/-45/90/45]



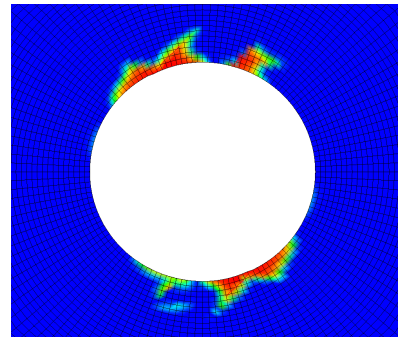
0° Ply 1



-45° ply 2



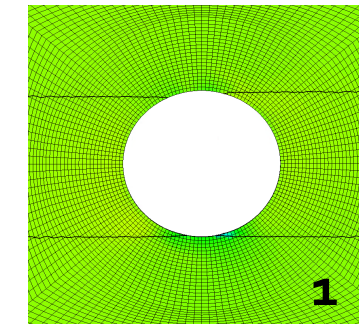
90° ply 3



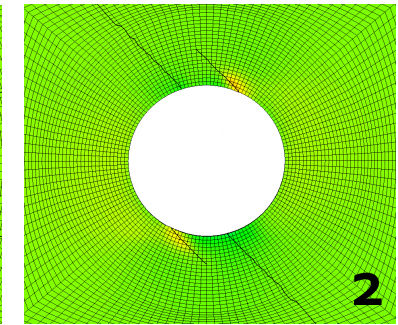
45° ply 4

1 2 3 4

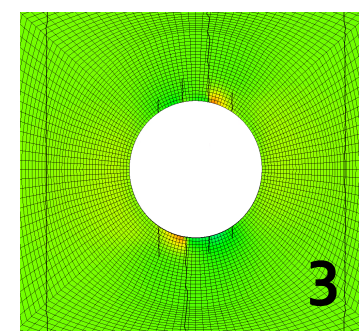
Potential "crack path" if crack continued



