

Failure of Notched Laminates Under Out-of-Plane Bending. Phase VI

Fall 2013 Meeting

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- Motivation and Key Issues

Develop analysis techniques useful in design of composite aircraft structures under out-of-plane loading (bending and shear)

- Objective

Determine failure modes and evaluate capabilities of current models to predict failure

- Approach

- Experiments: Mode 3 fracture
- Modeling: Progressive damage development and delamination (Abaqus) under Mode 3 fracture

Failure of Notched Laminates Under Out-of-Plane Bending. Phase VI

- Principal Investigators & Researchers
 - John Parmigiani (PI); OSU faculty
 - I. Hyder, N. Atanasov; OSU grad students
 - FAA Technical Monitor
 - Curt Davies
 - Lynn Pham
 - Other FAA Personnel Involved
 - Larry Ilcewicz
 - Industry Participation
 - Gerry Mabson, Boeing (technical advisor)
 - Tom Walker, NSE Composites (technical advisor)
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Project Overview

Phase I (2007-08)

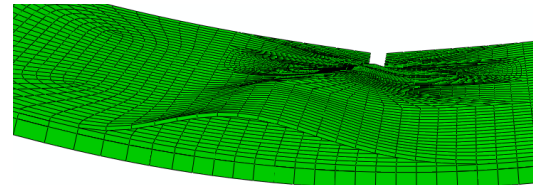
- Out-of-plane bending experiments w/composite plates
- Abaqus modeling with progressive damage

Phase II (2008-09)

- Abaqus modeling with buckling delamination added
- Sensitivity study of (generic) material property values

Phase III (2009-10)

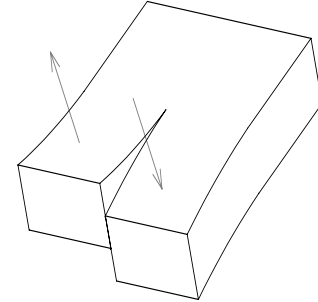
- Abaqus modeling w/ more delamination interfaces



Project Overview

Phase IV (2010-11)

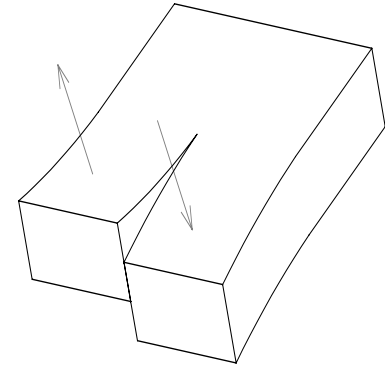
- Out-of-plane shear experiments
- Further study of additional delamination interfaces for out-of-plane bending
- Initiating vs. propagating toughness values for out-of-plane bending
- Feasibility of Abaqus/Explicit and XFEM for future work
- Sensitivity study using Boeing mat' l property values



Project Overview

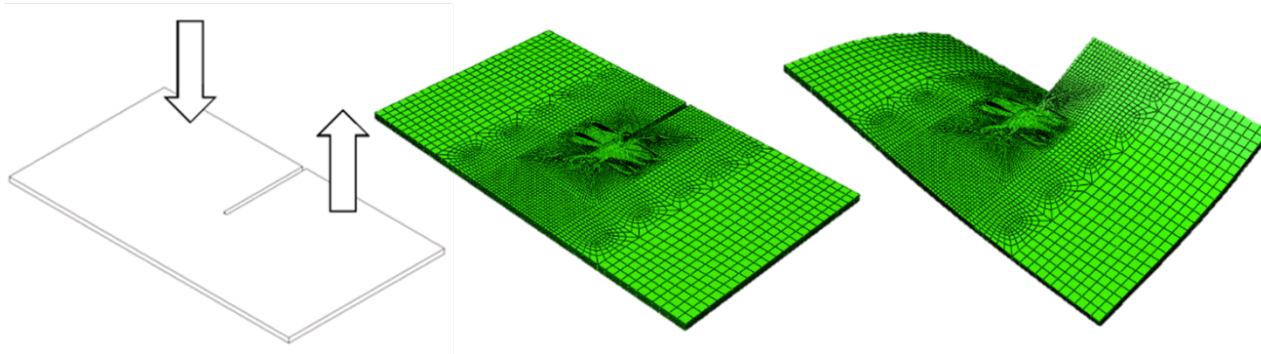
Phase V (2011-12)

- Complete Out-of-plane shear (mode III) experiments & begin preliminary Abaqus modeling
- Evaluate the Abaqus plug-in Helius:MCT (Firehole Composites) for use in modeling progressive damage in composites and applicability to this project – specifically for Out-of-plane bending



Phase VI (2012-13)

- Evaluation of Out-of-plane shear (mode III) modeling with built in capabilities of Abaqus Standard
- Evaluation of plug-in Helius: MCT (Firehole Composites) for mode III shear
- Evaluation for Abaqus Explicit for mode III shear



Today's Topics

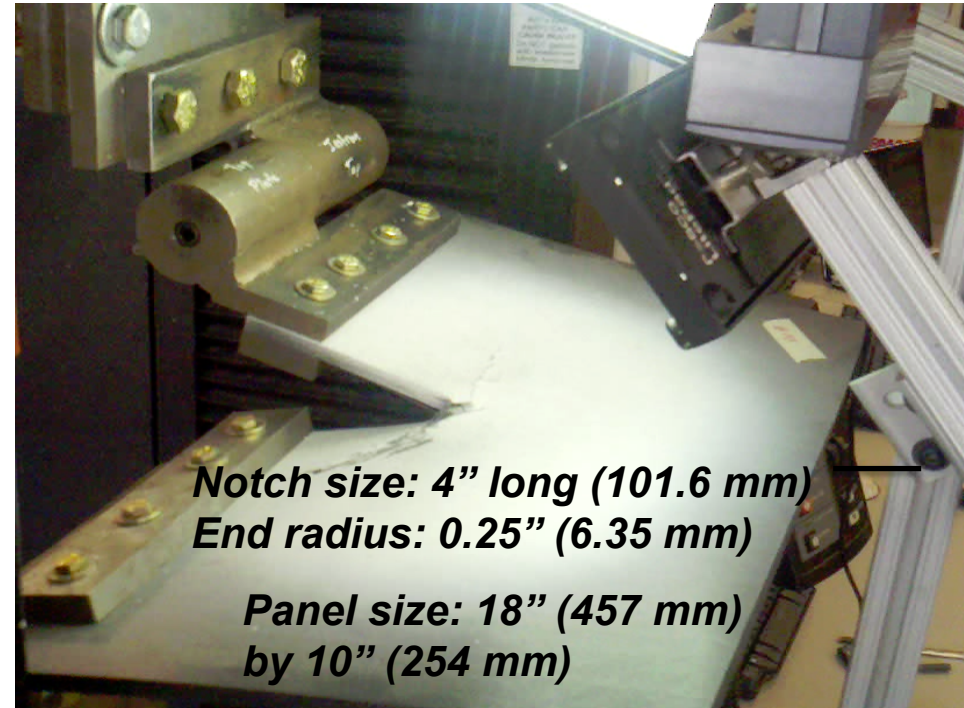
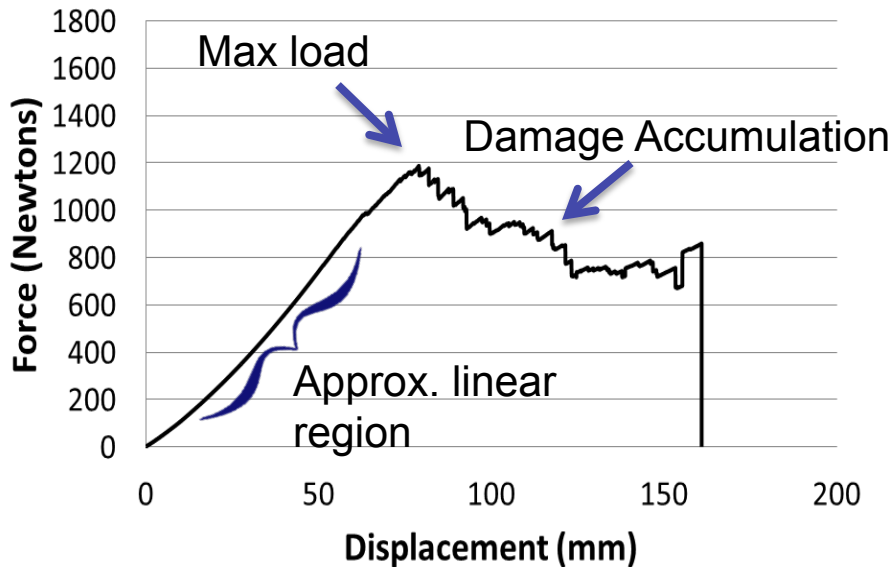
- Experimental results: Out-of-plane shear
- Evaluation of Abaqus Standard results
- Evaluation of Helius: MCT results
- Evaluation of Abaqus Explicit results

Today's Topics

- Experimental results: Out-of-plane shear
- Evaluation of Abaqus Standard results
- Evaluation of Helius MCT results
- Evaluation of Abaqus Explicit results

Out-of-Plane Shear: Summary of Experimental Results

20 Ply, 10% 0s - Average Experimental Load vs. Displacement Curve



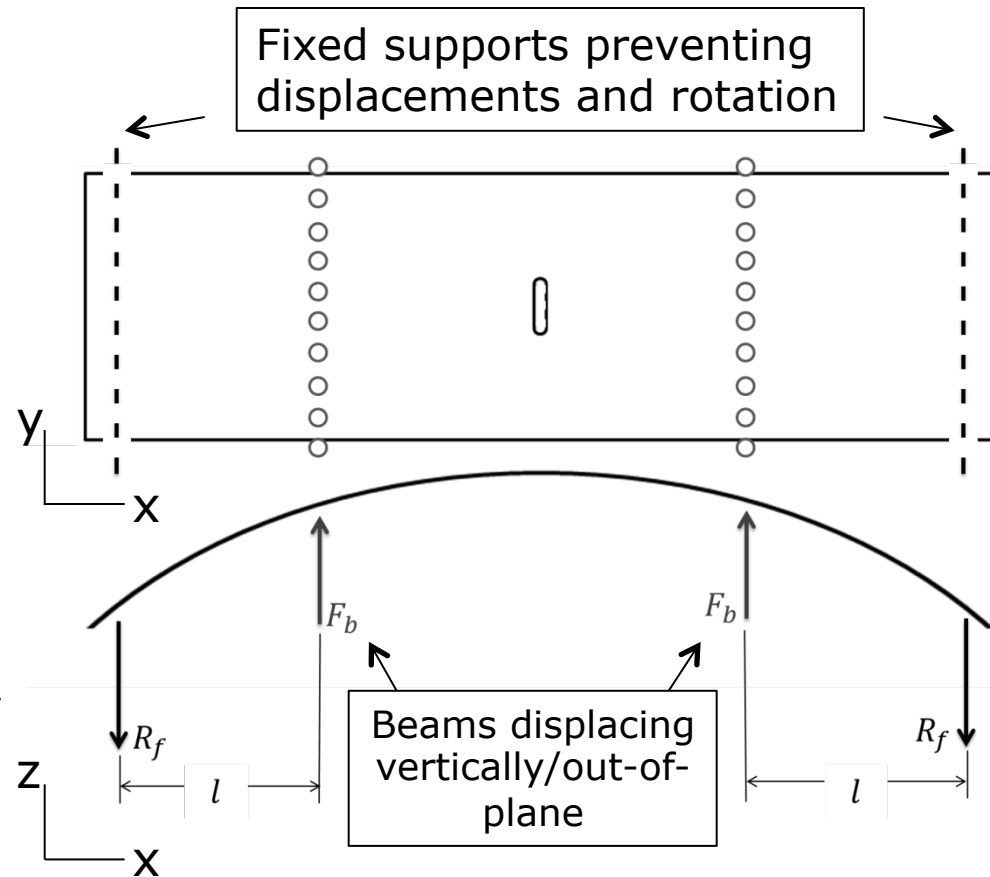
- Edge-notched CF panels displaced to maximum load
- 20 and 40 lamina thick panels with three lay ups: 10%, 30%, & 50% 0° plies
- Metrics: Applied displacement and applied load