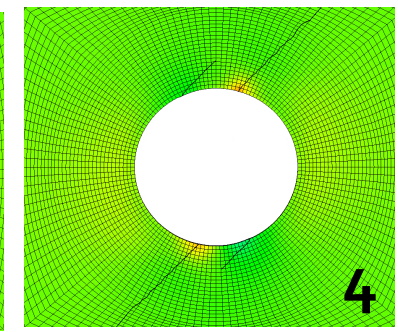
1



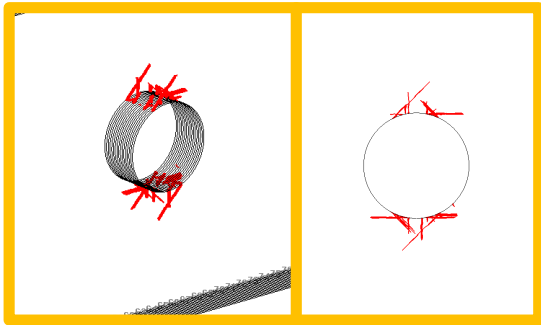
2



3



4



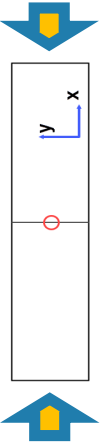
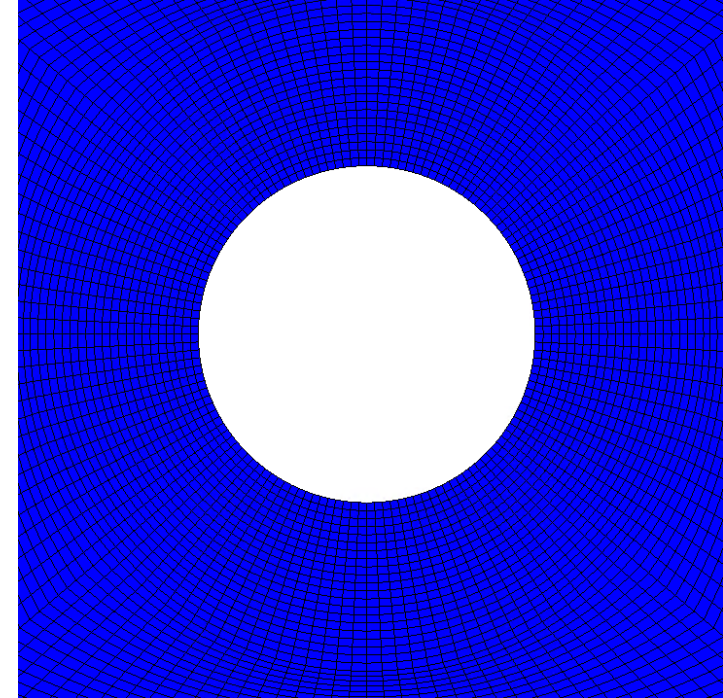
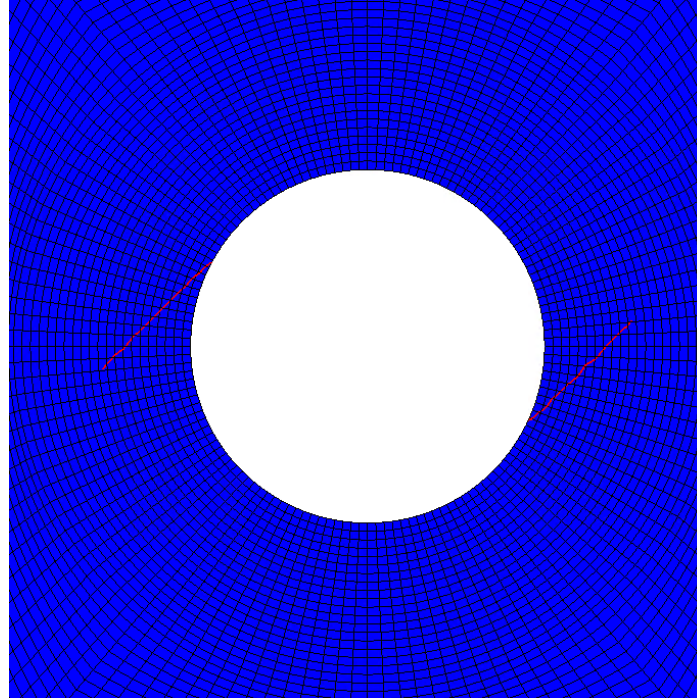
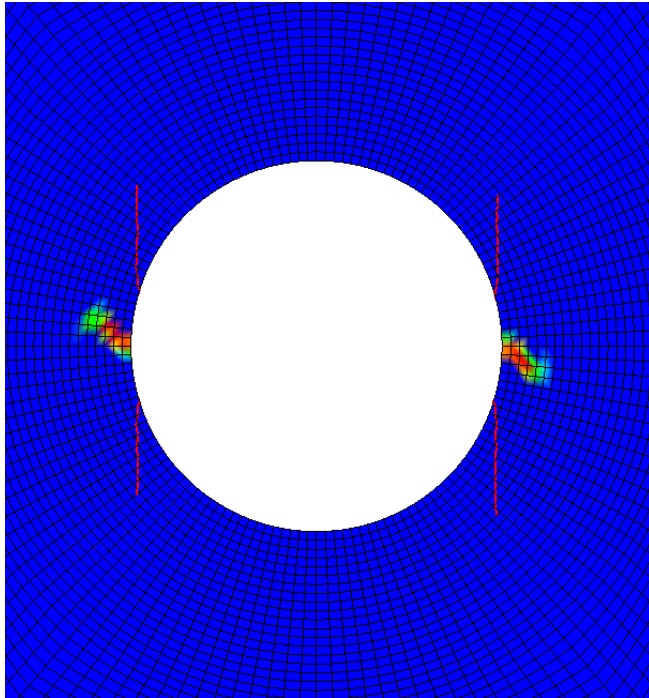