Today's Topics

- Experimental results: Out-of-plane shear
- **Evaluation of Abaqus Standard results**
- Evaluation of Helius MCT results
- Evaluation of Abaqus Explicit results

Evaluation of Abaqus Standard: Previous Study with Out-of-plane Bending

- Selected mesh based on a linear elastic convergence study
- Created single layer and multilayer models
- VCCT interfaces around 0° plies for delamination (0° plies more critical)
- Agreed with experimental results within 10%
- Applied same procedure to Mode III/
 Out-of-plane shear

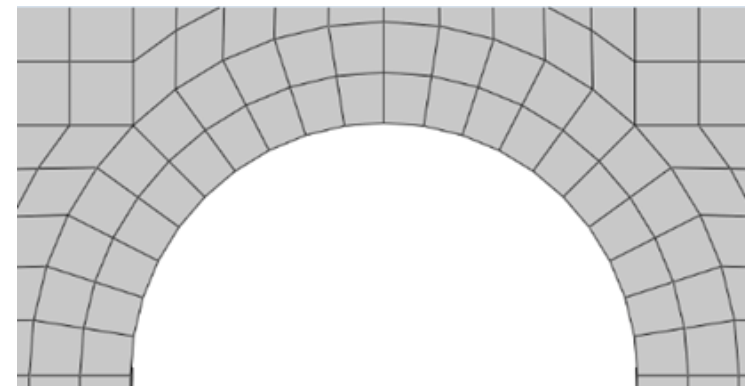
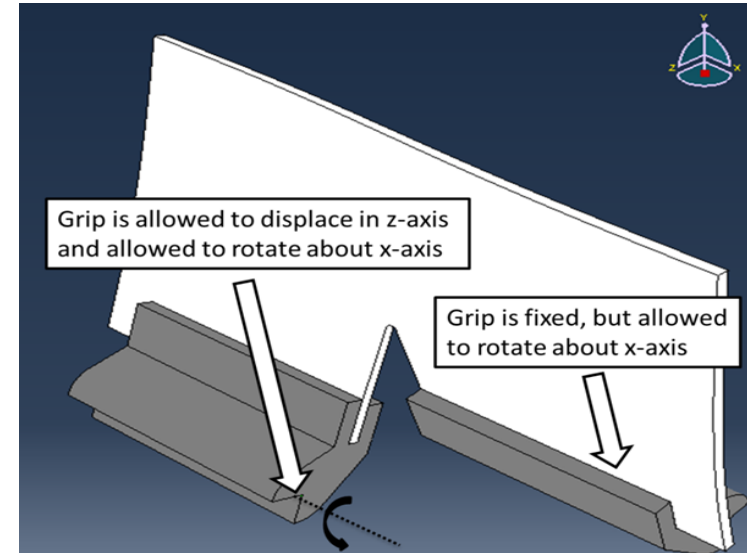


Evaluation of Abaqus Standard: Computational Model

- Solver basics:
 - Uses Newton-Raphson Technique to iterate to a converge solution for each time increment
 - Static equilibrium:

$$[K][U] = [R]$$

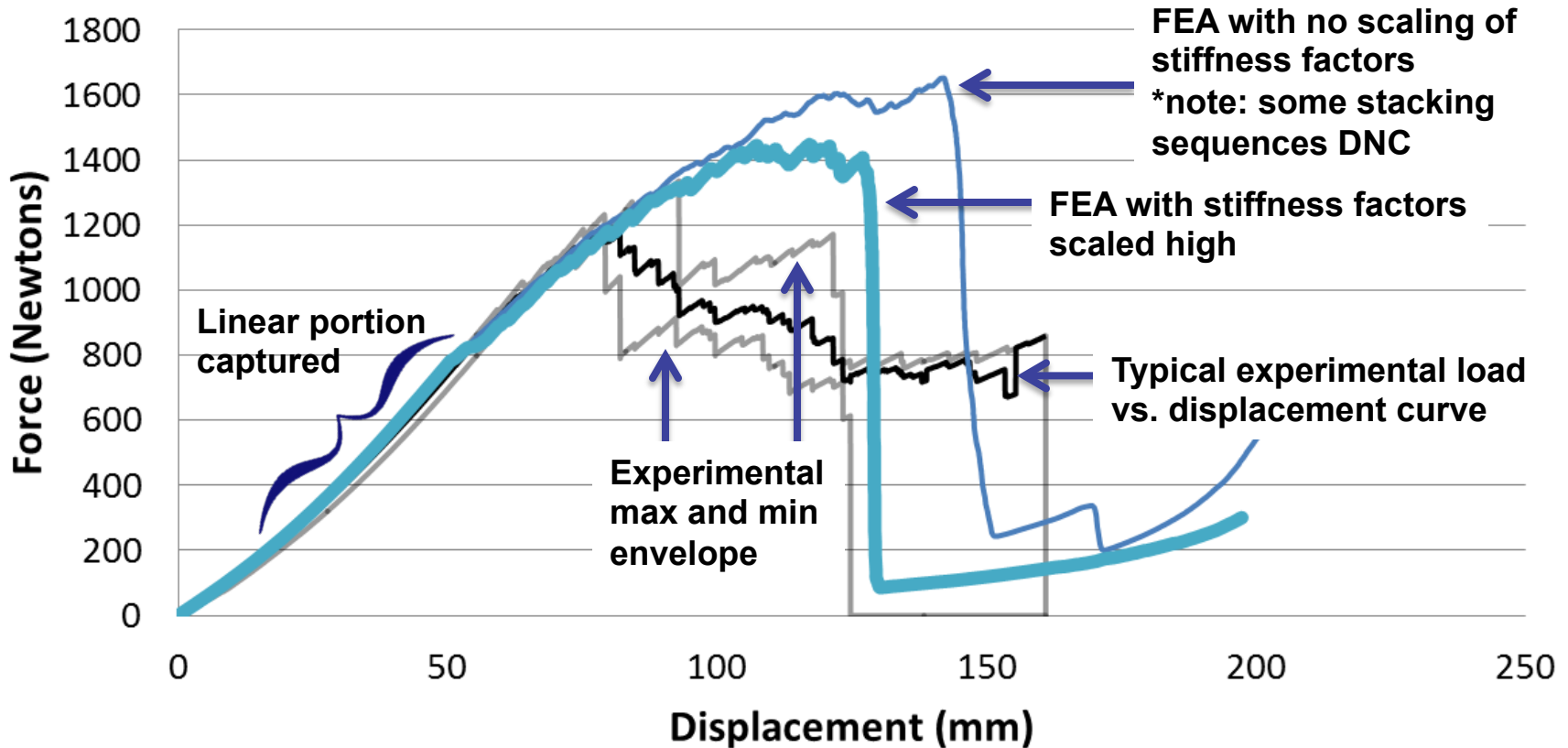
- Uses Hashin failure criteria
- Quasi-static analysis and Non-linear geometry turned on
- Panel: Continuum shell, reduced integration elements (SC8R)
- Grips: Continuum, 3-D, 8 node, reduced integration element (C3D8R)
- Boundary conditions implemented by grips
- Mesh Selection – 20 elements around notch tip, based on a linear elastic convergence study



- Viscous Regularization Scheme (used in standard/explicit) helps with convergence
 - Viscosity coefficients for fiber compression ($\eta \downarrow fc$), fiber tension ($\eta \downarrow ft$), matrix tension ($\eta \downarrow mt$), and matrix compression ($\eta \downarrow mc$)
 - Must be small with respect to the time increment, $t/\eta \downarrow i \rightarrow \infty$
 - Convergence trend at: $\eta \downarrow ft = \eta \downarrow fc = \eta \downarrow mt = \eta \downarrow mc = 0.0005$
- Hourglass stiffness scaled to prevent severe element deformation (Standard only)
 - Three hour glass scaling factors for displacement degree of freedom ($s \uparrow s$), rotational degree of freedom ($s \uparrow r$), and out-of-plane displacement degree of freedom ($s \uparrow w$)
 - Scaling to recommended values ($0.2 \leq s \uparrow s, s \uparrow r, s \uparrow w \leq 3.0$) didn't yield converged solutions for some stacking sequences in Standard
 - Needed to drastically increase factors, most models and stacking sequences converged

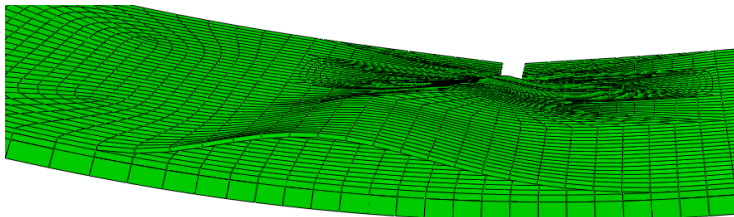
Evaluation of Abaqus Standard: Single Element Layer Results

20 Ply, 10% 0s - One Layer Model



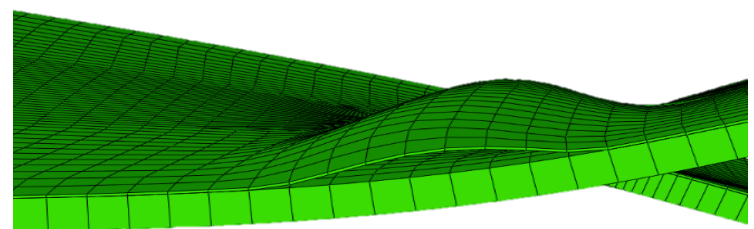
Evaluation of Abaqus Standard: Where to Insert VCCT Interfaces

Out-of-plane Bending



- 0° fibers going from left to right
- 0° plies would be most likely buckle/delaminate (experimentally verified)
- VCCT interfaces around 0° plies for delamination (0° plies more critical)