Rx-FEM - Matrix and Fiber Cracks in UNI OHC

0° ply

-45° ply

90° ply



Fiber break near hole on 0°

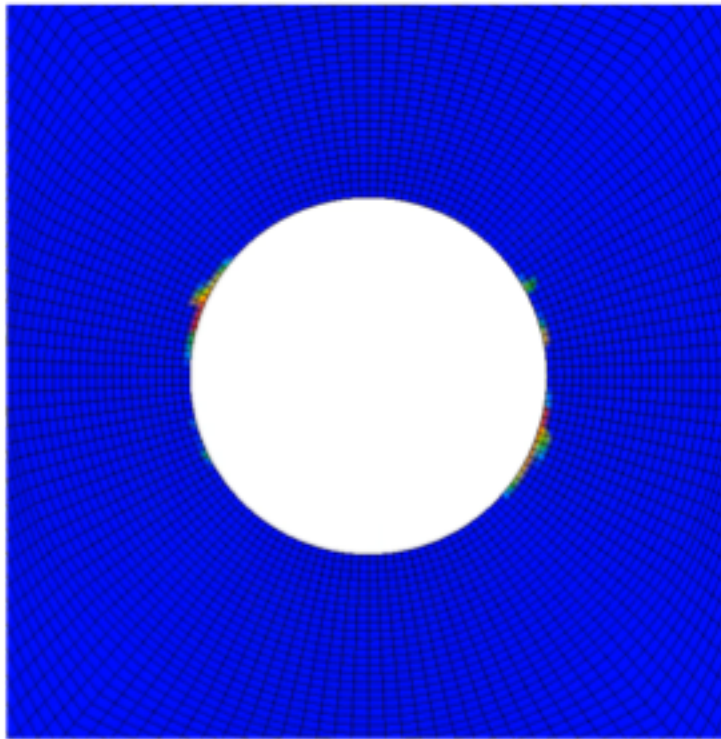
[45/90/-45/0/45/90/-45/0/0/-45/90/45/0/-45/90/45]





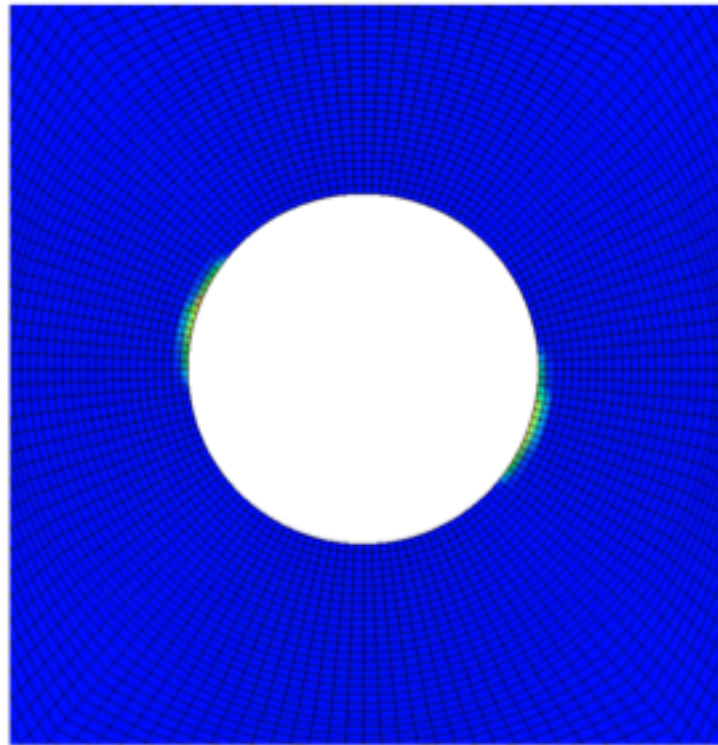
Rx-FEM - Delamination Propagation in UNI OHT

0° ply



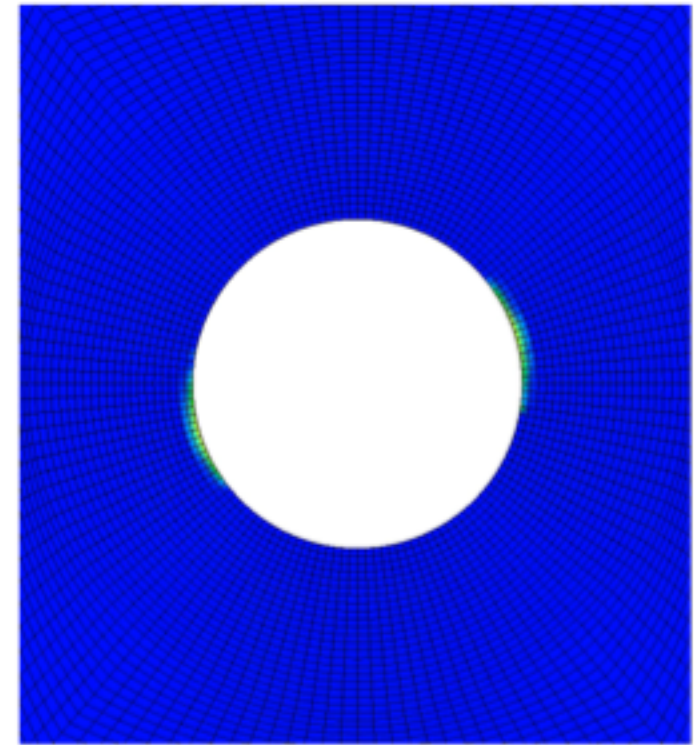
Delamination in 0/-45 interface

-45° ply



Delamination in -45/90 interface

90° ply



Delamination in 90/45 interface

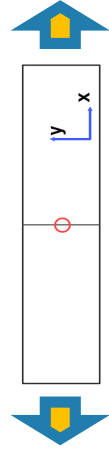
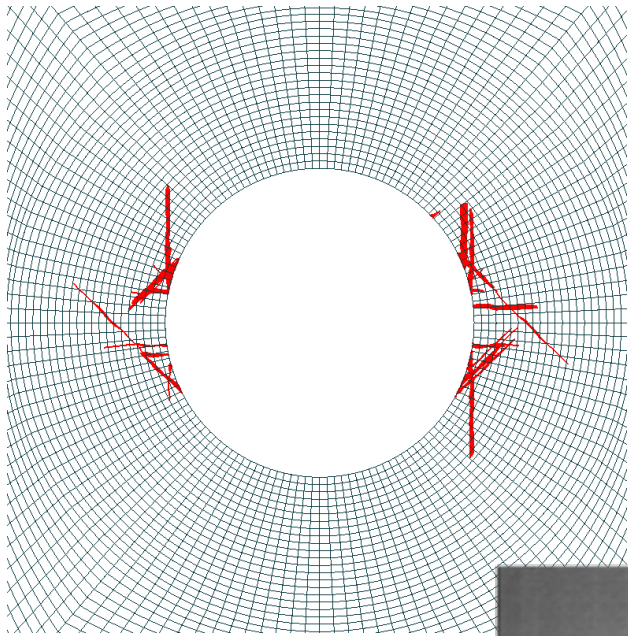
[45/90/-45/0/45/90/-45/0/0/-45/90/45/0/-45/90/45]