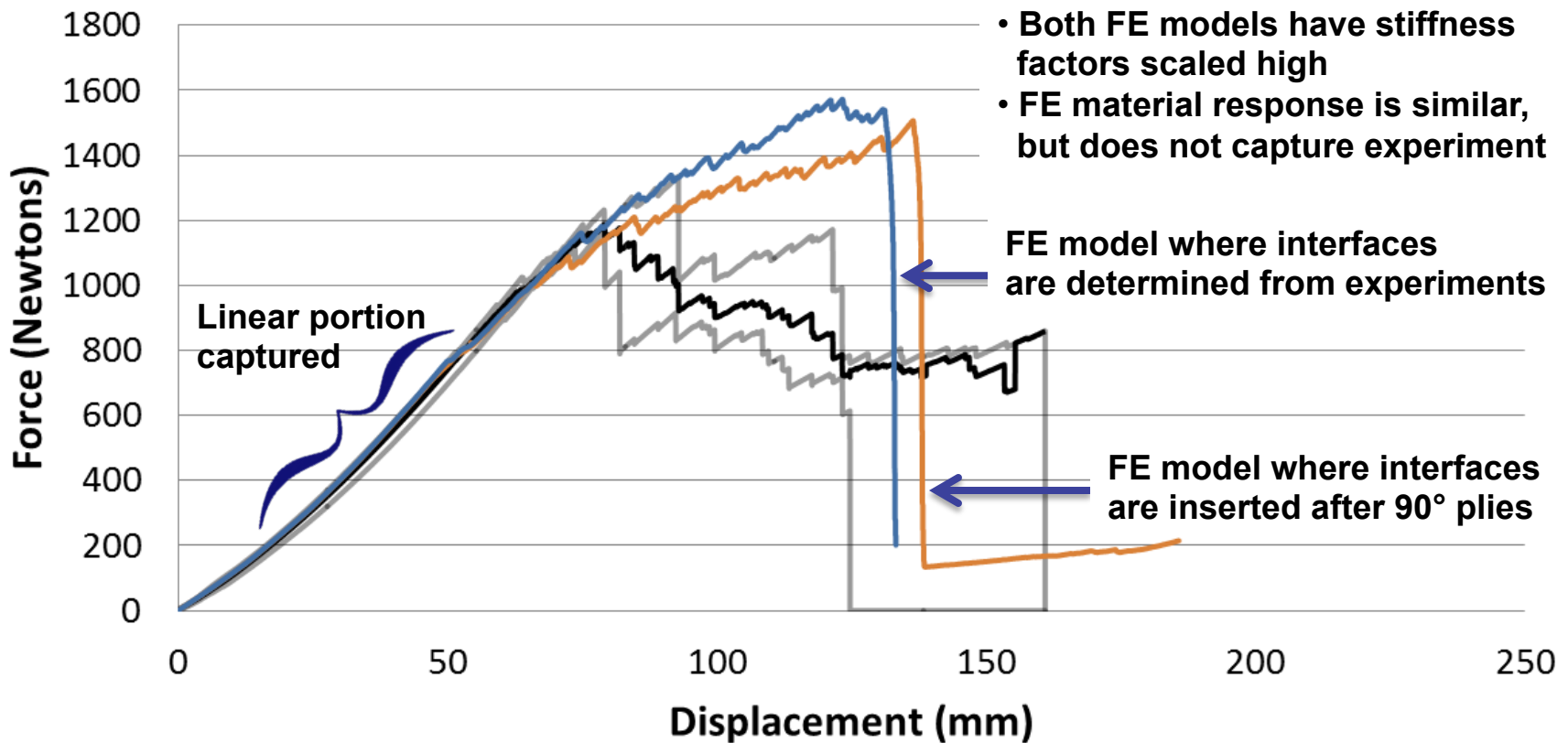
Out-of-plane Shear



- 90° fibers going from left to right
- 90° plies deemed likely to buckle/delaminate
- Delamination observed around 90° plies, but delamination on other interfaces observed as well
- Put VCCT interfaces after 90° plies and after experimentally observed delamination

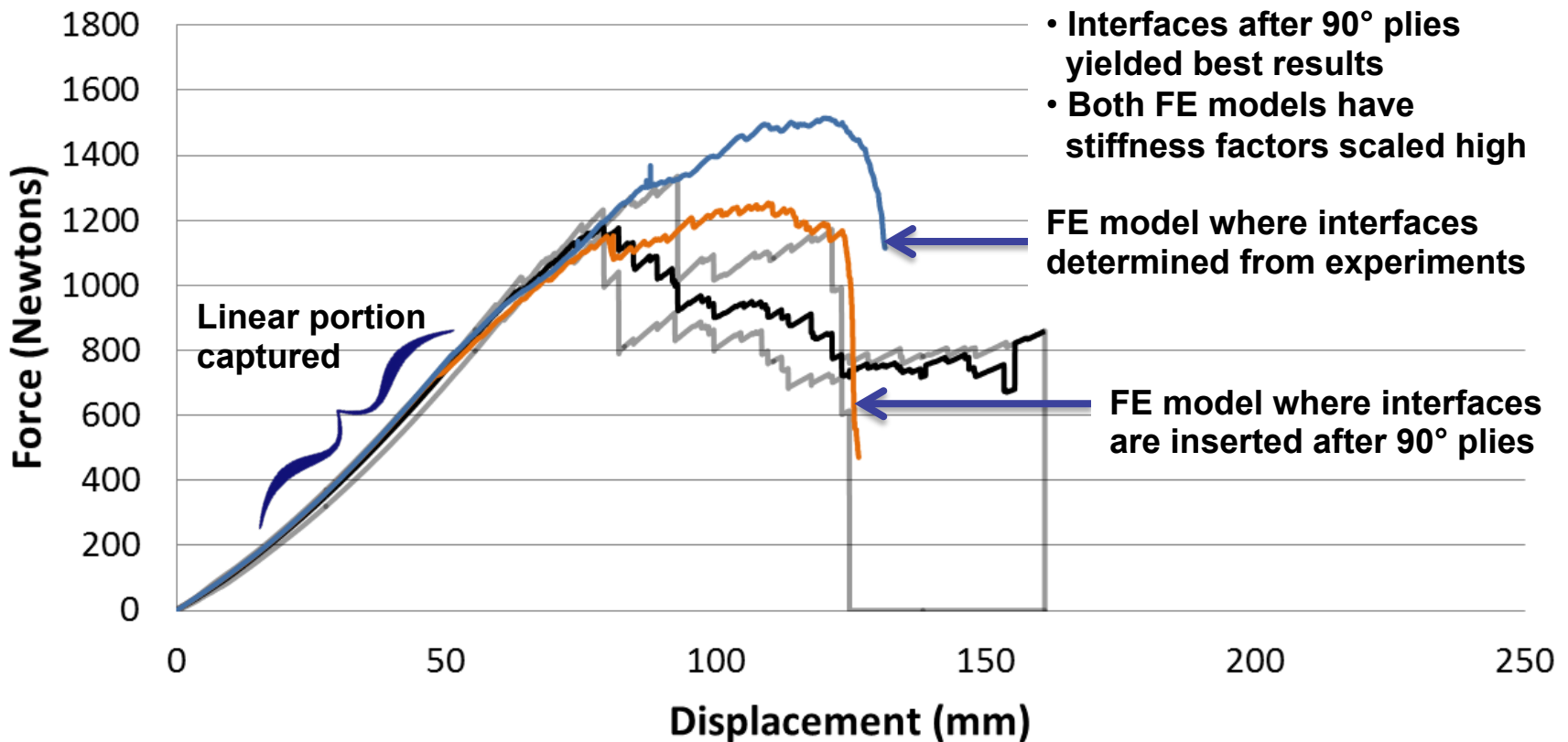
Evaluation of Abaqus Standard: Two Element Layer Delamination via VCCT Results

20 Ply, 10% 0s - Two Layer VCCT Model



Evaluation of Abaqus Standard: Three Element Layer Delamination via VCCT Results

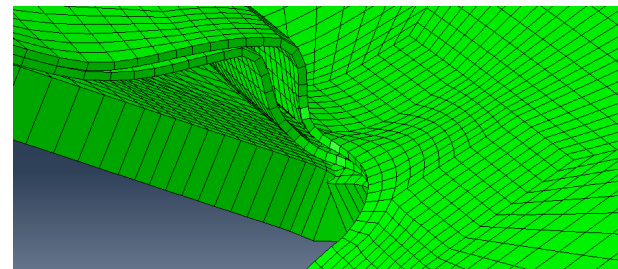
20 Ply, 10% 0s - Three Layer VCCT Model



Evaluation of Abaqus Standard: Summary of Results

- Benefit: Standard predicts max load within 20% of experiments
- Major Challenges:
 - Implicit analysis fails to converge without excessive stiffness factors
 - After the use of excessive stiffness factors, some models still fail to converge
- Suggestion:
 - Accuracy can be improved by changing VCCT interfaces – but no rational for it
 - Modify convergence parameters

		FEA % Difference from Average Experimental Maximum Load						
		% Zero	1 Element Layer - No Scaled Stiffness Factors (SSF)	1 Element Layer - with SSF	2 Element Layer VCCT with SSF - Interface from Experiments	2 Element Layer VCCT with SSF - Interface before 90° plies	3 Element Layer VCCT with SSF - Interface from Experiments	3 Element Layer VCCT with SSF - Interface before 90° plies
20 PLY	10%	10%	31%	15%	25%	20%	20%	-1%
	30%	30%	DNC	19%	21%	21%	DNC	18%
	50%	50%	-16%	-16%	-23%	-23%	DNC	DNC
40 PLY	10%	10%	45%	22%	DNC	18%	DNC	17%
	30%	30%	DNC	3%	-2%	-7%	42%	22%
	50%	50%	-3%	-5%	-4%	-4%	DNC	DNC



Today's Topics

- Experimental results: Out-of-plane shear
- Evaluation of Abaqus Standard results
- **Evaluation of Helius MCT results**
- Evaluation of Abaqus Explicit results

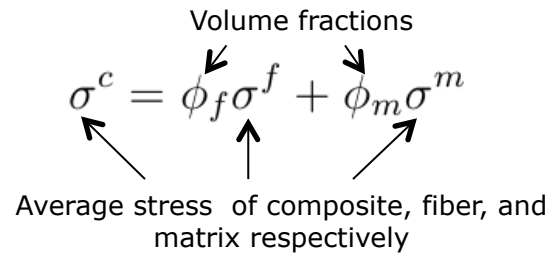
Abaqus/Standard with Helius:MCT

- Helius:MCT was utilized for its recognized convergence capabilities and fast solver algorithm for out-of-plane bending
- Solver basics: analyzes the composite based on its constituents as well as a whole:

$$\sigma^c = \phi_f \sigma^f + \phi_m \sigma^m$$

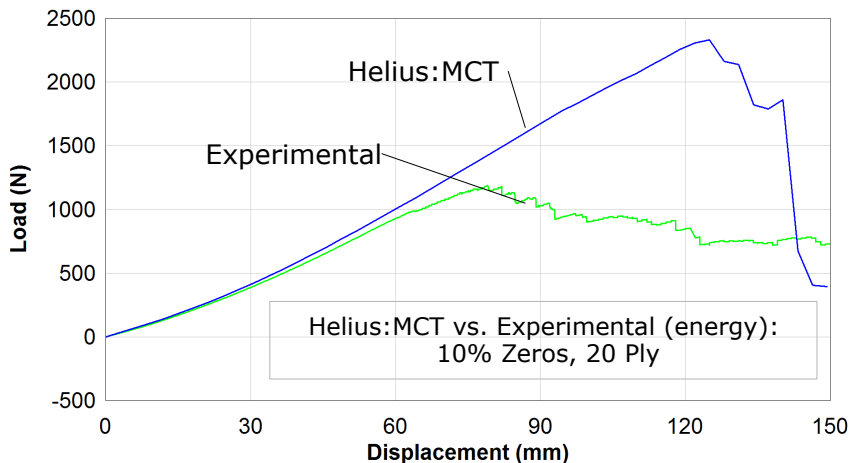
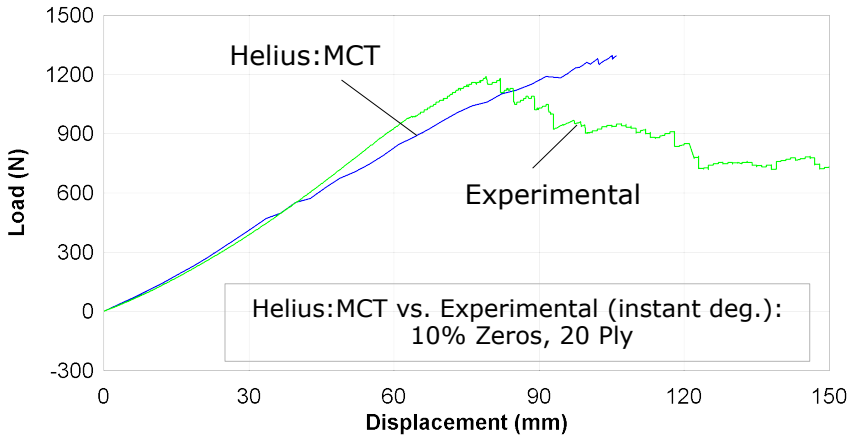
Volume fractions

Average stress of composite, fiber, and matrix respectively

The diagram shows the equation $\sigma^c = \phi_f \sigma^f + \phi_m \sigma^m$. Above the equation, the text "Volume fractions" has two arrows pointing down to ϕ_f and ϕ_m . Below the equation, the text "Average stress of composite, fiber, and matrix respectively" has three arrows pointing up to σ^c , σ^f , and σ^m .

- Method:
 - Adapt input file to include Helius:MCT solver
 - Use default parameters, instant degradation parameters, energy degradation parameters
 - Apply cohesive zones (CZ)

Abaqus/Standard with Helius:MCT



- Representative of all trials and configurations, including with CZ
- Benefits: fast solver: runtime < 10hrs
- Major challenges:
 - Convergence
 - Accuracy in certain situations
- Suggestions
 - Shows promise if convergence occurs, try different energy parameters or degradation values
 - Possible changes may occur in the future to better the solver: Autodesk ownership

Today's Topics

- Experimental results: Out-of-plane shear
- Evaluation of Abaqus Standard results
- Evaluation of Helius MCT results
- Evaluation of Abaqus Explicit results

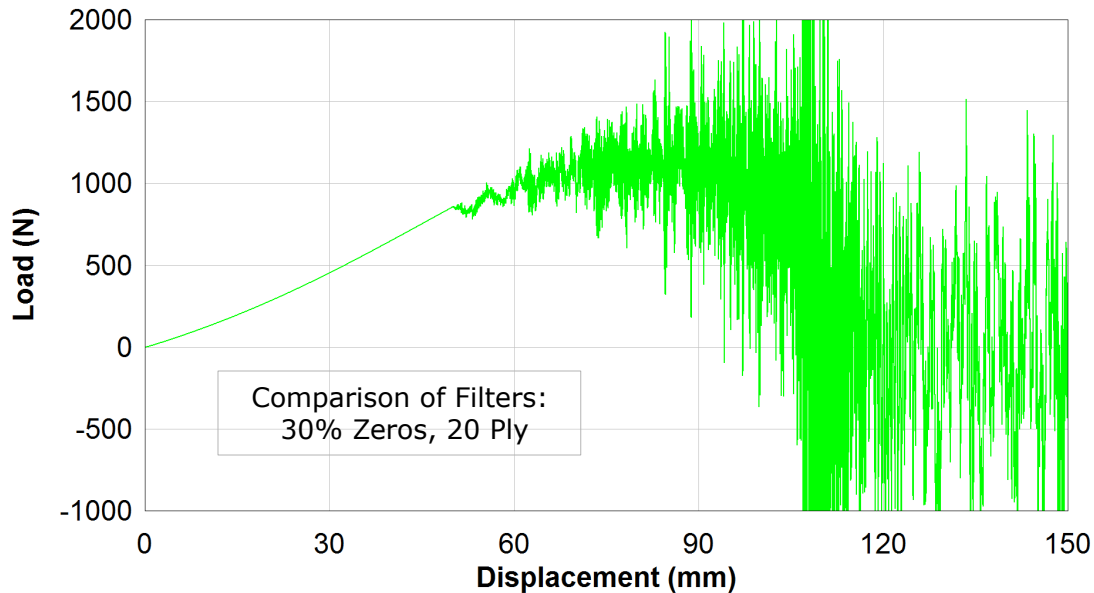
Abaqus/Explicit Analysis

- Why use explicit: implementation of element deletion and better convergence
- Solver basics:
 - Analysis used an explicit, dynamic solver:

$$[M][\ddot{U}] + [C][\dot{U}] + [K][U] = [R]$$

- Central difference method for enhanced convergence: hope to overcome the issues present in Abaqus/Standard
 - Hashin damage criteria
- Determination of quasi static state
 - Varied total time until a majority of analysis was quasi static: kinetic energy < 10% internal energy
 - Total time considered (seconds): 0.25, 0.50, 1.00, 2.00, 4.00, 6.00, 8.00
 - 8 seconds chosen as total time increment

Abaqus/Explicit Analysis: One Layer Results

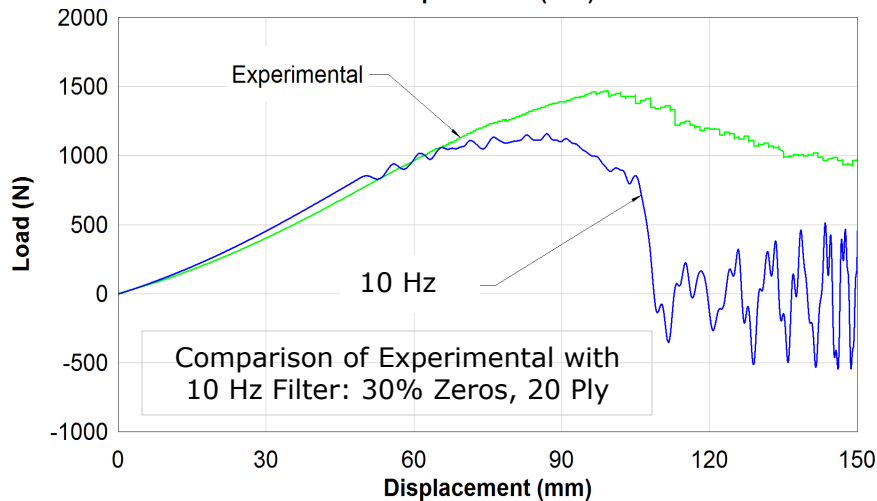
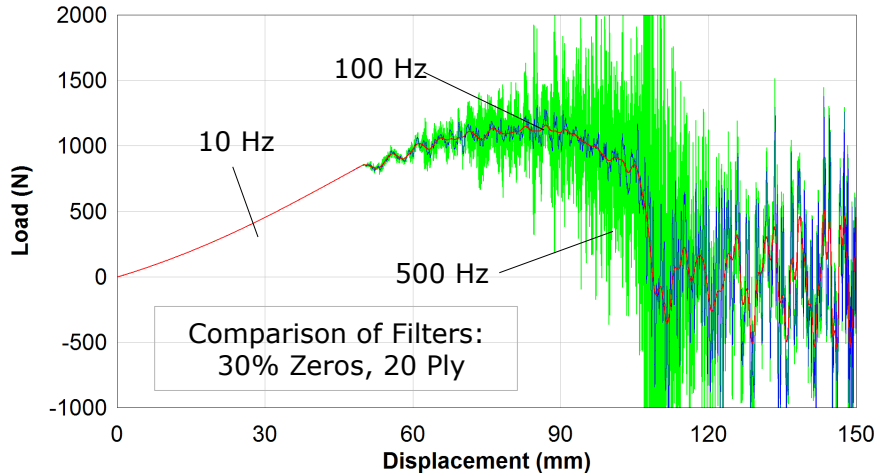


- Benefits: convergence in most cases
- Major challenges:
 - Extreme amounts of noise
 - Extremely long runtime
- Suggestions
 - Filtering the data
 - Implementing more layers

Abaqus/Explicit Analysis: Implementation of Filtering

- Dilemma: noise produced by the explicit solver possibly masks important information
- Solution: filter the load and displacement data
- Methods:
 - Determine natural frequency of model using Abaqus/Standard
 - Filter selected configuration as results are produced (pre-processing)
 - Apply additional filters after runs are complete (post-process)
 - 2nd order Butterworth filter

Abaqus/Explicit Analysis: Implementation of Filtering

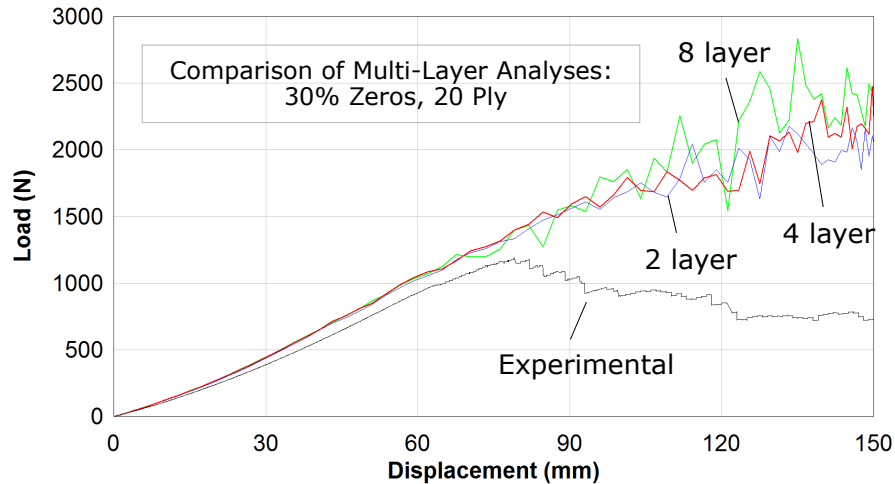


- Benefits: eliminates noise, presents a clearer picture of what is happening
- Major challenges:
 - Determining the cut-off frequency
 - Extremely large amounts of data, 10+ Gb per ODB file
- Suggestions
 - Method to determine the cut-off frequency
 - Determine what filter to apply
 - Would use method if confidence is higher

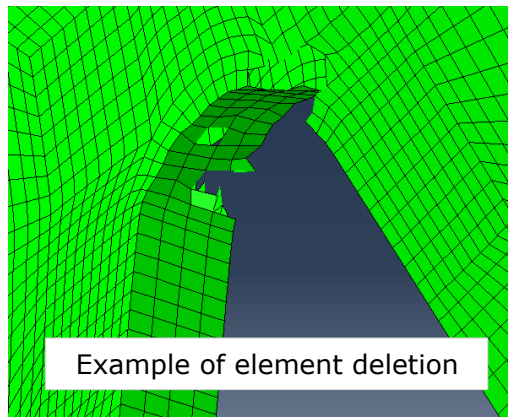
Abaqus/Explicit Analysis: Implementation of Multiple Layers and VCCT

- Dilemma: element deletion is not occurring
- Solution: create more layers so that the deletion criteria is met more readily
- Methods:
 - Create 2,4, and 8 layer models.
 - Varying degradation coefficient: 1.0,0.9,0.8,0.7
 - Implement VCCT

Abaqus/Explicit Analysis: Implementation of Multiple Layers



- Benefits: eliminate distorted elements
- Major Challenges:
 - Convergence
 - Extremely long run times
- Suggestion: not much can be gained overall from implementing multiple layers



Conclusions for Explicit Analysis

- Analyses are extremely long
- Analyses are inherently prone to noise during extreme deformations or accelerations. How do we appropriately filter this noise?
- Convergence is not guaranteed and element deletion may not always be something we can take advantage of.