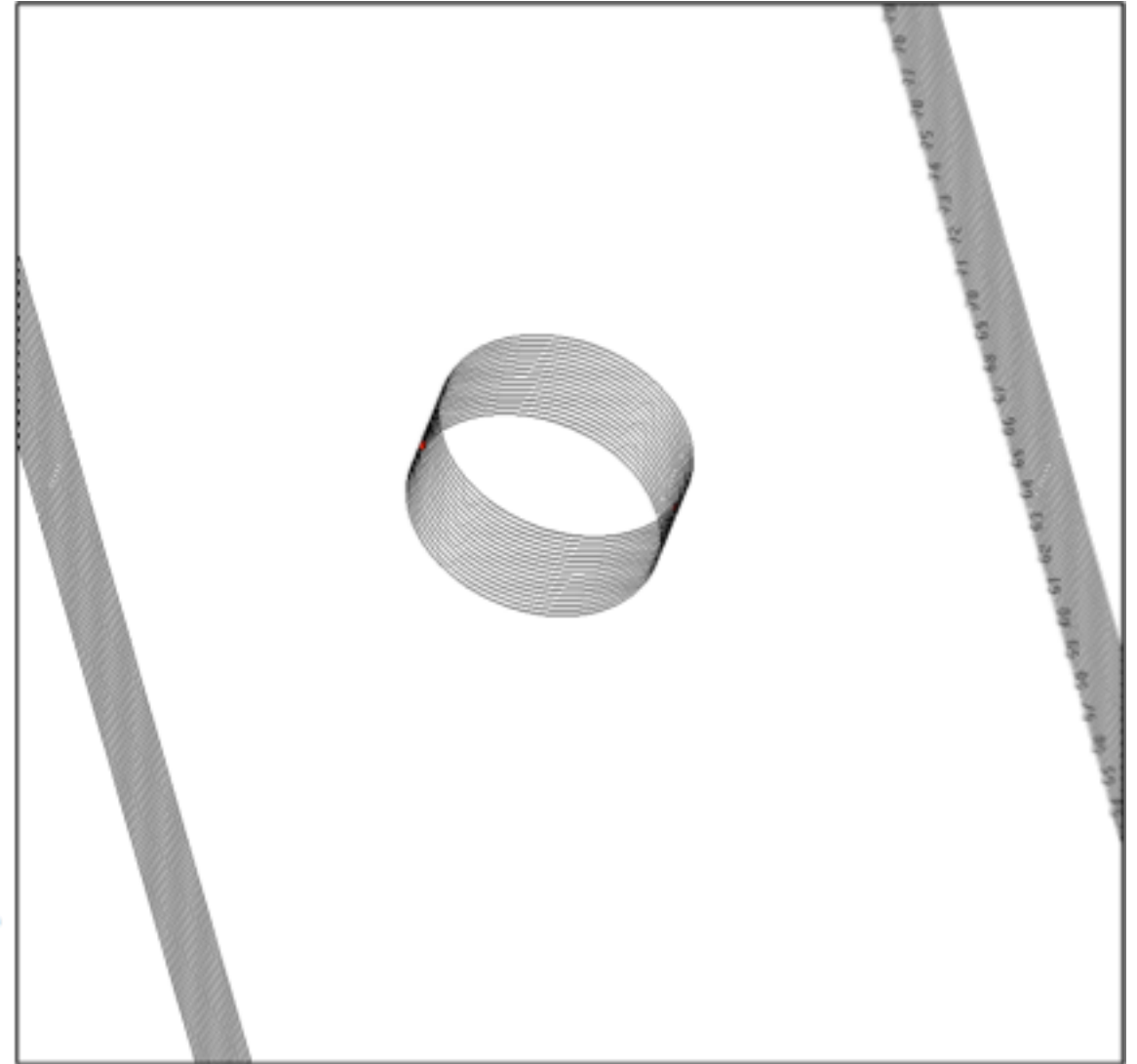
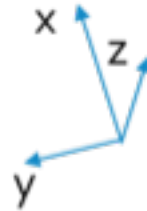
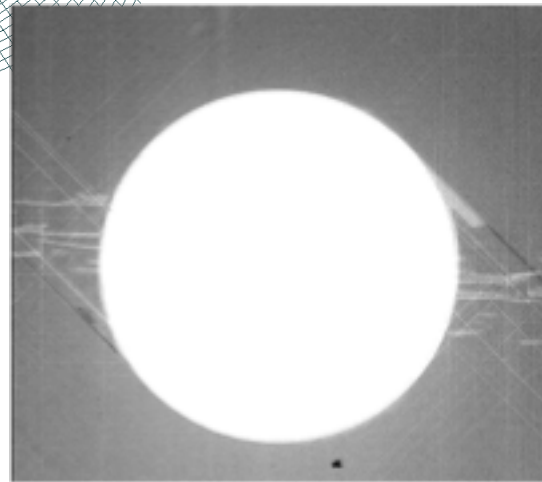
Fixed