Conclusion

- With Standard, it is possible to get max load predictions <20 % of experiments, however with major issues
 - Requires scaling convergence factors which produces excessively stiff elements
 - Some solutions still may not converge
- Helius: MCT has severe convergence issues
- Explicit can converge and can handle element deformation but other issues exist
 - Noisy solutions with damage
 - Extremely long run time
- Recommendations - Going beyond the built-in capabilities of Abaqus and Helius:MCT
 - Create a user defined element that can more effectively handle deformation
 - Create a user defined progressive damage criterion based on Tsai Wu, Tsai-Wu has shown to be more effective than Hashin Damage



Questions

Out-of-Plane Shear: Summary of Experimental Results

- Maximum applied load (failure load)

	Max Force per Test [kN]						
Layup (#plies / % zero degree)	1	2	3	4	5	6	MEAN
40/50%	5.552	5.345	5.122	6.103	5.395	5.321	5.473
40/30%	5.342	5.363	6.061	5.616	6.176	5.690	5.708
40/10%	3.891	4.161	4.112	4.016	4.277	4.148	4.101
20/50%	1.751	1.859	1.929	1.691	1.740	1.801	1.795
20/30%	1.484	1.541	1.541	1.456	1.527	1.638	1.531
20/10%	1.290	1.215	1.258	1.254	1.198	1.336	1.259

Why Continuum Shell Elements vs. Solid Elements

- Solid elements can be laminated but max order of variation of the displacement is quadratic
 - Hence strain variation is at most linear
 - Insufficient to model variation of strain through thickness of laminate
 - Potential Solution: stack solid elements at one element per lamina
 - In-plane dimensions can not be $> 10x$ thickness
 - Requires a really fine mesh
 - Alternate Solution: Use continuum shell elements
 - Does not have the same problems as a solid element
 - Can have multiple plies through the thickness
 - Also can be stacked for using with grips and delamination
 - Laminate stacking sequence was constructed using Composite Layup in Abaqus – define material prop' per ply
-

Viscous Regularization Scheme

- The viscous regularization scheme helps a model come to a converged solution
- Viscous coefficient must be small with respect to the time increment, $t/\eta \downarrow i \rightarrow \infty$
- Four viscous coefficients for each damage mode that needs to be user specified

η_{fc}	Viscosity Coefficient for Fiber Compression
η_{ft}	Viscosity Coefficient for Fiber Tension
η_{mc}	Viscosity Coefficient for Matrix Compression
η_{mt}	Viscosity Coefficient for Matrix Tension

Viscous Regularization Scheme Cont...

- How to determine $\eta \downarrow ft$, $\eta \downarrow fc$, $\eta \downarrow mt$, $\eta \downarrow mc$?
 - Set terms to relatively high values to get model convergence
 - For this study, $\eta \downarrow ft = \eta \downarrow fc = \eta \downarrow mt = \eta \downarrow mc$
 - Parameters were decreased until maximum load prediction did not change dramatically
 - This yielded a starting point in determining appropriate values for viscous coefficients
-

Scaling Hourglass Stiffness

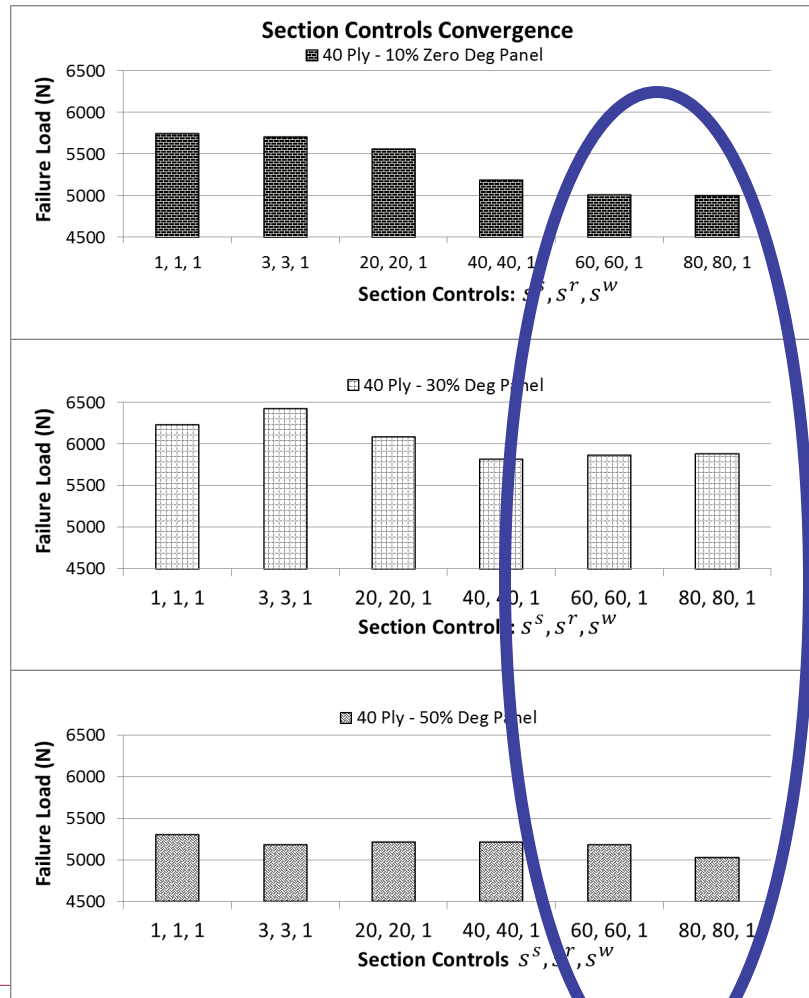
- Default hourglass stiffness was scaled to prevent severe element deformation
- Pure stiffness approach was recommended for quasi-static analysis
- Three user defined scaling factors

Factor	Description	Typical Range
$s\uparrow s$	Hour glass stiffness scaling factor for displacement degree of freedom	0.2 - 3.0
$s\uparrow r$	Hour glass stiffness scaling factor for rotational degree of freedom	0.2 - 3.0
$s\uparrow w$	Hour glass stiffness scaling factor for out-of-plane displacement degree of freedom	0.2 - 3.0

Scaling Hourglass Stiffness Cont

- Scaling $s \uparrow w$ caused solutions to fail prematurely
 - Only scaled $s \uparrow s$ and $s \uparrow r$
 - After scaling to the limits of the recommended value, not all stacking sequences converged
 - After drastically increasing factors, convergence was achieved for most models
 - Factors were selected based on a convergence study
-

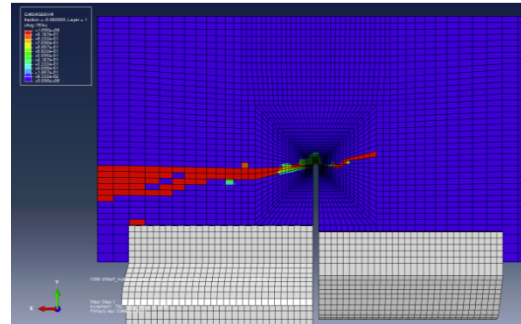
Scaling Hourglass Stiffness Cont



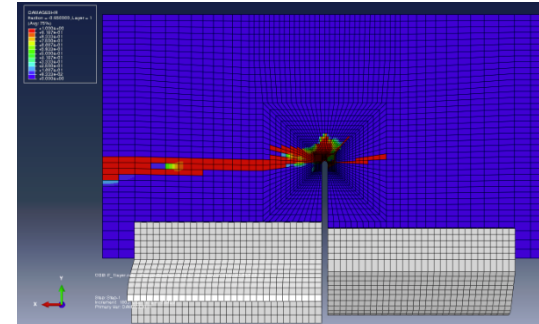
- Begin to see a converging trend at $s^s=60, s^r=60, s^w=1$
- This is consistent between the three stacking sequences

Damage Path Model

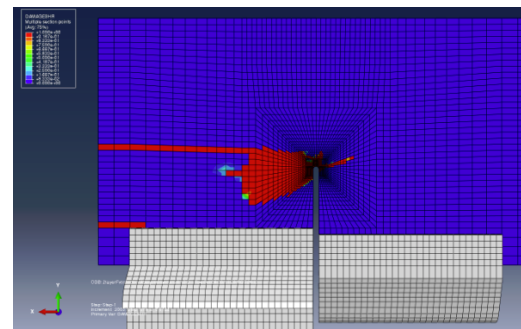
1 Layer – No SSF



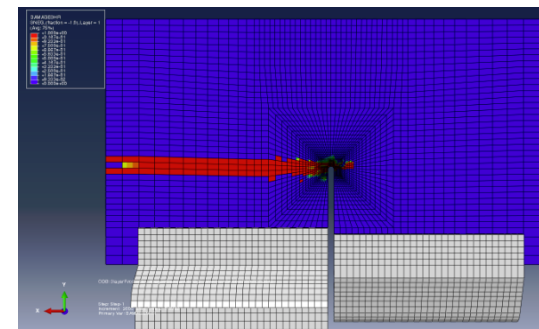
1 Layer – with SSF



2 Layer – VCCT



3 Layer – VCCT



Results Table: Explicit and Helius:MCT

Energy (Given)					Instant Degradation (Given)				
Combo	MCT (N)	Exp. (N)	% Diff	Converge	Combo	MCT (N)	Exp. (N)	% Diff	Converge
F	2330.83	1188	65.0	Y	F	1296.9	1188	8.8	N
N	2377.34	1689	33.9	Y	N	1184.99	1689	35.1	N
P	2598.69	1472	55.4	Y	P	1388.43	1472	5.8	Y
AN	9785.4	5111	62.8	N	AN	4989.86	5111	2.4	N
FP	9278.33	4005	79.4	Y	FP	5104.25	4005	24.1	N
AR	7394.08	5899	22.5	Y	AR	6528.27	5899	10.1	N
					Cohesive Zones (Given - Instant)				
					Combo	MCT (N)	Exp. (N)	% Diff	Converge
Instant Degradation (Default)					F	713	1188	50.0	N
Combo	MCT (N)	Exp. (N)	% Diff	Converge	N	996	1689	51.6	N
F	1254	1188	5.4	N	P	838	1472	54.8	N
N	1514	1689	10.9	N	Abaqus/Explicit: Filter				
P	1624	1472	9.9	N	Combo	Explicit (N)	Exp. (N)	% Diff	Converge
AN	5182	5111	1.4	N	F	1291	1188	8.3	Y
FP	4817	4005	18.4	N	N	928	1689	58.1	Y
AR	6528	5899	10.1	N	P	1158	1472	23.8	Y