Rx-FEM - Matrix Crack Growth in UNI OHT

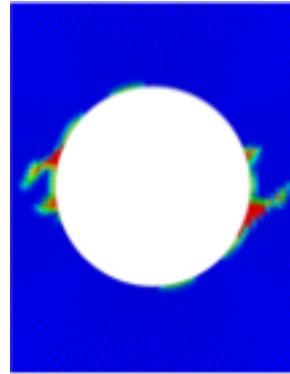
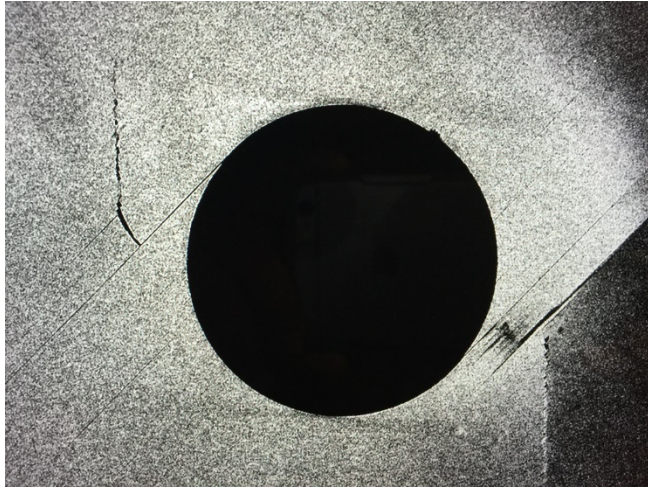


[45/90/-45/0]_{2S}





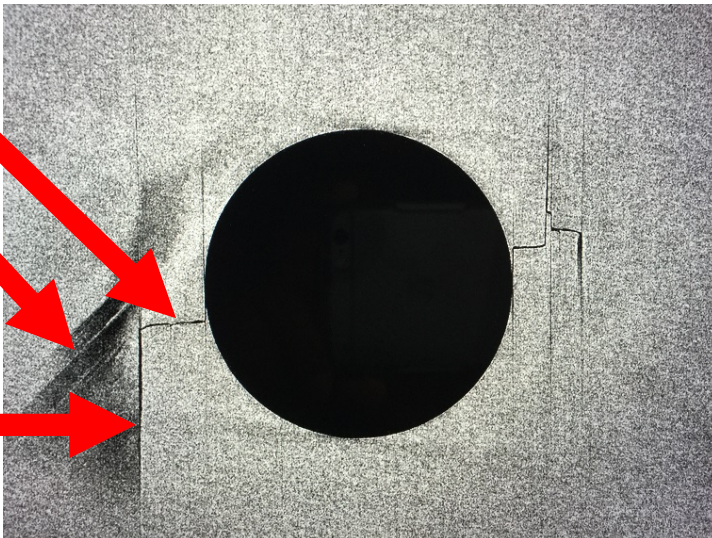
3D XCT UNI OH



Fiber Break
(Fiber Failure)

Delamination
(Interface Failure)