Legend: Y = Yes, N=No, Exp. = Experimental Values, MCT= Helius:MCT results

F= 10% zeros, 20 ply ; P = 30% zeros, 20 ply ; N=50% zeros, 20 ply ; FP = 10% zeros, 40 ply ; AR = 30% zeros, 40 ply ; AN = 50 % zeros, 40 ply

Helius:MCT Results – Boeing Parameters (Energy Degradation)

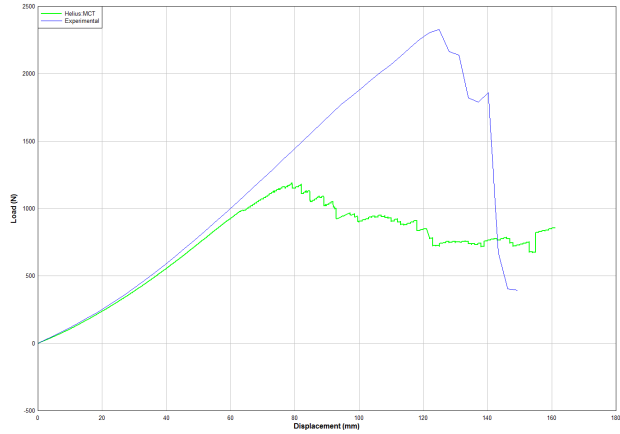


Fig 1. F Configuration

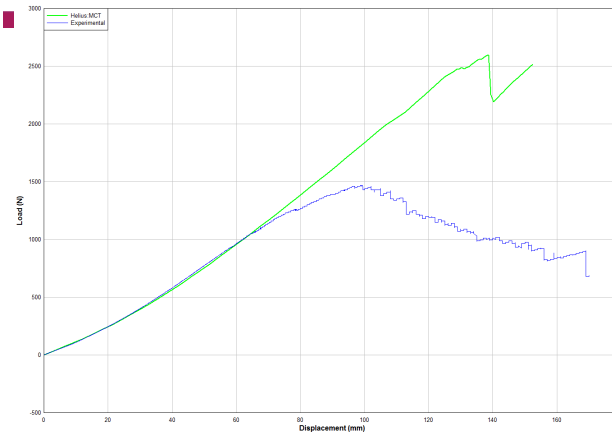


Fig 2. P Configuration

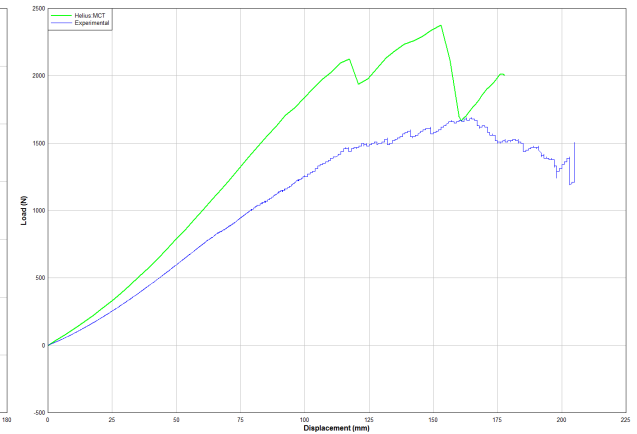


Fig 3. N Configuration

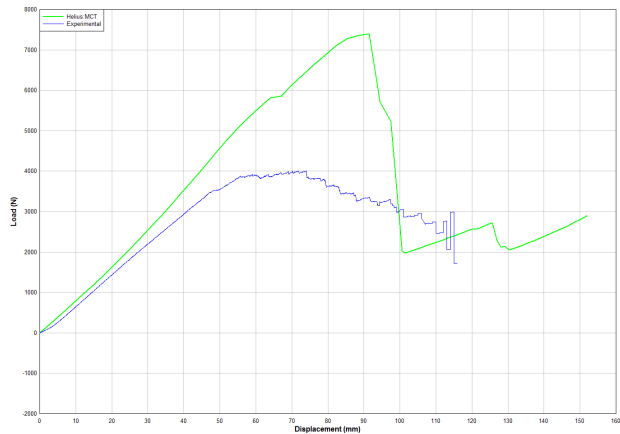


Fig 4. FP Configuration

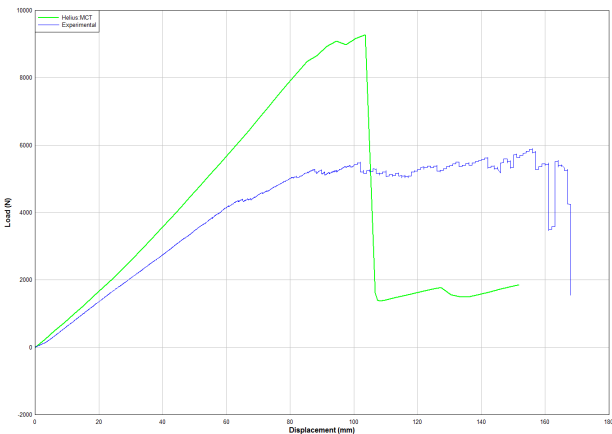


Fig 5. AR Configuration

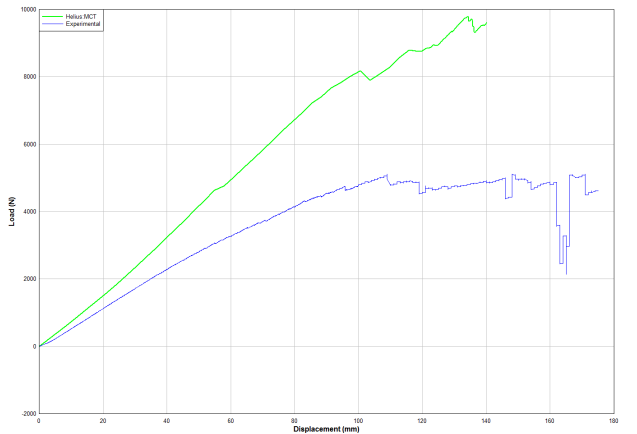


Fig 6. AN Configuration

Helius:MCT Results – Boeing Parameters (Instant Degradation)

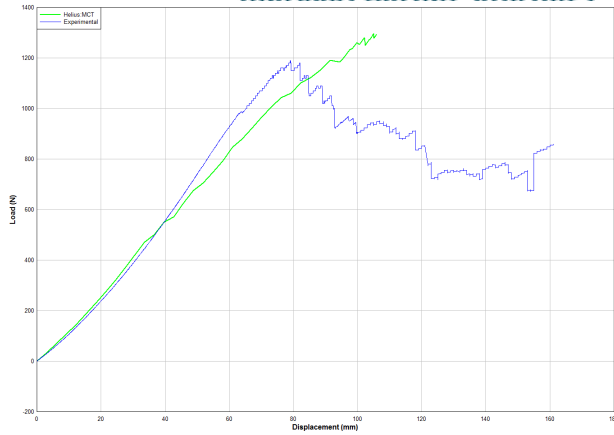


Fig 1. F Configuration

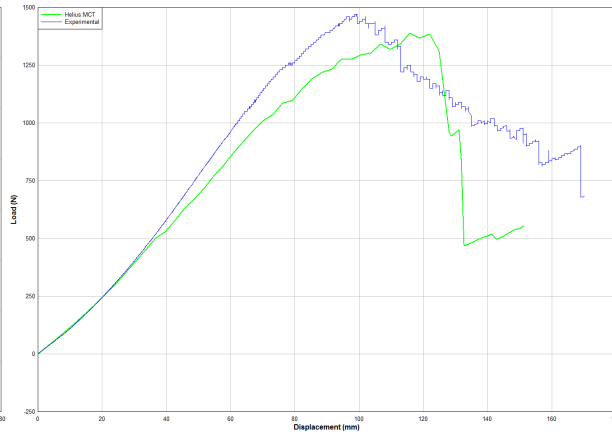


Fig 2. P Configuration

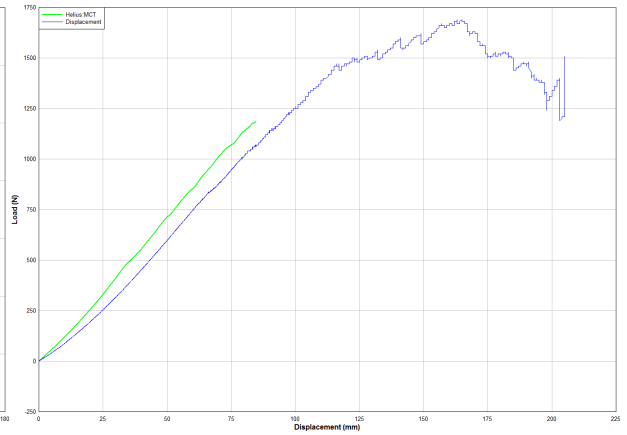


Fig 3. N Configuration

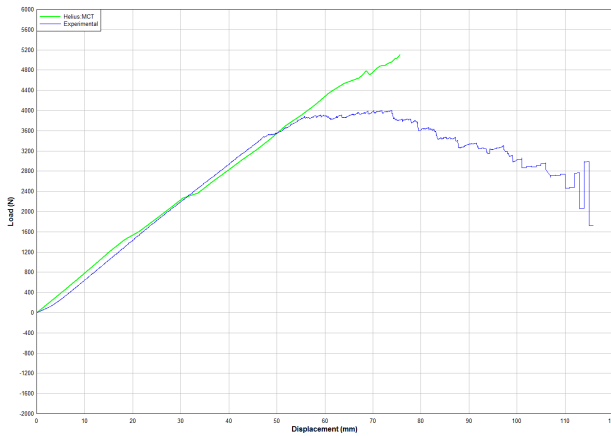


Fig 4. FP Configuration

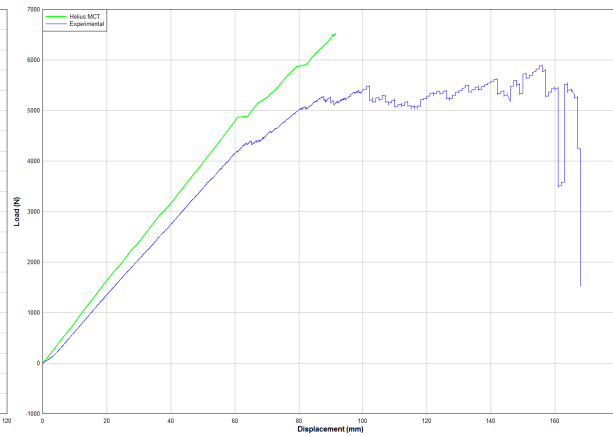


Fig 5. AR Configuration

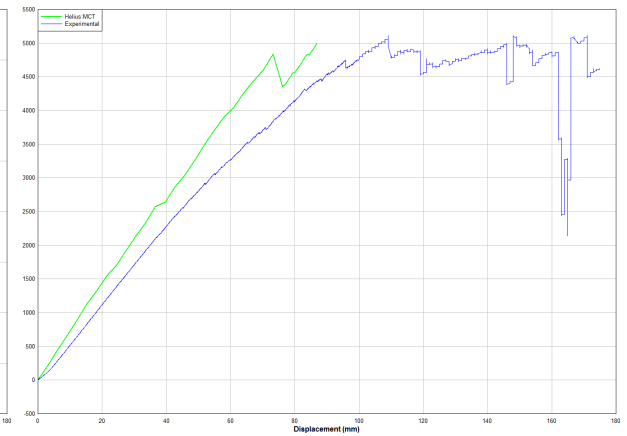


Fig 6. AN Configuration

Helius:MCT Results – Default Parameters

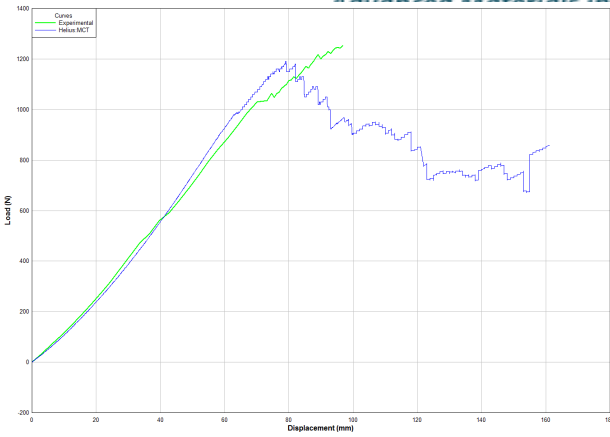


Fig 1. F Configuration

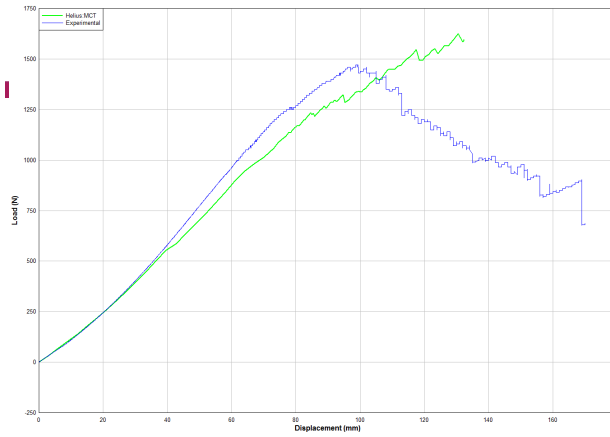


Fig 2. P Configuration

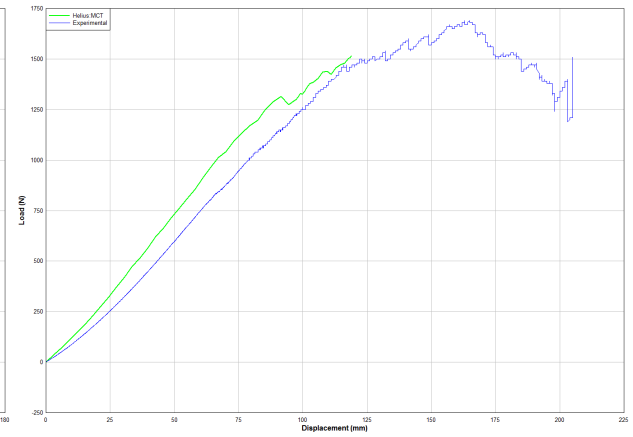


Fig 3. N Configuration

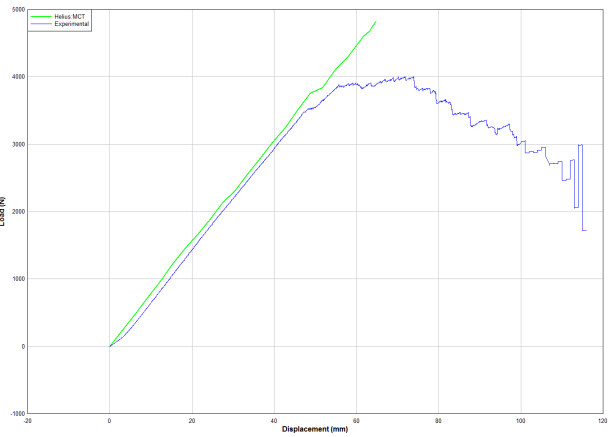


Fig 4. FP Configuration

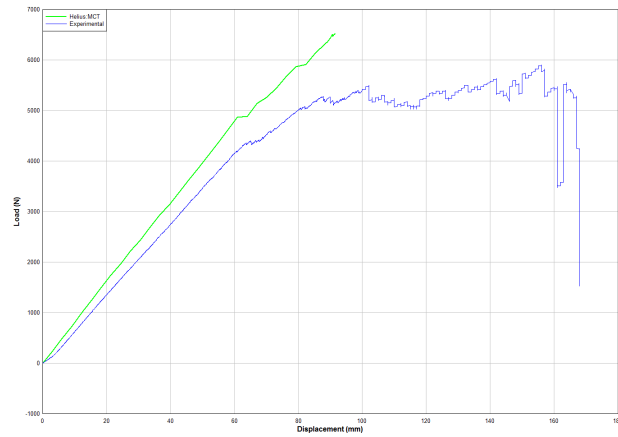


Fig 5. AR Configuration

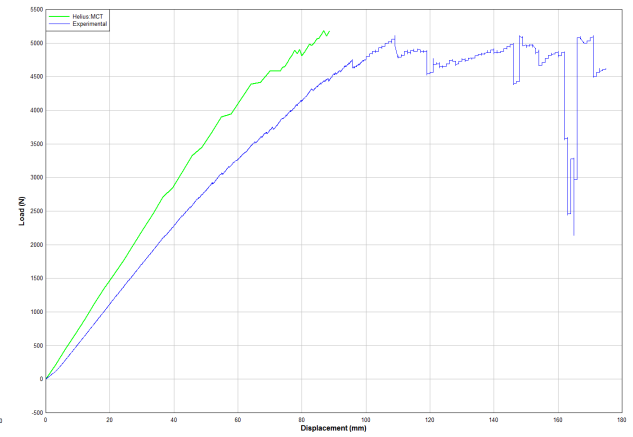
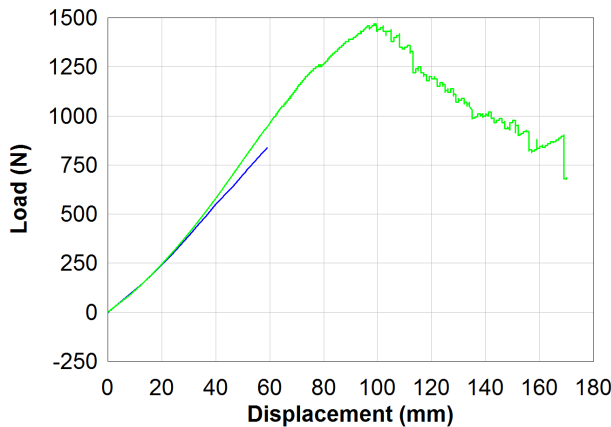
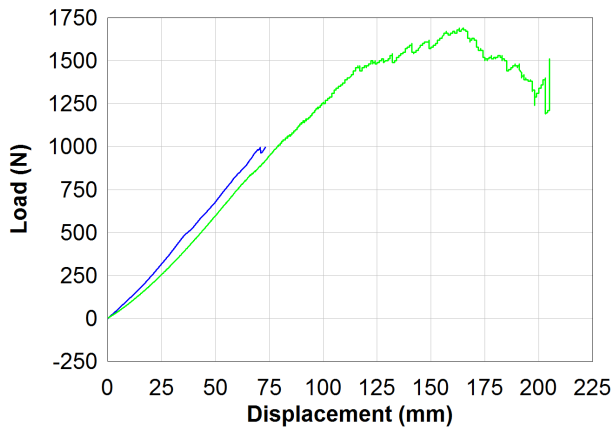
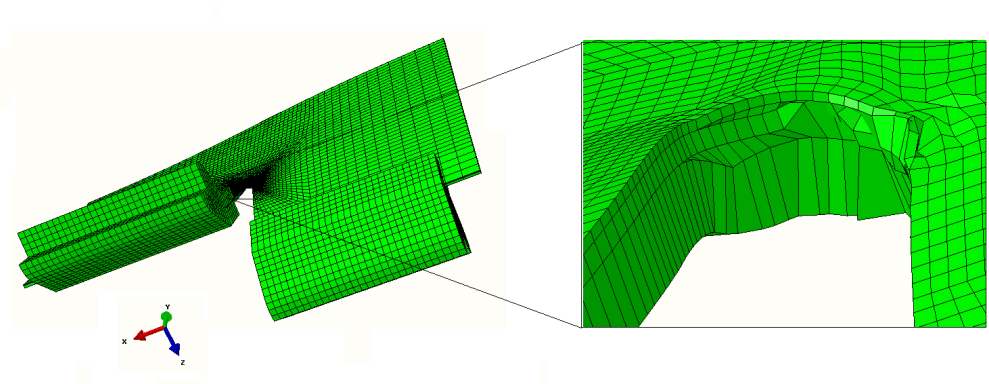
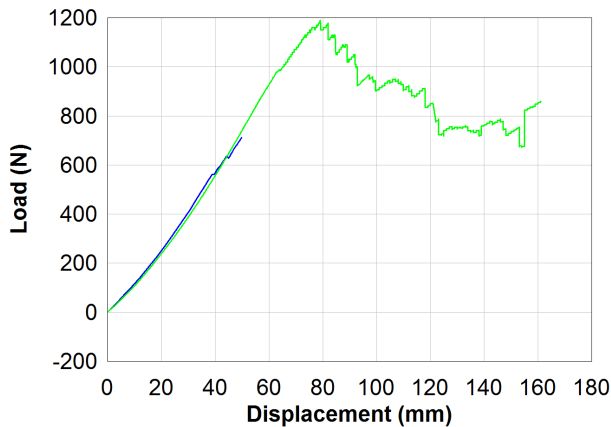