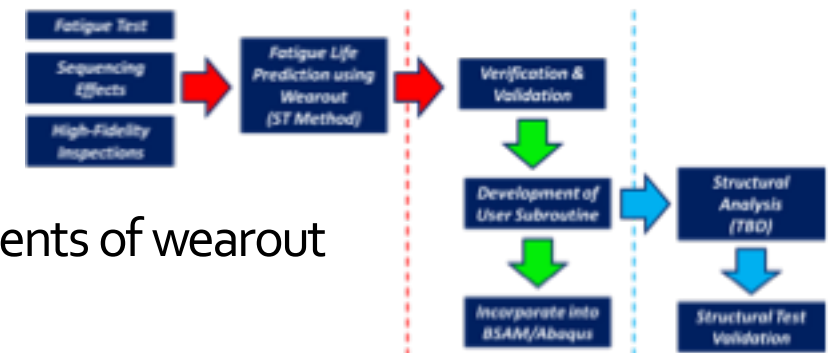
Fiber Splitting
(Matrix Cracks)





Summary - Strength Tracking (ST) Method

- Fatigue damage growth of composites under constant or variable amplitude (block/random) fatigue loading can be assessed
 - Can handle multiple R ratios
 - Sequencing effects will be incorporated
- Any validated residual strength degradation (wearout) model can be used
 - Sendeckyj wearout model is used for examples due to its robustness (ex., fitting curve for SN data provides an assessment of fitting parameters)
 - Incorporate reliability (analysis of fatigue data scatter)
 - Residual strength degradation for arbitrary stress levels
 - Simple Excel worksheet can be setup for life assessment
 - Provide opportunity to improve the technique for future developments of wearout models, both semi-empirical and analytical models

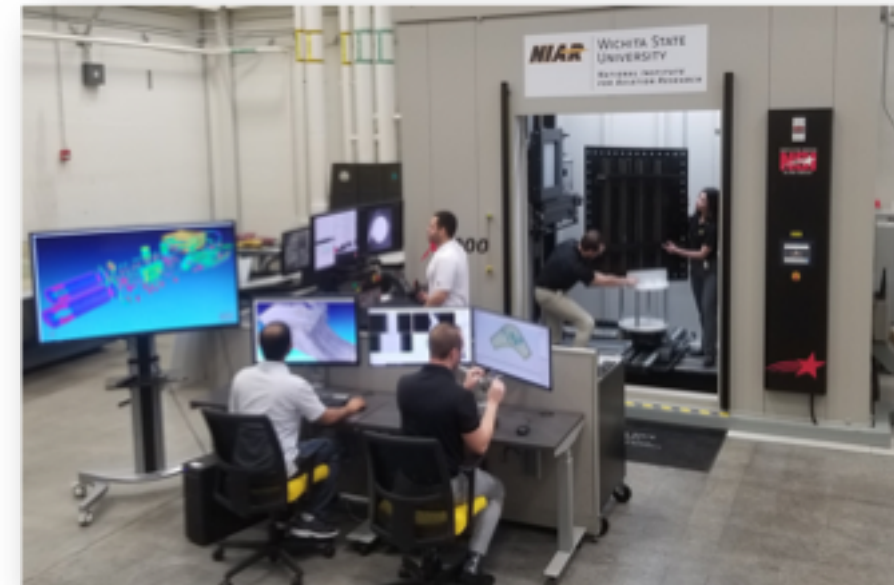




Summary – Damage Characterization (XCT)



- XCT system has significantly enhanced the research quality
 - Provided insight to interrogate internal defects/features of various material systems
 - Damage growth mechanics of advanced material systems under cyclic loading
 - Post-failure and accident investigation without sectioning
- Technique development is underway to enhance the quality of inspections
- Mimics software is used successfully for segmentation of various features from XCT reconstructions for analyses





Looking Forward

- **Benefit to Aviation**

- High-fidelity **database of fatigue damage growth characteristics** of composites under variable amplitude fatigue loading
- Development of **engineering tools** for determining the residual strength degradation and fatigue life under variable amplitude fatigue cycling

- **Future needs**

- Variable amplitude fatigue data for fatigue analysis and validation of wearout models for analytical life predictions
- Analytical models for predicting residual strength degradation (wearout)