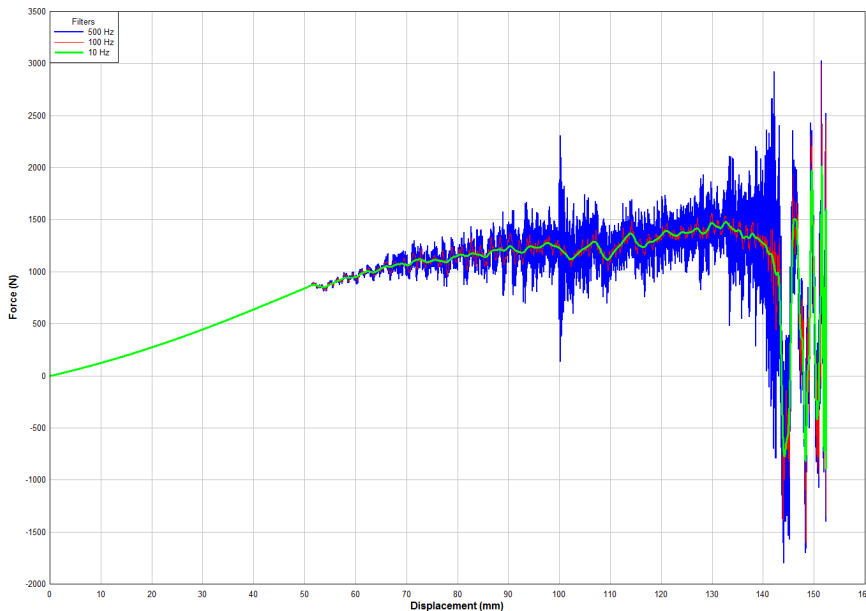
Fig 6. AN Configuration

Cohesive Zones in Helius:MCT



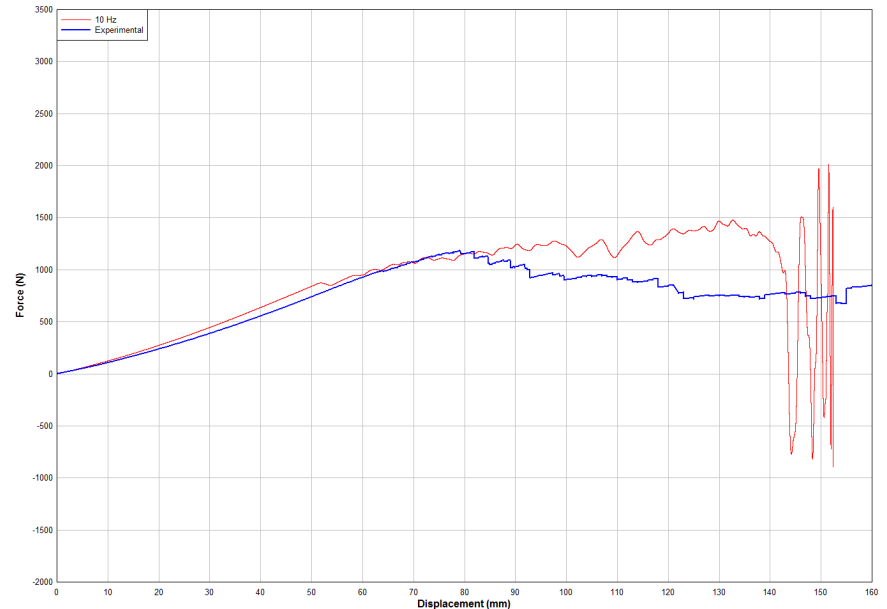
- Cohesive zone runs do not converge
- Deformation in cohesive zone areas can be observed but it is difficult to discern if this deformation is delamination

Filtering Results



Application of filters with varying cut-off frequencies for F-configuration

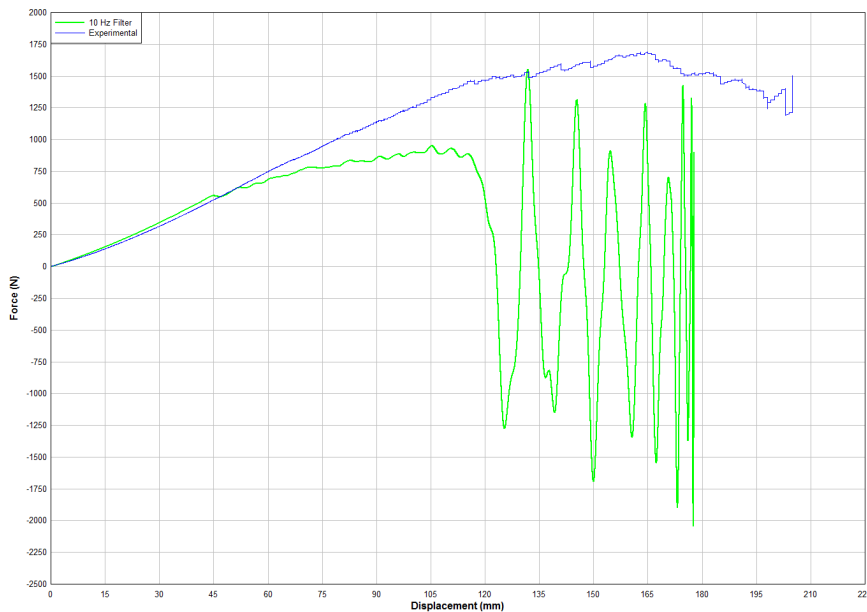
*10% zeros, 20 plies



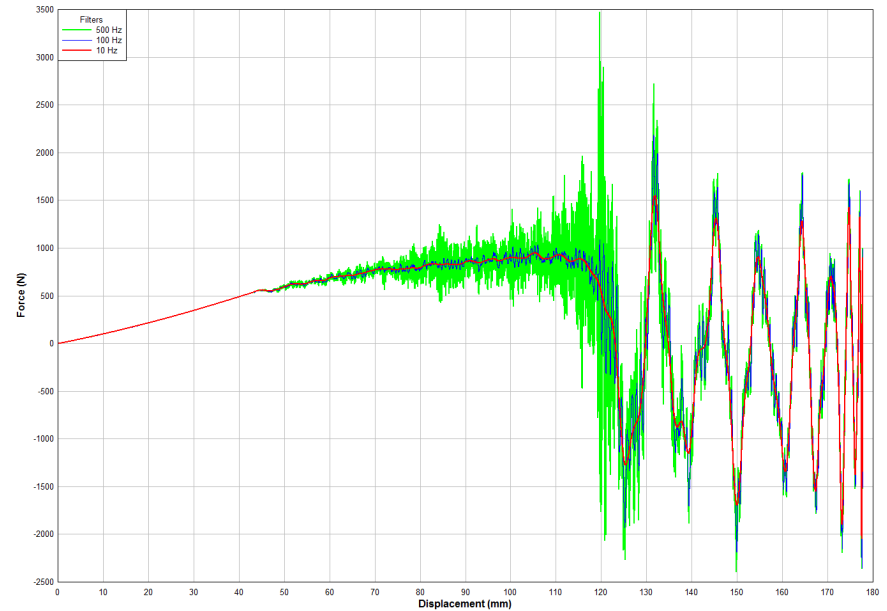
10 Hz cut-off filter compared to experimental results for F-configuration

Filtering Results

*50% zeros, 20 plies

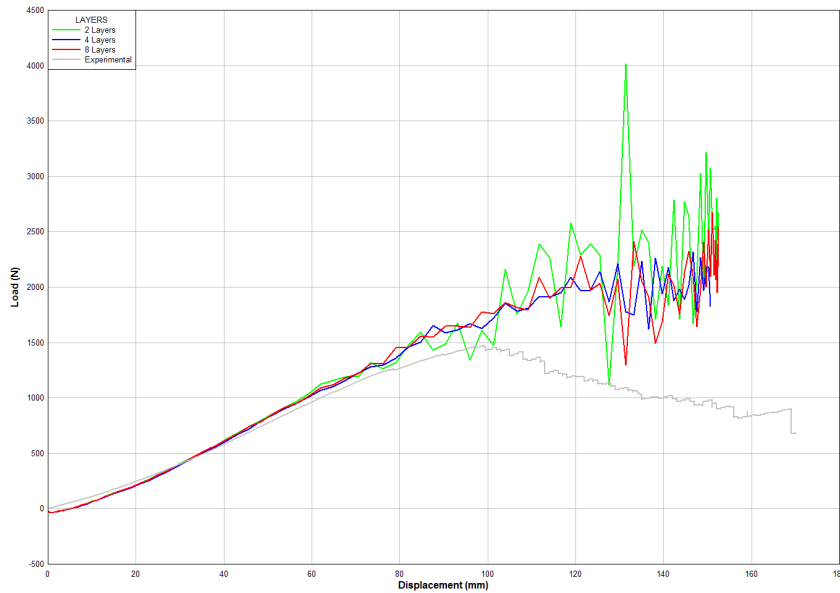


10 Hz cut-off filter compared to experimental results for N-configuration

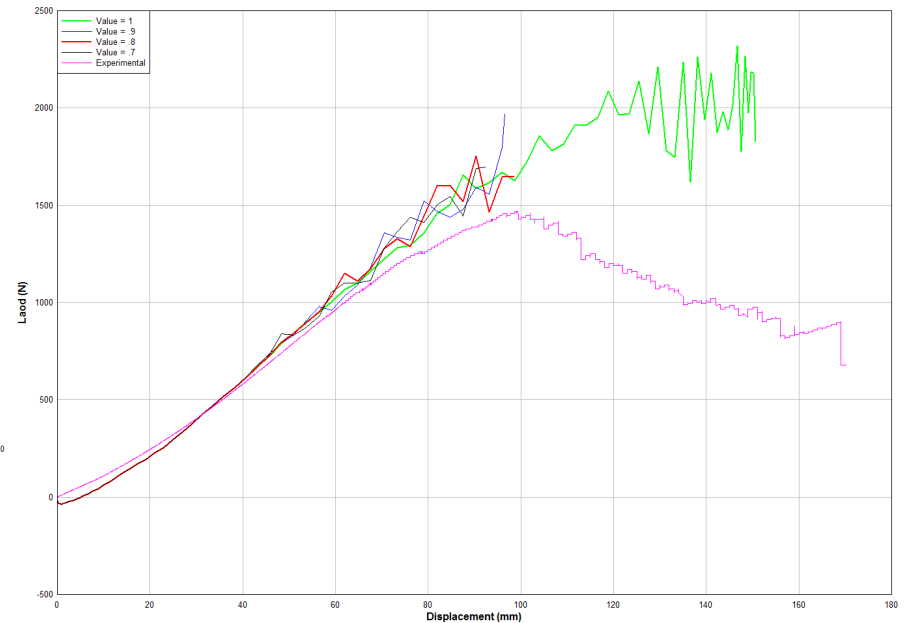


Application of filters with varying cut-off frequencies for N-configuration

More Multi-Layer Results



Multi-Layer Models : 30% zeros, 20 plies configuration



4 layer with varying degradation values:
 30% zeros, 20 plies configuration

Abaqus/Explicit Solver Runtime

- Analyses are extremely long
 - the Explicit solver is only conditionally stable and requires an extremely small time step. Critical time step must be considered:

$$\Delta t \leq \frac{2}{\omega_{max}} \leq \Delta t_{cr}$$

- Need to maintain a Quasi-static state: $E \downarrow K \leq 0.1 E \downarrow I$

Multi-Layer Run Time Table

Table 1. Run Times for Quasi-static models.

Layers (ct.)	Run Time (hr)
2	354
4	672
8	585